

Exercise 3.2

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Solve the following system of equations graphically: 1. x + y = 3 2x + 5y = 12Solution:

> Given, x + y = 3..... (i) 2x + 5y = 12.... (ii)

For equation (i), When y = 0, we have x = 3When x = 0, we have y = 3Thus we have the following table giving points on the line x + y = 3

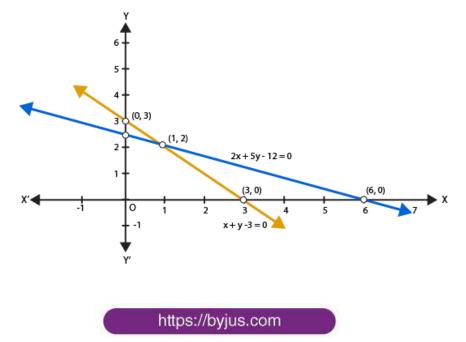
Х	0	3
У	3	0

For equation (ii), We solve for y: \Rightarrow y = (12 - 2x)/5 So, when x = 1 y = (12 - 2(1))/5 = 2 And, when x = 6

 $\Rightarrow y = (12 - 2(6))/5 = 0$

Thus we have the following table giving points on the line 2x + 5y = 12

x	1	6
У	2	0





Clearly the two lines intersect at a single point P (1, 2)Hence, x= 1 and y = 2

2. x - 2y = 52x + 3y = 10Solution:

> Given, x - 2y = 5..... (i) 2x + 3y = 10..... (ii)

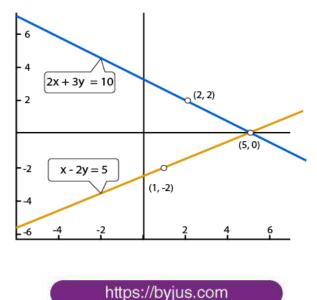
For equation (i), $\Rightarrow y = (x - 5)/2$ When y = 0, we have x = 5When x = 1, we have y = -2Thus we have the following table giving points on the line x - 2y = 5

Х	5	
У	0	-2

For equation (ii), We solve for y: \Rightarrow y = (10 - 2x)/3

So, when x = 5 y = (10 - 2(5))/3 = 0And, when x = 2 $\Rightarrow y = (10 - 2(2))/3 = 2$ Thus we have the following table giving points on the line 2x + 3y = 10

X	5	2
у	0	2





Clearly the two lines intersect at a single point P (5, 0)Hence, x=5 and y=0

3. 3x+ y + 1 = 0 2x - 3y + 8 = 0 Solution:

> Given, 3x+y+1=0 (i) 2x - 3y + 8 = 0..... (ii)

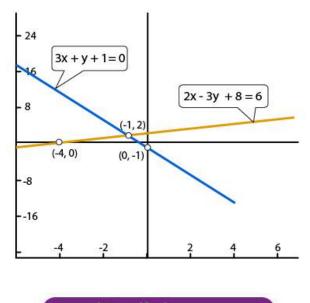
For equation (i), $\Rightarrow y = -(1 + 3x)$ When x = 0, we have y = -1 When x = -1, we have y = 2 Thus we have the following table giving points on the line 3x + y + 1 = 0

Х	-1	0
у	2	-1

For equation (ii), We solve for y: $\Rightarrow y = (2x + 8)/3$ So, when x = -4 y = (2(-4) + 8)/3 = 0And, when x = -1 $\Rightarrow y = (2(-1) + 8)/3 = 2$ Thus we have the following table giving points on the line 2x - 3y + 8 = 0x = -4

Х	-4	-1
у	0	2

Graph of the equations (i) and (ii) is as below:





Clearly the two lines intersect at a single point P (-1, 2) Hence, x = -4 and y = 0

4. 2x + y - 3 = 0 2x - 3y - 7 = 0 Solution:

Given,

2x + y - 3 = 0..... (i) 2x - 3y - 7 = 0..... (ii)

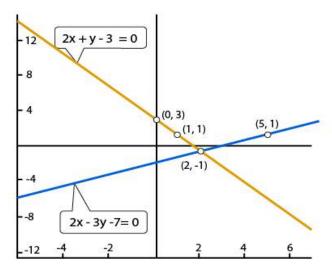
For equation (i), $\Rightarrow y = (3 - 2x)$ When x = 0, we have y = (3 - 2(0)) = 3When x = 1, we have y = (3 - 2(1)) = 1Thus we have the following table giving points on the line 2x + y - 3 = 0

