

### EXERCISE 12(C)

**1. Are the following numbers in proportion:**

(i) 32, 40, 48 and 60?

(ii) 12, 15, 18 and 20?

**Solution:**

(i) 32, 40, 48 and 60

Given

Numbers are 32, 40, 48 and 60

If  $32:40 = 48:60$  then the ratios are in continued proportion

Hence we can find out as shown below

$$32:40 = 48:60$$

$$32 \times 60 = 40 \times 48$$

$$1920 = 1920$$

Since they are equal

Therefore they are in continued proportion

(ii) 12, 15, 18 and 20

Given

Numbers are 12, 15, 18 and 20

If  $12:15 = 18:20$  then the ratios are in continued proportion

Hence we can find out as shown below

$$12:15 = 18:20$$

$$12 \times 20 = 15 \times 18$$

$$240 = 270$$

$$240 \neq 270$$

Since they are not equal

Therefore they are not in a continued proportion

**2. Find the value of x in each of the following such that the given numbers are in proportion**

(i) 14, 42, x and 75

(ii) 45, 135, 90 and x

**Solution:**

(i) 14, 42, x and 75

Given

Numbers are 14, 42, x and 75

If  $14:42 = x:75$  then they are in continued proportion

Hence we can find out as shown below

$$14:42 = x:75$$

$$14 \times 75 = x \times 42$$

$$x = (14 \times 75) / 42$$

$$x = 1050 / 42$$

$$x = 25$$

Therefore the value of x is 25

(ii) 45, 135, 90 and x

Given

Numbers are 45, 135, 90 and x

If 45: 135 = 90: x then they are in continued proportion

Hence we can find out value of x as shown below

$$45: 135 = 90: x$$

$$45 \times x = 90 \times 135$$

$$x = (90 \times 135) / 45$$

$$x = 12150 / 45$$

$$x = 270$$

Therefore the value of x is 270

**3. The costs of two articles are in the ratio 7: 4. If the cost of the first article is Rs 2800; find the cost of the second article**

**Solution:**

Given

Costs of two articles are in the ratio = 7: 4

Cost of first article = Rs 2800

Let us assume the cost of second article be x

Hence the value of second article can be calculated as shown below

$$7: 4 = 2800: x$$

$$7 / 4 = 2800 / x$$

$$7 \times x = 2800 \times 4$$

$$x = (2800 \times 4) / 7$$

$$x = 11200 / 7$$

$$x = 1600$$

Therefore the cost of second article is Rs 1600

**4. The ratio of the length and the width of a rectangular sheet of paper is 8: 5. If the width of the sheet is 17.5 cm; find the length**

**Solution:**

Given

Ratio of the length and the width of a rectangular sheet of paper = 8: 5

Width of the sheet = 17.5 cm

Hence the value of length can be calculated as shown below

$$8: 5 = x: 17.5$$

$$8 / 5 = x / 17.5$$

$$5 \times x = 8 \times 17.5$$

$$x = (8 \times 17.5) / 5$$

$$x = 140 / 5$$

$$x = 28$$

Therefore the length of sheet is 28 cm

**5. The ages of A and B are in the ratio 6: 5. If A's age is 18 years, find the age of B.**

**Solution:**

Given

The ages of A and B are in the ratio = 6: 5

Age of A = 18 years

Let the age of B be x years

Hence the value of B's age can be calculated as shown below

$$6: 5 = 18: x$$

$$6 / 5 = 18 / x$$

$$6 \times x = 18 \times 5$$

$$x = (18 \times 5) / 6$$

$$x = 90 / 6$$

$$x = 15$$

Therefore the age of B is 15 years

**6. A sum of Rs 10, 500 is divided among A, B and C in the ratio 5: 6: 4. Find the share of each.**

**Solution:**

Given

Amount divided among A, B and C in the ratio = 5: 6: 4

Total amount divided = Rs 10500

Hence the sum of ratios can be calculated as below

$$\text{Sum of ratios} = 5 + 6 + 4$$

$$= 15$$

Hence the share's of A, B and C can be calculated as below

$$\text{A's share} = \text{Rs } (10500) / 15 \times 5$$

$$= 700 \times 5$$

$$= \text{Rs } 3500$$

$$\text{B's share} = \text{Rs } (10500) / 15 \times 6$$

$$= 700 \times 6$$

$$= 4200$$

$$\begin{aligned}\text{C's share} &= \text{Rs } (10500) / 15 \times 4 \\ &= 700 \times 4 \\ &= \text{Rs } 2800\end{aligned}$$

