

**EXERCISE 33.2****PAGE NO: 33.15**

**1. A coin is tossed. Find the total number of elementary events and also the total number of events associated with the random experiment.**

**Solution:**

Given: A coin is tossed.

When a coin is tossed, there will be two possible outcomes, Head (H) and Tail (T).

Since, the no. of elementary events is 2 {H, T}

We know, if there are  $n$  elements in a set, then the number of total element in its subset is  $2^n$ .

So, the total number of the experiment is 4,

There are 4 subset of  $S = \{H\}, \{T\}, \{H, T\}$  and  $\Phi$

$\therefore$  There are total 4 events in a given experiment.

**2. List all events associated with the random experiment of tossing of two coins. How many of them are elementary events?**

**Solution:**

Given: Two coins are tossed once.

We know, when two coins are tossed then the no. of possible outcomes are  $2^2 = 4$

So, the Sample spaces are {HH, HT, TT, TH}

$\therefore$  There are total 4 events associated with the given experiment.

**3. Three coins are tossed once. Describe the following events associated with this random experiment:**

**A = Getting three heads, B = Getting two heads and one tail, C = Getting three tails, D = Getting a head on the first coin.**

**(i) Which pairs of events are mutually exclusive?**

**(ii) Which events are elementary events?**

**(iii) Which events are compound events?**

**Solution:**

Given: There are three coins tossed once.

When three coins are tossed, then the sample spaces are:

$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$

So, according to the question,

$A = \{HHH\}$

$B = \{HHT, HTH, THH\}$

$C = \{TTT\}$

$D = \{HHH, HHT, HTH, HTT\}$

$$\begin{aligned}\text{Now, } A \cap B &= \Phi, \\ A \cap C &= \Phi, \\ A \cap D &= \{HHH\}\end{aligned}$$

$$\begin{aligned}B \cap C &= \Phi, \\ B \cap D &= \{HHT, HTH\}\end{aligned}$$

$$C \cap D = \Phi$$

We know that, if the intersection of two sets are null or empty it means both the sets are Mutually Exclusive.

(i) Events A and B, Events A and C, Events B and C and events C and D are mutually exclusive.

(ii) Here, We know, if an event has only one sample point of a sample space, then it is called elementary events.

So, A and C are elementary events.

(iii) If there is an event that has more than one sample point of a sample space, it is called a compound event.

Since,  $B \cap D = \{HHT, HTH\}$

So, B and D are compound events.

**4. In a single throw of a die describe the following events:**

(i) A = Getting a number less than 7

(ii) B = Getting a number greater than 7

(iii) C = Getting a multiple of 3

(iv) D = Getting a number less than 4

(v) E = Getting an even number greater than 4.

(vi) F = Getting a number not less than 3.

Also, find  $A \cup B$ ,  $A \cap B$ ,  $B \cap C$ ,  $E \cap F$ ,  $D \cap F$  and  $\bar{F}$ .

**Solution:**

Given: A dice is thrown once.

Let us find the given events, and also find  $A \cup B$ ,  $A \cap B$ ,  $B \cap C$ ,  $E \cap F$ ,  $D \cap F$  and  $\bar{F}$ .

$$S = \{1, 2, 3, 4, 5, 6\}$$

According to the subparts of the question, we have certain events as:

(i) A = getting a number below 7

So, the sample spaces for A are:

$$A = \{1, 2, 3, 4, 5, 6\}$$

(ii) B = Getting a number greater than 7

So, the sample spaces for B are:

$$B = \{\Phi\}$$

(iii) C = Getting multiple of 3

So, the Sample space of C is

$$C = \{3, 6\}$$

(iv) D = Getting a number less than 4

So, the sample space for D is

$$D = \{1, 2, 3\}$$

(v) E = Getting an even number greater than 4.

So, the sample space for E is

$$E = \{6\}$$

(vi) F = Getting a number not less than 3.