Х	0	
У	3	1

For equation (ii), We solve for y: $\Rightarrow y = (2x - 7)/3$ So, when x = 2 y = (2(2) - 7)/3 = -1And, when x = 5 $\Rightarrow y = (2(5) - 7)/3 = 1$ Thus we have the following table giving points on the line 2x - 3y - 7 = 0x = 2

X	2	5
У	-1	1

Graph of the equations (i) and (ii) is as below:





Clearly the two lines intersect at a single point P (2, -1)Hence, x=2 and y=-1

5. x + y = 6 x - y = 2 Solution:

Given, x + y = 6.....(i)x - y = 2....(ii)

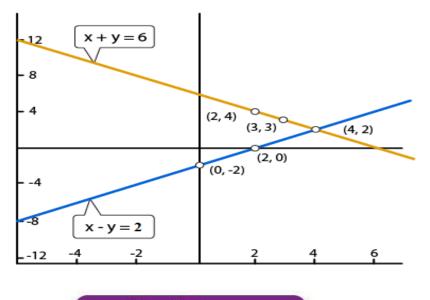
For equation (i), $\Rightarrow y = (6 - x)$ When x = 2, we have y = (6 - 2)) = 4 When x = 3, we have y = (6 - 3) = 3 Thus we have the following table giving points on the line x + y = 6

Х	2	3
у	4	3

For equation (ii), We solve for y: $\Rightarrow y = (x - 2)$ So, when x = 2 y = (0 - 2) = -2And, when x = 5 $\Rightarrow y = (2 - 2) = 0$ Thus we have the following table giving points on the line x - y = 2x = 0

X	0	2
у	-2	0

Graph of the equations (i) and (ii) is as below:





Clearly the two lines intersect at a single point P (4, 2) Hence, x=4 and y=2

6. x - 2y = 63x - 6y = 0 Solution:

> Given, x - 2y = 6..... (i) 3x - 6y = 0..... (ii)

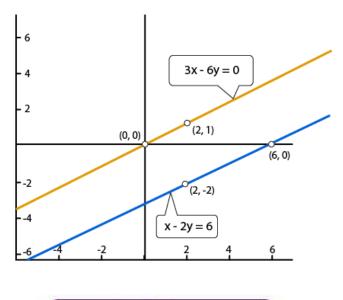
For equation (i), $\Rightarrow y = (x - 6)/2$ When x = 2, we have y = (2 - 6)/2 = -2When x = 0, we have y = (0 - 6)/2 = -3Thus we have the following table giving points on the line x - 2y = 6

Х	2	0
у	-2	-3

For equation (ii), We solve for y: $\Rightarrow y = x/2$ So, when x = 0 y = 0/2 = 0And, when x = 2 $\Rightarrow y = 2/2 = 1$ Thus we have the following table giving points on the line 3x - 6y = 0x 0

X	0	2
у	0	1

Graph of the equations (i) and (ii) is as below:





2

2

0

-1

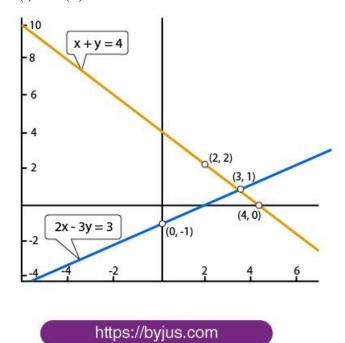
Clearly the two lines are parallel to each other. So, the two lines do not intersect. Hence, the given system has no solutions.

7. x + y = 42x - 3y = 3 Solution:

> Given, x + y = 4..... (i) 2x - 3y = 3..... (ii)

For equation (i), $\Rightarrow y = (4 - x)$ When x = 4, we have y = (4 - 4) = 0When x = 2, we have y = (4 - 2) = 2Thus we have the following table giving points on the line x + y = 4 $\hline x \qquad 4 \qquad 0$

For equation (ii), We solve for y: $\Rightarrow y = (2x - 3)/3$ So, when x = 3 y = (2(3) - 3)/3 = 1And, when x = 0 $\Rightarrow y = (2(0) - 3)/3 = -1$ Thus we have the following table giving points on the line 2x - 3y = 3x 3 y 1





Clearly the two lines intersect at a single point P (3, 1)Hence, x=3 and y=1

8. 2x + 3y = 4x - y + 3 = 0Solution:

> Given, 2x + 3y = 4.....(i) x - y + 3 = 0.....(ii)

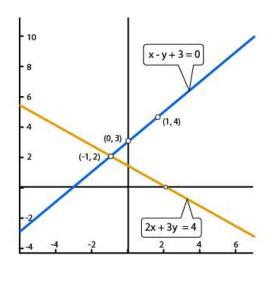
For equation (i), $\Rightarrow y = (4 - 2x)/3$ When x = -1, we have y = (4 - 2(-1))/3 = 2 When x = 2, we have y = (4 - 2(2))/3 = 0 Thus we have the following table giving points on the line 2x + 3y = 4

X	-1	2
у	2	0

For equation (ii), We solve for y: $\Rightarrow y = (x + 3)$ So, when x = 0 y = (0 + 3) = 3And, when x = 1 $\Rightarrow y = (1 + 3) = 4$ Thus we have the following table giving points on the line x - y + 3 = 0 x 0

Х	0	1
у	3	4

Graph of the equations (i) and (ii) is as below:





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Clearly the two lines intersect at a single point P (-1, 2) Hence, x = -1 and y = 2
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9. 2x - 3y + 13 = 0
3x - 2y + 12 = 0
Solution:
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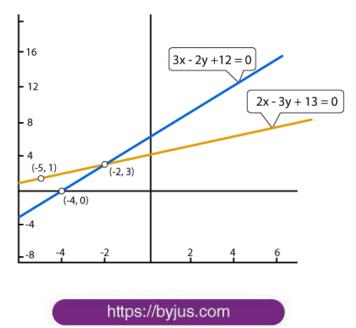
Given, 2x - 3y + 13 = 0..... (i) 3x - 2y + 12 = 0..... (ii)

For equation (i), $\Rightarrow y = (2x + 13)/3$ When x = -5, we have y = (2(-5) + 13))/3 = 1 When x = -2, we have y = (2(-2) + 13))/3 = 3 Thus we have the following table giving points on the line 2x - 3y + 13 = 0

Х	-5	-2
у	1	3

For equation (ii), We solve for y: $\Rightarrow y = (3x + 12)/2$ So, when x = -4 y = (3(-4) + 12)/2 = 0And, when x = -2 $\Rightarrow y = (3(-2) + 12)/2 = 3$ Thus we have the following table giving points on the line 3x - 2y + 12 = 0x -4

Х	-4	-2
у	0	3





-1

-1

Clearly the two lines intersect at a single point P (-2, 3) Hence, x = -2 and y = 3

10. 2x + 3y + 5 = 03x + 2y - 12 = 0Solution:

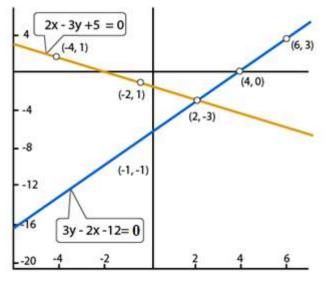
Given, 2x + 3y + 5 = 0.....(i) 3x - 2y - 12 = 0.....(ii)

For equation (i), $\Rightarrow y = -(2x + 5) / 3$ When x = -4, we have y = -(2(-4) + 5))/3 = 1When x = -2, we have y = -(2(-2) + 5))/3 = -1Thus we have the following table giving points on the line 2x + 3y + 5 = 0 $\boxed{\begin{array}{c|c} x & -4 \\ y & 1 \end{array}}$

For equation (ii), We solve for y: $\Rightarrow y = (3x - 12)/2$ So, when x = 4 y = (3(4) - 12)/2 = 0And, when x = 6 $\Rightarrow y = (3(6) - 12)/2 = 3$ Thus we have the following table giving points on the line 3x - 2y - 12 = 0x 4

x	4	6
у	0	3

Graph of the equations (i) and (ii) is as below:





Clearly the two lines intersect at a single point P (2, -3)Hence, x=2 and y=-3

Show graphically that each one of the following systems of equation has infinitely many solution: 11. 2x + 3y = 64x + 6y = 12

Solution:

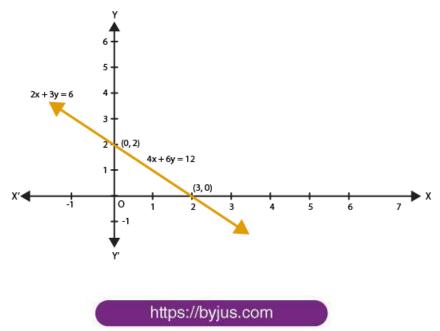
Given, 2x + 3y = 6..... (i) 4x + 6y = 12..... (ii)

