

EXERCISE 12(A)

1. In each of the following, check whether or not the given ratios form a proportion:

(i) 8: 16 and 12: 15

(ii) 16: 28 and 24: 42

(iii) $12 \div 3$ and $8 \div 2$

(iv) 25: 40 and 20: 32

(v) $15 / 18$ and $10 / 12$

Solution:

(i) 8: 16 and 12: 15

The above expression can be written as follows:

$$8: 16 = 8 / 16$$

$$= 1 / 2 \text{ and}$$

$$12: 15 = 12 / 15$$

$$= 4 / 5$$

Since $8: 16 \neq 12: 15$

Therefore they are not in proportion

(ii) 16: 28 and 24: 42

The above expression can be written as follows:

$$16: 28 = 16 / 28$$

$$= 4 / 7 \text{ and}$$

$$24: 42 = 24 / 42$$

$$= 4 / 7$$

Since $16: 28 = 24: 42$

Therefore they form a proportion

(iii) $12 \div 3$ and $8 \div 2$

The above expression can be written as follows:

$$12 \div 3 = 12 / 3$$

$$= 4 \text{ and}$$

$$8 \div 2 = 8 / 2$$

$$= 4$$

Since $12: 3 = 8: 2$

Therefore they form a proportion

(iv) 25: 40 and 20: 32

The above expression can be written as follows:

$$25: 40 = 25 / 40$$

$$= 5 / 8 \text{ and}$$

$$20: 32 = 20 / 32$$

$$= 5 / 8$$

Since $25: 40 = 20: 32$

Therefore they form a proportion

(v) $15 / 18$ and $10 / 12$

$$15 / 18 = 5 / 6 \text{ and}$$

$$10 / 12 = 5 / 6$$

Since $15 / 18 = 10 / 12$

Therefore they form a proportion

2. Find the value of x in each of the following proportions:

(i) $x: 4 = 6: 8$

(ii) $14: x = 7: 9$

(iii) $4: 6 = x: 18$

(iv) $8: 10 = x: 25$

(v) $5: 15 = 4: x$

Solution:

(i) $x: 4 = 6: 8$

The given proportion can be calculated for the value of x as follows:

$$x: 4 = 6: 8$$

$$x / 4 = 6 / 8$$

$$\Rightarrow x \times 8 = 4 \times 6$$

$$\Rightarrow x = (4 \times 6) / 8$$

$$\Rightarrow x = 3$$

Therefore the value of x is 3

(ii) $14: x = 7: 9$

The given proportion can be calculated for the value of x as follows:

$$14: x = 7: 9$$

$$14 / x = 7 / 9$$

$$\Rightarrow x \times 7 = 14 \times 9$$

$$\Rightarrow x = (14 \times 9) / 7$$

$$\Rightarrow x = 18$$

Therefore the value of x is 18

(iii) $4: 6 = x: 18$

The given proportion can be calculated for the value of x as follows:

$$4 / 6 = x / 18$$

$$\Rightarrow x \times 6 = 4 \times 18$$

$$\Rightarrow x = (4 \times 18) / 6$$

$$\Rightarrow x = 12$$

Therefore the value of x is 12

(iv) $8: 10 = x: 25$

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}8 / 10 &= x / 25 \\ \Rightarrow 10 \times x &= 25 \times 8 \\ \Rightarrow x &= (25 \times 8) / 10 \\ \Rightarrow x &= 20\end{aligned}$$

Therefore the value of x is 20

(v) $5: 15 = 4: x$

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}5 / 15 &= 4 / x \\ \Rightarrow 5 \times x &= 15 \times 4 \\ \Rightarrow x &= (15 \times 4) / 5 \\ \Rightarrow x &= 12\end{aligned}$$

Therefore the value of x is 12

3. Find the value of x so that the given four numbers are in proportion:

(i) x, 6, 10 and 15

(ii) x, 4, 15 and 30

(iii) 2, x, 10 and 25

(iv) 4, x, 6 and 18

(v) 9, 12, x and 8

Solution:

(i) x, 6, 10 and 15

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}x: 6: 10: 15 \\ \Rightarrow x \times 15 &= 6 \times 10 \\ \Rightarrow x &= (6 \times 10) / 15 \\ \Rightarrow x &= 60 / 15 \\ \Rightarrow x &= 4\end{aligned}$$

Therefore the value of x is 4

(ii) x, 4, 15 and 30

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}x: 4: 15: 30 \\ \Rightarrow x \times 30 &= 4 \times 15 \\ \Rightarrow x &= (4 \times 15) / 30 \\ \Rightarrow x &= 60 / 30 \\ \Rightarrow x &= 2\end{aligned}$$

Therefore the value of x is 2

(iii) 2, x, 10 and 25

The given proportion can be calculated for the value of x as follows:

$$2: x: 10: 25$$

$$\begin{aligned}\Rightarrow x \times 10 &= 2 \times 25 \\ \Rightarrow x &= (2 \times 25) / 10 \\ \Rightarrow x &= 50 / 10 \\ \Rightarrow x &= 5\end{aligned}$$

Therefore the value of x is 5

(iv) 4, x, 6 and 18

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}4: x: 6: 18 \\ \Rightarrow x \times 6 &= 18 \times 4 \\ \Rightarrow x &= (18 \times 4) / 6 \\ \Rightarrow x &= 72 / 6 \\ \Rightarrow x &= 12\end{aligned}$$

Therefore the value of x is 12

(v) 9, 12, x and 8

The given proportion can be calculated for the value of x as follows:

$$\begin{aligned}9: 12: x: 8 \\ \Rightarrow 12 \times x &= 9 \times 8 \\ \Rightarrow x &= (9 \times 8) / 12 \\ \Rightarrow x &= 72 / 12 \\ \Rightarrow x &= 6\end{aligned}$$

Therefore the value of x is 6

4. The first, second and the fourth terms of a proportion are 6, 18 and 75, respectively. Find its third term

Solution:

Given

First term = 6

Second term = 18

Fourth term = 75

Third term = ?

