

Exercise 5(A)

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1. Find which of the following equations are quadratic: (i) $(3x - 1)^2 = 5(x + 8)$ (ii) $5x^2 - 8x = -3(7 - 2x)$ (iii) (x - 4) (3x + 1) = (3x - 1) (x + 2)(iv) $x^2 + 5x - 5 = (x - 3)^2$ (v) $7x^3 - 2x^2 + 10 = (2x - 5)^2$ (vi) $(x - 1)^2 + (x + 2)^2 + 3(x + 1) = 0$ Solution:

Solution:

(i) $(3x - 1)^2 = 5(x + 8)$ $\Rightarrow (9x^2 - 6x + 1) = 5x + 40$ $\Rightarrow 9x^2 - 11x - 39 = 0$; which is of the general form $ax^2 + bx + c = 0$. Thus, the given equation is a quadratic equation.

- (ii) $5x^2 8x = -3(7 2x)$ $\Rightarrow 5x^2 - 8x = 6x - 21$ $\Rightarrow 5x^2 - 14x + 21 = 0$; which is of the general form $ax^2 + bx + c = 0$. Thus, the given equation is a quadratic equation.
- (iii) (x 4) (3x + 1) = (3x 1) (x + 2) $\Rightarrow 3x^2 + x - 12x - 4 = 3x^2 + 6x - x - 2$ $\Rightarrow 16x + 2 = 0$; which is not of the general form $ax^2 + bx + c = 0$. And it's a linear equation. Thus, the given equation is not a quadratic equation.
- (iv) $x^2 + 5x 5 = (x 3)^2$ $\Rightarrow x^2 + 5x - 5 = x^2 - 6x + 9$ $\Rightarrow 11x - 14 = 0$; which is not of the general form $ax^2 + bx + c = 0$. And it's a linear equation. Thus, the given equation is not a quadratic equation.
- (v) $7x^3 2x^2 + 10 = (2x 5)^2$ $\Rightarrow 7x^3 - 2x^2 + 10 = 4x^2 - 20x + 25$ $\Rightarrow 7x^3 - 6x^2 + 20x - 15 = 0$; which is not of the general form $ax^2 + bx + c = 0$. And it's a cubic equation. Thus, the given equation is not a quadratic equation.

(vi) $(x - 1)^2 + (x + 2)^2 + 3(x + 1) = 0$ $\Rightarrow x^2 - 2x + 1 + x^2 + 4x + 4 + 3x + 3 = 0$ $\Rightarrow 2x^2 + 5x + 8 = 0$; which is of the general form $ax^2 + bx + c = 0$. Thus, the given equation is a quadratic equation.

2. (i) Is x = 5 a solution of the quadratic equation $x^2 - 2x - 15 = 0$? Solution:

Given quadratic equation, $x^2 - 2x - 15 = 0$



We know that, for x = 5 to be a solution of the given quadratic equation it should satisfy the equation. Now, on substituting x = 5 in the given equation, we have

L.H.S = $(5)^2 - 2(5) - 15$ = 25 - 10 - 15 = 0 = R.H.S

Therefore, x = 5 is a solution of the given quadratic equation $x^2 - 2x - 15 = 0$

(ii) Is x = -3 a solution of the quadratic equation $2x^2 - 7x + 9 = 0$? Solution:

Given quadratic equation, $2x^2 - 7x + 9 = 0$

We know that, for x = -3 to be solution of the given quadratic equation it should satisfy the equation. Now, on substituting x = 5 in the given equation, we have L.H.S = $2(-3)^2 - 7(-3) + 9$

= 18 + 21 + 9 = 48

$$\neq$$
 R.H.S

Therefore, x = -3 is not a solution of the given quadratic equation $2x^2 - 7x + 9 = 0$.



Exercise 5(B)

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1. Without solving, comment upon the nature of roots of each of the following equations: (i) $7x^2 - 9x + 2 = 0$ (ii) $6x^2 - 13x + 4 = 0$ (iii) $25x^2 - 10x + 1 = 0$ (iv) $x^2 + 2\sqrt{3}x - 9 = 0$ (v) $x^2 - ax - b^2 = 0$ (vi) $2x^2 + 8x + 9 = 0$

Solution:

(i) Given quadratic equation, $7x^2 - 9x + 2 = 0$ Here, a = 7, b = -9 and c = 2So, the Discriminant (D) = $b^2 - 4ac$ D = $(-9)^2 - 4(7)(2)$ = 81 - 56= 25As D > 0, the roots of the equation is real and unequal.