For equation (i), $\Rightarrow y = (6 - 2x)/3$ When x = 0, we have y = (6 - 2(0))/3 = 2 When x = 3, we have y = (6 - 2(3))/3 = 0 Thus we have the following table giving points on the line 2x + 3y = 6

X	0	3
У	2	0

For equation (ii), We solve for y: $\Rightarrow y = (12 - 4x)/6$ So, when x = 0 y = (12 - 4(0))/6 = 2And, when x = 3 $\Rightarrow y = (12 - 4(3))/6 = 0$ Thus we have the following table giving points on the line 4x + 6y = 12

Х	0	3
у	2	0





Thus, the graphs of the two equations are coincident. Hence, the system of equations has infinitely many solutions.

12. x - 2y = 53x - 6y = 15Solution:

Given,

x - 2y = 5.....(i)3x - 6y = 15....(ii)

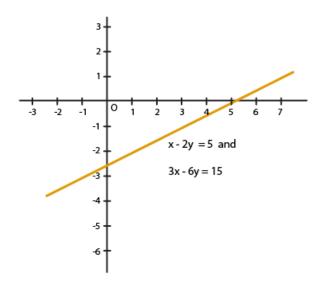
For equation (i), $\Rightarrow y = (x - 5)/2$ When x = 3, we have y = (3 - 5)/2 = -1 When x = 5, we have y = (5 - 5)/2 = 0 Thus we have the following table giving points on the line x - 2y = 5 x

Х	3	5
У	-1	0

For equation (ii), We solve for y: $\Rightarrow y = (3x - 15)/6$ So, when x = 1 y = (3(1) - 15)/6 = -2And, when x = -1 $\Rightarrow y = (3(-1) - 15)/6 = -3$ Thus we have the following table giving points on the line 3x - 6y = 15

x	1	-1
у	-2	-3

Graph of the equations (i) and (ii) is as below:





3

-1

Thus, the graphs of the two equations are coincident.

Hence, the system of equations has infinitely many solutions.

13. 3x + y = 86x + 2y = 16Solution:

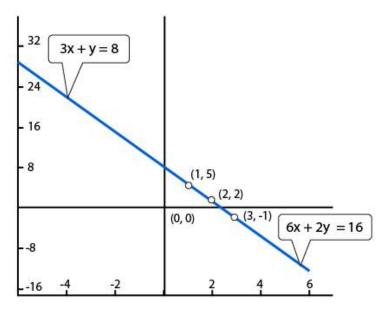
> Given, 3x + y = 8.....(i)6x + 2y = 16....(ii)

For equation (i), $\Rightarrow y = (8 - 3x)$ When x = 2, we have y = (8 - 3(2)) = 2 When x = 3, we have y = (8 - 3(3)) = -1 Thus we have the following table giving points on the line 3x + y = 8 $\boxed{\begin{array}{c|c} x & 2 \\ y & 2 \end{array}}$

For equation (ii), We solve for y: $\Rightarrow y = (16 - 6x)/2$ So, when x = 3 y = (16 - 6(3))/2 = -1And, when x = 1 $\Rightarrow y = (16 - 6(1))/2 = 5$ Thus we have the following table giving points on the line 6x + 2y = 16x 3 1

X	3	1
у	-1	5
	1 1	

Graph of the equations (i) and (ii) is as below:





Thus, the graphs of the two equations are coincident. Hence, the system of equations has infinitely many solutions.

14. x - 2y + 11 = 03x + 6y + 33 = 0Solution:

Given, x - 2y + 11 = 0..... (i) 3x - 6y + 33 = 0..... (ii)

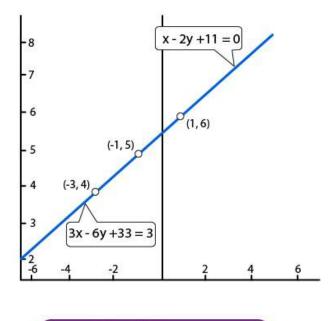
For equation (i), $\Rightarrow y = (x + 11)/2$ When x = -1, we have y = (-1 + 11)/2 = 5 When x = -3, we have y = (-3 + 11)/2 = 4 Thus we have the following table giving points on the line x - 2y + 11 = 0

Х	-1	-3
У	5	4

For equation (ii), We solve for y: $\Rightarrow y = (3x + 33)/6$ So, when x = 1 y = (3(1) + 33)/6 = 6And, when x = -1 $\Rightarrow y = (3(-1) + 33)/6 = 5$ Thus we have the following table giving points on the line 3x - 6y + 33 = 0

x	1	-1
у	6	5

Graph of the equations (i) and (ii) is as below:





Thus, the graphs of the two equations are coincident. Hence, the system of equations has infinitely many solutions.