Let the third term be x

$$\begin{aligned}6: 18: x: 75 \\ \Rightarrow x \times 18 &= 6 \times 75 \\ \Rightarrow x &= (6 \times 75) / 18 \\ \Rightarrow x &= 25\end{aligned}$$

Therefore the value of third term is 25

5. Find the second term of the proportion whose first, third and fourth terms are 9, 8 and 24 respectively.

Solution:

Given

First term = 9

Third term = 8

Fourth term = 24

Second term = ?

Let the second term be x 9: x : 8: 24

$$\Rightarrow x \times 8 = 9 \times 24$$

$$\Rightarrow x = (9 \times 24) / 8$$

$$\Rightarrow x = 216 / 8$$

$$\Rightarrow x = 27$$

Therefore the value of x is 27**6. Find the fourth term of the proportion whose first, second and third terms are 18, 27 and 32 respectively.****Solution:**

Given

First term = 18

Second term = 27

Third term = 32

Fourth term = ?

Let the fourth term be x 18: 27: 32: x

$$\Rightarrow x \times 18 = 32 \times 27$$

$$\Rightarrow x = (32 \times 27) / 18$$

$$\Rightarrow x = 48$$

Therefore the value of x is 48**7. The ratio of the length and the width of a school ground is 5: 2. Find the length, if the width is 40 metres.****Solution:**

Given

The ratio of the length and the width of a school ground = 5: 2

The width of the school ground = 40 metre

Let the length of the school ground be x metre

Hence the length of the ground can be calculated as follows:

Ratio of length to width of a school ground = x : 40

According to the given statement

$$\begin{aligned}5: 2 &= x: 40 \\ \Rightarrow 2 \times x &= 40 \times 5 \\ \Rightarrow x &= (40 \times 5) / 2 \\ \Rightarrow x &= 200 / 2 \\ \Rightarrow x &= 100 \text{ m}\end{aligned}$$

Therefore the length of the school ground is 100 m

8. The ratio of the sale of eggs on a Sunday and that of the whole week at a grocery shop was 2: 9. If the total value of the sale of eggs in the same week was Rs 360, find the value of the sale of eggs that Sunday.

Solution:

Given

Ratio of sale of eggs on a Sunday and whole week at a grocery shop = 2: 9

Total sale of eggs in the same week = Rs 360

Let the sale of eggs on Sunday be x

Hence the sale of eggs on Sunday can be calculated as follows:

$$\begin{aligned}2: 9 &= x: 360 \\ \Rightarrow 9 \times x &= 360 \times 2 \\ \Rightarrow x &= (360 \times 2) / 9 \\ \Rightarrow x &= 720 / 9 \\ \Rightarrow x &= 80\end{aligned}$$

Therefore the value of the sale of eggs on Sunday is of Rs 80

9. The ratio of copper and zinc in an alloy is 9: 8. If the weight of zinc, in the alloy, is 9.6 kg, find the weight of copper in the alloy.

Solution:

Given

Ratio of copper and zinc in an alloy = 9: 8

Weight of zinc in an alloy = 9.6 kg

Let x kg be the weight of copper in the alloy

Hence the weight of copper can be calculated as below

$$\begin{aligned}9: 8 &= x: 9.6 \\ \Rightarrow 8 \times x &= 9 \times 9.6 \\ \Rightarrow x &= (9 \times 9.6) / 8 \\ \Rightarrow x &= 86.4 / 8 \\ \Rightarrow x &= 10.8\end{aligned}$$

Therefore the weight of copper in the alloy is 10.8 kg

10. The ratio of the number of girls to the number of boys in a school is 2: 5. If the

number of boys is 225; find:

- (i) the number of girls in the school
- (ii) the number of students in the school.

Solution:

Given

Ratio of girls to the boys in a school = 2.5

Number of boys in a school = 225

(i) Let x be the number of girls in a school

Hence number of girls in a school can be calculated as follows:

$$2: 5 = x: 225$$

$$\Rightarrow 5 \times x = 2 \times 225$$

$$\Rightarrow x = (2 \times 225) / 5$$

$$\Rightarrow x = 450 / 5$$

$$\Rightarrow x = 90$$

Therefore the number of girls in the school is 90

(ii) Total number of students in a school becomes

Total student = Total boys + Total girls

$$= 225 + 90$$

$$= 315$$

Therefore total number of students in the school is 315

11. In a class 1 out of every 5 students pass. If there are 225 students in all the sections of a class, find how many pass?

Solution:

Given

Total number of students in all the sections of a class = 225

And 1 out of every 5 students pass

So, total number of pass students can be calculated as follows:

$$\text{Total student pass} = 225 \times 1 / 5$$

$$= 45$$

Therefore total pass students are 45

12. Make set of all possible proportions from the numbers 15, 18, 35 and 42

Solution:

Given

Numbers are 15, 18, 35 and 42

Hence the possible proportions are as follows:

(i) $15: 18:: 35: 42$

(ii) $15: 35:: 18: 42$

(iii) $42: 18:: 35: 15$

(iv) $42: 35:: 18: 15$