(ii) Given quadratic equation, $6x^2 - 13x + 4 = 0$ Here, a = 6, b = -13 and c = 4So, the Discriminant (D) $= b^2 - 4ac$ $D = (-13)^2 - 4(6)(4)$ = 169 - 96= 73As D > 0, the roots of the equation is real and unequal.

(iii) Given quadratic equation, $25x^2 - 10x + 1 = 0$ Here, a = 25, b = -10 and c = 1So, the Discriminant (D) $= b^2 - 4ac$ $D = (-10)^2 - 4(25)(1)$ = 100 - 100= 0As D = 0, the roots of the equation is real and equal.

(iv) Given quadratic equation, $x^2 + 2\sqrt{3x} - 9 = 0$ Here, a = 1, $b = 2\sqrt{3}$ and c = -9So, the Discriminant (D) $= b^2 - 4ac$ D $= (2\sqrt{3})^2 - 4(1)(-9)$ = 12 + 36= 48As D > 0, the roots of the equation is real and unequal.

(v) Given quadratic equation, $x^2 - ax - b^2 = 0$ Here, a = 1, b = -a and $c = -b^2$ So, the Discriminant (D) $= b^2 - 4ac$ $D = (a)^2 - 4(1)(-b^2)$ $= a^2 + 4b^2$ $a^2 + 4b^2$ is always positive value.



Thus D > 0, and the roots of the equation is real and unequal

(vi) Given quadratic equation, $2x^2 + 8x + 9 = 0$ Here, a = 2, b = 8 and c = 9So, the Discriminant (D) $= b^2 - 4ac$ D $= (8)^2 - 4(2)(9)$ = 64 - 72= -8As D < 0, the equation has no roots.

2. Find the value of 'p', if the following quadratic equations has equal roots: (i) $4x^2 - (p - 2)x + 1 = 0$ (ii) $x^2 + (p - 3)x + p = 0$

Solution:

- (i) $4x^2 (p 2)x + 1 = 0$ Here, a = 4, b = -(p - 2), c = 1Given that the roots are equal, So, Discriminant = $0 \Rightarrow b^2 - 4ac = 0$ $D = (-(p - 2))^2 - 4(4)(1) = 0$ $\Rightarrow p^2 + 4 - 4p - 16 = 0$ $\Rightarrow p^2 - 4p - 12 = 0$ $\Rightarrow p^2 - 6p + 2p - 12 = 0$ $\Rightarrow p(p - 6) + 2(p - 6) = 0$ $\Rightarrow p + 2 = 0$ or p - 6 = 0Hence, p = -2 or p = 6
- (ii) $x^{2} + (p 3)x + p = 0$ Here, a = 1, b = (p - 3), c = pGiven that the roots are equal, So, Discriminant = $0 \Rightarrow b^{2}-4ac = 0$ $D = (p - 3)^{2} - 4(1)(p) = 0$ $\Rightarrow p^{2} + 9 - 6p - 4p = 0$ $\Rightarrow p^{2}-10p + 9 = 0$ $\Rightarrow p^{2}-9p - p + 9 = 0$ $\Rightarrow p(p - 9) - 1(p - 9) = 0$ $\Rightarrow (p - 9)(p - 1) = 0$ $\Rightarrow p - 9 = 0$ or p - 1 = 0Hence, p = 9 or p = 1



Exercise 5(C)

Solve equations, number 1 to 20, given below, using factorization method: 1. $x^2 - 10x - 24 = 0$ Solution:

Given equation, $x^2 - 10x - 24 = 0$ $x^2 - 12x + 2x - 24 = 0$ x(x - 12) + 2(x - 12) = 0 (x + 2)(x - 12) = 0So, x + 2 = 0 or x - 12 = 0Hence, x = -2 or x = 12

2. $x^2 - 16 = 0$ Solution:

Given equation, $x^2 - 16 = 0$ $x^2 + 4x - 4x + 16 = 0$ x(x + 4) -4(x + 4) = 0 (x - 4) (x + 4) = 0So, (x - 4) = 0 or (x + 4) = 0Hence, x = 4 or x = -4