Show graphically that each one of the following systems of equations is in-consistent (i.e has no solution):

15. 3x - 5y = 206x - 10y = -40Solution:

> Given, 3x - 5y = 20.....(i)6x - 10y = -40.....(ii)

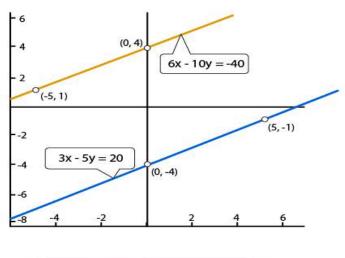
For equation (i), $\Rightarrow y = (3x - 20)/5$ When x = 5, we have y = (3(5) - 20)/5 = -1 When x = 0, we have y = (3(0) - 20)/5 = -4 Thus we have the following table giving points on the line 3x - 5y = 20

Х	5	0
У	-1	-4

For equation (ii), We solve for y: $\Rightarrow y = (6x + 40)/10$ So, when x = 0 y = (6(0) + 40)/10 = 4And, when x = -5 $\Rightarrow y = (6(-5) + 40)/10 = 1$ Thus we have the following table giving points on the line 6x - 10y = -40

х	0	-5
у	4	1

Graph of the equations (i) and (ii) is as below:





2

-2

It is clearly seen that, there is no common point between these two lines. Hence, the given systems of equations is in-consistent.

16. x - 2y = 63x - 6y = 0Solution:

> Given, x - 2y = 6....(i)3x - 6y = 0.....(ii)

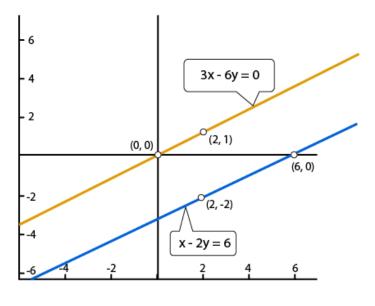
For equation (i), \Rightarrow y = (x - 6)/2 When x = 6, we have y = (6 - 6)/2 = 0When x = 2 we have y = (2 - 6)/2 = -2Thus we have the following table giving points on the line x - 2y = 66 Х 0

For equation (ii), We solve for y: \Rightarrow y = x/2 So, when x = 0y = 0/2 = 0And, when x = 2 \Rightarrow y = 2/2 = 1 Thus we have the following table giving points on the line 3x - 6y = 0

x	0	2
у	0	1

Graph of the equations (i) and (ii) is as below:

у





-1

4

-1

3

It is clearly seen that, there is no common point between these two lines. Hence, the given systems of equations is in-consistent.

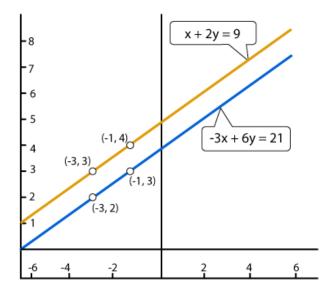
17. 2y - x = 96y - 3x = 21Solution:

Given, 2y - x = 9.....(i) 6y - 3x = 21.....(ii)

For equation (ii), We solve for y: $\Rightarrow y = (21 + 3x)/6$ So, when x = -3 y = (21 + 3(-3))/6 = 2And, when x = -1 $\Rightarrow y = (21 + 3(-1))/6 = 3$ Thus we have the following table giving points on the line 6y - 3x = 21x -3

		у	2		1	2	
0	C .1	. •	(*)	1 /			

Graph of the equations (i) and (ii) is as below:





3

2

3

It is clearly seen that, there is no common point between these two lines. Hence, the given systems of equations is in-consistent.