Therefore the share of A, B and C are Rs 3500, Rs 4200 and Rs 2800

**7. Do the ratios 15 cm to 2 m and 10 sec to 3 minutes form a proportion?**

**Solution:**

Given

$$15 \text{ cm} : 2 \text{ m} :: 10 \text{ sec} : 3 \text{ min}$$

We know that,

$$1 \text{ m} = 100 \text{ cm}$$

$$1 \text{ min} = 60 \text{ sec}$$

$$\text{Hence } 2 \text{ m} = 200 \text{ cm}$$

$$3 \text{ min} = 180 \text{ sec}$$

We can check that they form the proportion or not as shown below:

$$15 : 200 :: 10 : 180$$

$$3 : 40 :: 1 : 180$$

Therefore they do not form the proportion

**8. Do the ratios 2 kg: 80 kg and 25 g: 625 g form a proportion?**

**Solution:**

Given

$$2 \text{ kg} : 80 :: 25 \text{ g} : 625 \text{ g}$$

We can check that they form the proportion or not as shown below

$$2 : 80 :: 25 : 625$$

$$1 : 40 :: 1 : 25$$

Therefore they do not form the proportion

**9. 10 kg sugar cost Rs 350. If x kg sugar of the same kind costs Rs 175, find the value of x**

**Solution:**

Given

$$\text{Cost of 10 kg sugar} = \text{Rs } 350$$

$$\text{Cost of x kg sugar} = \text{Rs } 175$$

The value of x can be calculated as shown below

$$10 \text{ kg} : x \text{ kg} :: 350 : 175$$

$$10 \times 175 = 350 \times x$$

$$350 x = 1750$$

$$x = 1750 / 350$$

$$x = 5$$

Therefore, 5 kg of sugar costs Rs 175

**10. The length of two ropes are in the ratio 7: 5. Find the length of:**

**(i) shorter rope, if the longer one is 22.5 m**

**(ii) longer rope, if the shorter is 9.8 m**

**Solution:**

(i) shorter rope, if the longer one is 22.5 m

Given

Ratio of length of two rope = 7: 5

And longer rope = 22.5 m

Let the shorter rope length be x

Hence, length of shorter rope can be calculated as below

$$7: 5 = 22.5: x$$

$$7x = 22.5 \times 5$$

$$x = (22.5 \times 5) / 7$$

$$x = 112.5 / 7$$

$$x = 16.07 \text{ m}$$

Therefore the length of shorter rope is 16.07 m

(ii) longer rope, if the shorter is 9.8 m

Given

Ratio of length of two rope = 7: 5

And shorter rope = 9.8 m

Let the length of longer rope be x

Hence, the length of longer rope can be calculated as below

$$7: 5 = x: 9.8$$

$$5x = 9.8 \times 7$$

$$x = (9.8 \times 7) / 5$$

$$x = 68.6 / 5$$

$$x = 13.72 \text{ m}$$

Therefore the length of longer rope is 13.72 m

**11. If 4, x and 9 are in continued proportion, find the value of x**

**Solution:**

Given

Numbers are 4, x and 9 are in continued proportion

Hence we can find out value of x as below

$$4: x = x: 9$$

$$x^2 = 9 \times 4$$

$$x = \sqrt{36}$$

$$x = 6$$

Therefore the value of x is 6

**12. If 25, 35 and x are in continued proportion, find the value of x**

**Solution:**

Given

Numbers are 25, 35 and x are in continued proportion

Hence we can find out value of x as below

$$25: 35 = 35: x$$

$$25 \times x = 35 \times 35$$

$$x = (35 \times 35) / 25$$

$$x = 1225 / 25$$

$$x = 49$$

Therefore the value of x is 49