3. $2x^2 - \frac{1}{2}x = 0$ Solution:

Given equation, $2x^2 - \frac{1}{2}x = 0$ $4x^2 - x = 0$ x(4x - 1) = 0So, either x = 0 or 4x - 1 = 0Hence, x = 0 or $x = \frac{1}{4}$

4. x(x - 5) = 24 Solution:

Given equation, x(x - 5) = 24 $x^{2} - 5x = 24$ $x^{2} - 5x - 24 = 0$ $x^{2} - 8x + 3x - 24 = 0$ x(x - 8) + 3(x - 8) = 0 (x + 3)(x - 8) = 0So, x + 3 = 0 or x - 8 = 0Hence, Page No: 59



x = -3 or x = 8

5. $9/2 = 5 + x^2$ Solution:

Given equation, $9/2 = 5 + x^2$ On multiplying by 2 both sides, we have $9x = 2(5 + x^2)$ $9x = 10 + 2x^2$ $2x^2 - 9x + 10 = 0$ $2x^2 - 4x - 5x + 10 = 0$ 2x(x - 2) - 5(x - 2) = 0(2x - 5)(x - 2) = 0So, 2x - 5 = 0 or x - 2 = 0Hence, x = 5/2 or x = 2

6. 6/x = 1 + x Solution:

Given equation, 6/x = 1 + xOn multiplying by x both sides, we have 6 = x(1 + x) $6 = x + x^2$ $x^2 + x - 6 = 0$ $x^2 + 3x - 2x - 6 = 0$ x(x + 3) - 2(x + 3) = 0(x - 2) (x + 3) = 0So, x - 2 = 0 or x + 3 = 0Hence, x = 2 or x = -3

7. x = (3x + 1)/ 4x Solution:

Given equation, x = (3x + 1)/4xOn multiplying by 4x both sides, we have 4x(x) = 3x + 1 $4x^2 = 3x + 1$ $4x^2 - 3x - 1 = 0$ $4x^2 - 4x + x - 1 = 0$ 4x(x - 1) + 1(x - 1) = 0(4x + 1) (x - 1) = 0So, 4x + 1 = 0 or x - 1 = 0Hence, x = -1/4 or x = 1



8. x + 1/x = 2.5 Solution:

Given equation, x + 1/x = 2.5 x + 1/x = 5/2Taking LCM on L.H.S, we have $(x^2 + 1)/x = 5/2$ $2(x^2 + 1) = 5x$ $2x^2 + 2 = 5x$ $2x^2 - 5x + 2 = 0$ $2x^2 - 4x - x + 2 = 0$ 2x(x - 2) -1(x - 2) = 0 (2x - 1)(x - 2) = 0So, 2x - 1 = 0 or x - 2 = 0Hence, $x = \frac{1}{2}$ or x = 2

9. $(2x - 3)^2 = 49$ Solution:

Given equation, $(2x - 3)^2 = 49$ Expanding the L.H.S, we have $4x^2 - 12x + 9 = 49$ $4x^2 - 12x - 40 = 0$ Dividing by 4 on both side $x^2 - 3x - 10 = 0$ $x^2 - 5x + 2x - 10 = 0$ x(x - 5) + 2(x - 5) = 0(x + 2) (x - 5) = 0So, x + 2 = 0 or x - 5 = 0Hence, x = -2 or 5

10. $2(x^2 - 6) = 3(x - 4)$ Solution:

Given equation, $2(x^2 - 6) = 3(x - 4)$ $2x^2 - 12 = 3x - 12$ $2x^2 = 3x$ x(2x - 3) = 0So, x = 0 or (2x - 3) = 0Hence, x = 0 or x = 3/2

11. (x + 1) (2x + 8) = (x + 7) (x + 3)



Solution:

Given equation, (x + 1) (2x + 8) = (x + 7) (x + 3) $2x^{2} + 2x + 8x + 8 = x^{2} + 7x + 3x + 21$ $2x^{2} + 10x + 8 = x^{2} + 10x + 21$ $x^{2} = 21 - 8$ $x^{2} - 13 = 0$ $(x - \sqrt{13}) (x + \sqrt{13}) = 0$ So, $x - \sqrt{13} = 0$ or $x + \sqrt{13} = 0$ Hence, $x = -\sqrt{13}$ or $x = \sqrt{13}$