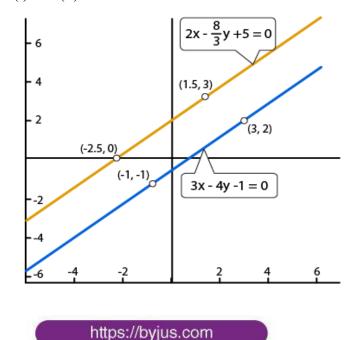
18. 3x - 4y - 1 = 02x - (8/3)y + 5 = 0Solution:

Given, 3x - 4y - 1 = 0.....(i) 2x - (8/3)y + 5 = 0.....(ii)

For equation (i), $\Rightarrow y = (3x - 1)/4$ When x = -1, we have y = (3(-1) - 1)/4= -1 When x = 3, we have y = (3(3) - 1)/4= 2 Thus we have the following table giving points on the line 3x - 4y - 1 = 0 x -1y -1

For equation (ii), We solve for y: $\Rightarrow y = (6x + 15)/8$ So, when x = -2.5 y = (6(-2.5) + 15)/8 = 0And, when x = 1.5 $\Rightarrow y = (6(1.5) + 15)/8 = 3$ Thus we have the following table giving points on the line 2x - (8/3)y + 5 = 0 x - 2.51.5

Graph of the equations (i) and (ii) is as below:



0



It is clearly seen that, there is no common point between these two lines. Hence, the given systems of equations is in-consistent.

19. Determine graphically the vertices of the triangle, the equations of whose sides are given below:

(i) 2y - x = 8, 5y - x = 14 and y - 2x = 1Solution:

> Given, 2y - x = 8..... (i) 5y - x = 14.... (ii) y - 2x = 1.... (iii)

For equation (i), $\Rightarrow y = (x + 8)/2$ When x = -4, we have y = (-4 + 8)/2 = 2 When x = 0, we have y = (0 + 8)/2 = 4 Thus we have the following table giving points on the line 2y - x = 8

Х	-4	0	
у	2	4	

For equation (ii), We solve for y: \Rightarrow y = (x + 14)/5

So, when x = -4 y = ((-4) + 14)/5 = 2And, when x = 1 $\Rightarrow y = (1 + 14)/5 = 3$ Thus we have the following table giving points on the line 5y - x = 14

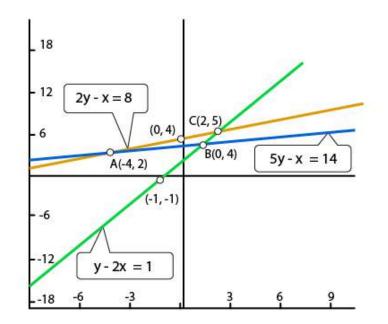
Х	-4	l
у	2	3

1

3

Finally, for equation (iii), $\Rightarrow y = (2x + 1)$ When x = -1, we have y = (2(-1) + 1) = -1 When x = 1, we have y = (2(1) + 1) = 3 Thus we have the following table giving points on the line y - 2x = 1 $\boxed{\begin{array}{c|c} x & -1 \\ y & 1 \end{array}}$





From the above graph, we observe that the lines taken in pairs intersect at points A(-4,2), B(1,3) and C(2,5)

Hence the vertices of the triangle are A(-4, 2), B(1, 3) and C(2,5)

(ii) y = x, y = 0 and 3x + 3y = 10Solution:

Given,

y = x (i) y = 0 (ii) 3x + 3y = 10...... (iii)

For equation (i), When x = 1, we have y = 1When x = -2, we have y = -2Thus we have the following table giving points on the line y = x

Х	1	-2
у	1	-2

10/3

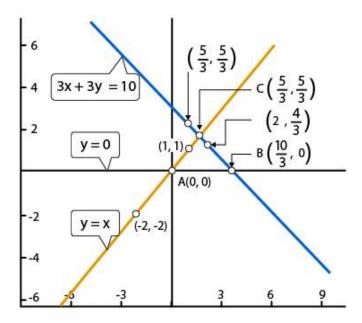
10/3

For equation (ii), When x = 0 y = 0And, when x = 10/3 $\Rightarrow y = 0$ Thus we have the following table giving points on the line y = 0 $\hline x \qquad 0$ $y \qquad 0$



Finally, for equation (iii),				
\Rightarrow y = (10 - 3x)/3				
When $x = 1$, we have $y = (10 - 3(1))/3) = 7/3$				
When $x = 2$, we have $y = (10 - 3(2))/3 = 4/3$				
Thus we have the following table giving points on the line $3x + 3y = 10$				
X	1	2		
V	7/3	4/3		

Graph of the equations (i), (ii) and (iii) is as below:



From the above graph, we observe that the lines taken in pairs intersect at points A(0,0) B(10/3,0) and C(5/3, 5/3)

Hence the vertices of the triangle are A(0,0) B(10/3,0) and C(5/3, 5/3).