So, the sample space for F is

$$F = \{3, 4, 5, 6\}$$

Now,

$$A = \{1, 2, 3, 4, 5, 6\} \text{ and } B = \{\Phi\}$$

$$A \cup B = \{1, 2, 3, 4, 5, 6\}$$

$$A = \{1, 2, 3, 4, 5, 6\} \text{ and } B = \{\Phi\}$$

$$A \cap B = \{\Phi\}$$

$$B = \{\Phi\} \text{ and } C = \{3, 6\}$$

$$B \cap C = \{\Phi\}$$

$$F = \{3, 4, 5, 6\} \text{ and } E = \{6\}$$

$$E \cap F = \{6\}$$

$$E = \{6\} \text{ and } D = \{1, 2, 3\}$$

$$D \cap E = \{\Phi\}$$

And, for  $\bar{F} = S - F$

$S = \{1, 2, 3, 4, 5, 6\}$  and  $F = \{3, 4, 5, 6\}$

$\bar{F} = \{1, 2\}$

∴ These are the events for given experiment.

### 5. Three coins are tossed. Describe

- (i) two events A and B which are mutually exclusive.
- (ii) three events A, B and C which are mutually exclusive and exhaustive.
- (iii) two events A and B which are not mutually exclusive.
- (iv) two events A and B which are mutually exclusive but not exhaustive.

**Solution:**

Given: Three coins are tossed.

When three coins are tossed, then the sample space is

$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$

Now, the subparts are:

(i) The two events which are mutually exclusive are when,

A: getting no tails

B: getting no heads

Then,  $A = \{HHH\}$  and  $B = \{TTT\}$

So, the intersection of this set will be null. Or, the sets are disjoint.

(ii) Three events which are mutually exclusive and exhaustive are:

A: getting no heads

B: getting exactly one head

C: getting at least two head

So,  $A = \{TTT\}$   $B = \{TTH, THT, HTT\}$  and  $C = \{HHH, HHT, HTH, THH\}$

Since,  $A \cap B = B \cap C = C \cap A = \Phi$  and

$A \cup B \cup C = S$

(iii) The two events that are not mutually exclusive are:

A: getting three heads

B: getting at least 2 heads

So,  $A = \{HHH\}$   $B = \{HHH, HHT, HTH, THH\}$

Hence,  $A \cap B = \{HHH\} = \Phi$

(iv) The two events which are mutually exclusive but not exhaustive are:

A: getting exactly one head

B: getting exactly one tail

So,  $A = \{HTT, THT, TTH\}$  and  $B = \{HHT, HTH, THH\}$

It is because  $A \cap B = \Phi$  but  $A \cup B \neq S$

**6. A die is thrown twice. Each time the number appearing on it is recorded. Describe the following events:**

(i) **A = Both numbers are odd.**

(ii) **B = Both numbers are even**

(iii) **C = sum of the numbers is less than 6.**

**Also, find  $A \cup B$ ,  $A \cap B$ ,  $A \cup C$ ,  $A \cap C$ . Which pairs of events are mutually exclusive?**

**Solution:**

Given: A dice is thrown twice. And each time number appearing on it is recorded.

When the dice is thrown twice then the number of sample spaces are  $6^2 = 36$

Now,

The possibility both odd numbers are:

$A = \{(1, 1), (1, 3), (1, 5), (3, 1), (3, 3), (3, 5), (5, 1), (5, 3), (5, 5)\}$

Since, possibility of both even numbers is:

$B = \{(2, 2), (2, 4), (2, 6), (4, 2), (4, 4), (4, 6), (6, 2), (6, 4), (6, 6)\}$

And, possible outcome of sum of the numbers is less than 6.

$C = \{(1, 1)(1, 2)(1, 3)(1, 4)(2, 1)(2, 2)(2, 3)(3, 1)(3, 2)(4, 1)\}$

Hence,

$(A \cup B) = \{(1, 1), (1, 3), (1, 5), (3, 1), (3, 3), (3, 5), (5, 1), (5, 3), (5, 5), (2, 2)(2, 4)(2, 6)(4, 2)(4, 4)(4, 6)(6, 2)(6, 4)(6, 6)\}$

$(A \cap B) = \{\Phi\}$

$(A \cup C) = \{(1, 1), (1, 3), (1, 5), (3, 1), (3, 3), (3, 5), (5, 1), (5, 3), (5, 5), (1, 2)(1, 4)(2, 1)(2, 2)(2, 3)(3, 1)(3, 2)(4, 1)\}$

$(A \cap C) = \{(1, 1), (1, 3), (3, 1)\}$

$\therefore (A \cap B) = \Phi$  and  $(A \cap C) \neq \Phi$ , A and B are mutually exclusive, but A and C are not.