12. $x^2 - (a + b)x + ab = 0$ Solution:

Given equation, $x^2 - (a + b)x + ab = 0$ $x^2 - ax - bx + ab = 0$ x(x - a) - b(x - a) = 0 (x - b) (x - a) = 0So, x - b = 0 or x - a = 0Hence, x = b or x = a

13. $(x + 3)^2 - 4(x + 3) - 5 = 0$ Solution:

Given equation, $(x + 3)^2 - 4(x + 3) - 5 = 0$ $(x^2 + 9 + 6x) - 4x - 12 - 5 = 0$ $x^2 + 2x - 8 = 0$ $x^2 + 4x - 2x - 8 = 0$ x(x + 4) - 2(x - 4) = 0 (x - 2)(x + 4) = 0So, x - 2 = 0 or x + 4 = 0Hence, x = 2 or x = -4

14. $4(2x - 3)^2 - (2x - 3) - 14 = 0$ Solution:

Given equation, $4(2x - 3)^2 - (2x - 3) - 14 = 0$ Let substitute 2x - 3 = yThen the equation becomes, $4y^2 - y - 14 = 0$ $4y^2 - 8y + 7y - 14 = 0$ 4y(y - 2) + 7(y - 2) = 0(4y + 7)(y - 2) = 0



So, 4y + 7 = 0 or y - 2 = 0Hence, y = -7/4 or y = 2But we have taken y = 2x - 3Thus, 2x - 3 = -7/4 or 2x - 3 = 22x = 5/4 or 2x = 5x = 5/8 or x = 5/2

15. 3x - 2/2x - 3 = 3x - 8/x + 4Solution:

Given equation, 3x - 2/2x - 3 = 3x - 8/x + 4On cross-multiplying we have, (3x - 2)(x + 4) = (3x - 8)(2x - 3) $3x^2 - 2x + 12x - 8 = 6x^2 - 16x - 9x + 24$ $3x^2 + 10x - 8 = 6x^2 - 25x + 24$ $3x^2 - 35x + 32 = 0$ $3x^2 - 3x - 32x + 32 = 0$ 3x(x - 1) - 32(x - 1) = 0(3x - 32)(x - 1) = 0 So, 3x - 32 = 0 or x - 1 = 0Hence, x = 32/3 or x = 1

16. $2x^2 - 9x + 10 = 0$, when: (i) $x \in N$ (ii) $x \in Q$ Solution:

Given equation, $2x^2 - 9x + 10 = 0$ $2x^2 - 4x - 5x + 10 = 0$ 2x(x - 2) - 5(x - 2) = 0 (2x - 5)(x - 2) = 0So, 2x - 5 = 0 or x - 2 = 0Hence, x = 5/2 or x = 2(i) When $x \in N$ x = 2 is the solution.

(ii) When $x \in Q$ x = 2, 5/2 are the solutions

$$17. \quad \frac{x-3}{x+3} + \frac{x+3}{x-3} = 2\frac{1}{2}$$

Solution:



$$\frac{x-3}{x+3} + \frac{x+3}{x-3} = 2\frac{1}{2}$$

$$\Rightarrow \frac{(x-3)^2 + (x+3)^2}{(x+3)(x-3)} = \frac{5}{2}$$

$$\Rightarrow \frac{x^2 - 6x + 9 + x^2 + 6x + 9}{x^2 - 9} = \frac{5}{2}$$

$$2(2x^2 + 18) = 5(x^2 - 9)$$

$$4x^2 + 36 = 5x^2 - 45$$

$$x^2 - 81 = 0$$

$$(x - 9)(x + 9) = 0$$
So, $x - 9 = 0$ or $x + 9 = 0$
Hence,
 $x = 9$ or $x = -9$



Exercise 5(D)

Solve, each of the following equations, using the formula:
 (i) x² - 6x = 27
 Solution:

Given equation, $x^2 - 6x = 27$ $x^2 - 6x - 27 = 0$ Here, a = 1, b = -6 and c = -27By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(-27)}}{2(1)}$$

$$x = \frac{6 \pm \sqrt{36 - -108}}{2}$$

$$x = \frac{6 \pm \sqrt{144}}{2}$$

$$x = \frac{6 \pm 12}{2}$$

$$x = \frac{6 \pm 12}{2}$$

$$x = \frac{18}{2} \quad x = -\frac{6}{2}$$

$$x = 9$$

$$x = -3$$
Therefore, x = 9 or -3

(ii) $x^2 - 10x + 21 = 0$ Solution:

Given equation, $x^2 - 10x + 21 = 0$ Here, a = 1, b = -10 and c = 21By quadratic formula, we have Page No: 59



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(1)(21)}}{2(1)}$$

$$x = \frac{10 \pm \sqrt{100 - 84}}{2}$$

$$x = \frac{10 \pm \sqrt{16}}{2}$$

$$x = \frac{10 \pm \sqrt{16}}{2}$$

$$x = \frac{10 \pm 4}{2}$$

$$x = \frac{14}{2} \quad x = \frac{6}{2}$$

$$x = 7 \quad x = 3$$
Therefore, x = 7 or x = 3

(iii) $x^2 + 6x - 10 = 0$ Solution:

Given equation, $x^2 + 6x - 10 = 0$ Here, a = 1, b = 6 and c = -10By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-6 \pm \sqrt{6^2 - 4(1)(-10)}}{2(1)}$$

$$x = \frac{-6 \pm \sqrt{36 - -40}}{2}$$

$$x = \frac{-6 \pm \sqrt{76}}{2}$$

$$x = \frac{-6 \pm 2\sqrt{19}}{2}$$

$$x = \frac{-6 \pm 2\sqrt{19}}{2}$$

$$x = -3 \pm \sqrt{19}$$
Therefore, $x = -3 \pm \sqrt{19}$ or $x = -3 - \sqrt{19}$



(iv) $x^2 + 2x - 6 = 0$ Solution:

Given equation, $x^2 + 2x - 6 = 0$ Here, a = 1, b = 2 and c = -6By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-2 \pm \sqrt{2^2 - 4(1)(-6)}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{4 - -24}}{2}$$

$$x = \frac{-2 \pm \sqrt{28}}{2}$$

$$x = \frac{-2 \pm 2\sqrt{7}}{2}$$

$$x = \frac{-2 \pm 2\sqrt{7}}{2}$$

$$x = -1 \pm \sqrt{7}$$
Therefore, x = -1 + $\sqrt{7}$ or x = -1 - $\sqrt{7}$

(v) $3x^2 + 2x - 1 = 0$ Solution:

Given equation, $3x^2 + 2x - 1 = 0$ Here, a = 3, b = 2 and c = -1By quadratic formula, we have





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Therefore, x = 1/3 or x = -1
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(vi) $2x^2 + 7x + 5 = 0$ Solution:

Given equation, $2x^2 + 7x + 5 = 0$ Here, a = 2, b = 7 and c = 5By quadratic formula, we have







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Therefore, x = -1 or x = -5/2
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(vii) $2/3 x = -1/6 x^2 - 1/3$ Solution:

Given equation, $2/3 x = -1/6 x^2 - 1/3$ $1/6 x^2 + 2/3 x + 1/3 = 0$ Multiplying by 6 on both sides $x^2 + 4x + 2 = 0$ Here, a = 1, b = 4 and c = 2By quadratic formula, we have





Therefore, $x = -2 + \sqrt{2}$ or $x = -2 - \sqrt{2}$

(viii) $1/15 x^2 + 5/3 = 2/3 x$ Solution:

Given equation, $1/15 x^2 + 5/3 = 2/3 x$ $1/15 x^2 - 2/3 x + 5/3 = 0$ Multiplying by 15 on both sides $x^2 - 10x + 25 = 0$ Here, a = 1, b = -10 and c = 25By quadratic formula, we have