20. Determine graphically whether the system of equations x - 2y = 2, 4x - 2y = 5 is consistent or in-consistent. Solution:

Given, x - 2y = 2..... (i) 4x - 2y = 5..... (ii) For equation (i), $\Rightarrow y = (x - 2)/2$ When x = 2, we have y = (2 - 2)/2 = 0When x = 0, we have y = (0 - 2)/2 = -1



Thus we have the following table giving points on the line x - 2y = 2

Х	2	0
у	0	-1

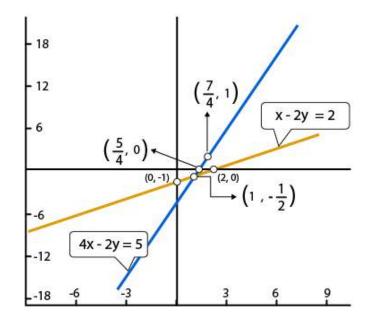
For equation (ii), We solve for x: $\Rightarrow x = (5 + 2y)/4$

So, when y = 0x = (5 + 2(0))/4 = 5/4And, when y = 1.5 \Rightarrow x = (5 + 2(1))/4 = 7/4

Thus we have the following table giving points on the line 4x - 2y = 5

Х	5/4	7/4
у	0	1

Graph of the equations (i) and (ii) is as below:



It is clearly seen that the two lines intersect at (1,0) Hence, the system of equations is consistent.

21. Determine by drawing graphs, whether the following system of linear equation has a unique solution or not:

(i) 2x - 3y = 6 and x + y = 1 Solution:

Given,



1

2x - 3y = 6 (i) x + y = 1..... (ii)

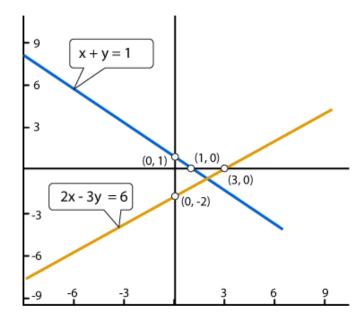
For equation (i), $\Rightarrow y = (2x - 6)/3$ When x = 3, we have y = (2(3) - 6)/3 = 0 When x = 0, we have y = (2(0) - 6)/3 = -2 Thus we have the following table giving points on the line 2x - 3y = 6x = 3 = 0 y = 0 = -2For equation (ii)

For equation (ii), We solve for y: \Rightarrow y = (1 - x)

So, when x = 0 y = (1 - 0) = 1And, when x = 1 $\Rightarrow y = (1 - 1) = 0$ Thus we have the following table giving points on the line x + y = 1x = 0

X	0	l
У		0

Graph of the equations (i) and (ii) is as below:



It's seen clearly that the two lines intersect at one.

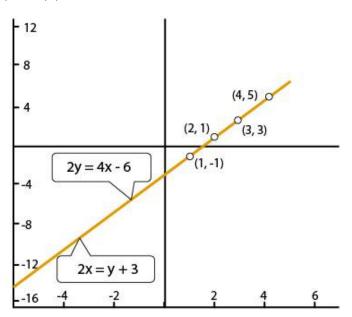
Thus, we can conclude that the system of equations has a unique solution.



(ii) 2y = 4x - 6 and 2x = y + 3 Solution:

Given, 2y = 4x - 6(i) 2x = y + 3(ii)		
For equation (i), \Rightarrow y = (4x - 6)/2 When x = 1, we have y = (4(1) - 6)	/2 = -1	
When $x = 4$, we have $y = (4(4) - 6)$		
• • • • • • •	giving points on the line $2y = 4x - 6$	
Х	1	4
У	-1	5
For equation (ii), We solve for y: $\Rightarrow y = 2x - 3$ So, when $x = 2$ y = 2(2) - 3 = 1 And, when $x = 3$ $\Rightarrow y = 2(3) - 3 = 3$ Thus we have the following table g	giving points on the line $2x = y + 3$	
Х	2	3
у		3

Graph of the equations (i) and (ii) is as below:



We see that the two lines are coincident. And, hence it has infinitely many solutions. Therefore, the system of equations does not have a unique solution.