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(1)(25)}}{2(1)}$$

$$x = \frac{10 \pm \sqrt{100 - 100}}{2}$$

$$x = \frac{10 \pm \sqrt{0}}{2}$$

$$x = \frac{10}{2}$$

$$x = 5$$
Therefore, x = 5 (equal roots)
(ix) x^2 - 6 = 2 \sqrt{2} x
Solution:
Given equation, x^2 - 6 = 2 $\sqrt{2} x$
Solution:
Given equation, x^2 - 6 = 2 $\sqrt{2} x$

$$x^2 - 2\sqrt{2} x - 6 = 0$$
Here, a = 1, b = $-2\sqrt{2}$ and c = -6
By quadratic formula, we have
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-2\sqrt{2}) \pm \sqrt{(-2\sqrt{2})^2 - 4(1)(-6)}}{2(1)}$$

$$= \frac{2\sqrt{2} \pm \sqrt{32}}{2} = \frac{2\sqrt{2} \pm 4\sqrt{2}}{2} = \frac{2\sqrt{2} \pm 4\sqrt{2}}{2} \text{ and } \frac{2\sqrt{2} - 4\sqrt{2}}{2}$$

$$= \frac{6\sqrt{2}}{2} \text{ and } \frac{-2\sqrt{2}}{2} = 3\sqrt{2} \text{ and } -\sqrt{2}$$
Therefore, x = $3\sqrt{2}$ or x = $-\sqrt{2}$
(x) $4/x - 3 = 5/(2x + 3)$
Solution:

Given equation, 4/x - 3 = 5/(2x + 3)(4 - 3x)/x = 5/(2x + 3)On cross multiplying, we have (4 - 3x)(2x + 3) = 5x $8x - 6x^2 + 12 - 9x = 5x$ $6x^2 + 6x - 12 = 0$



Dividing by 6, we get $\mathbf{x}^2 + \mathbf{x} - 2 = \mathbf{0}$ Here, a = 1, b = 1 and c = -2By quadratic formula, we have $x=rac{-b\pm\sqrt{b^2-4ac}}{2a}$ $x=rac{-1\pm\sqrt{1^2-4(1)(-2)}}{2(1)}$ $x=rac{-1\pm\sqrt{1--8}}{2}$ $x=rac{-1\pm\sqrt{9}}{2}$ $x=rac{-1\pm 3}{2}$ $x=rac{2}{2}$ $x=-rac{4}{2}$ x = 1x = -2Therefore, x = 1 or x = -2(xi) 2x + 3/x + 3 = x + 4/x + 2Solution:

Given equation, 2x + 3/x + 3 = x + 4/x + 2On cross-multiplying, we have (2x + 3) (x + 2) = (x + 4) (x + 3) $2x^2 + 4x + 3x + 6 = x^2 + 3x + 4x + 12$ $2x^2 + 7x + 6 = x^2 + 7x + 12$ $x^2 + 0x - 6 = 0$ Here, a = 1, b = 0 and c = -6By quadratic formula, we have



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{0 \pm \sqrt{0^2 - 4(1)(-6)}}{2(1)}$$

$$x = \frac{0 \pm \sqrt{0 - -24}}{2}$$

$$x = \frac{0 \pm \sqrt{24}}{2}$$

$$x = \frac{0 \pm \sqrt{24}}{2}$$

$$x = \frac{0 \pm 2\sqrt{6}}{2}$$

$$x = \frac{0}{2} \pm \frac{2\sqrt{6}}{2}$$

$$x = 0 \pm \sqrt{6}$$

Therefore, $x = \sqrt{6}$ or $x = -\sqrt{6}$

(xii) $\sqrt{6x^2 - 4x} - 2\sqrt{6} = 0$ Solution:

Given equation, $\sqrt{6x^2 - 4x} - 2\sqrt{6} = 0$ Here, $a = \sqrt{6}$, b = -4 and $c = -2\sqrt{6}$ By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(\sqrt{6})(-2\sqrt{6})}}{2(\sqrt{6})}$$

$$= \frac{4 \pm \sqrt{64}}{2\sqrt{6}} = \frac{4 \pm 8}{2\sqrt{6}} = \frac{4 + 8}{2\sqrt{6}} \text{ and } \frac{4 - 8}{2\sqrt{6}}$$

$$= \frac{6}{\sqrt{6}} \text{ and } \frac{-2}{\sqrt{6}} = \sqrt{6} \text{ and } \frac{-\sqrt{6}}{3}$$

Therefore, $x = \sqrt{6}$ or $-\sqrt{6/3}$

(xiii) $2x/x - 4 + (2x - 5)/(x - 3) = -8\frac{1}{3}$ Solution:

Given equation, $2x/x - 4 + (2x - 5)/(x - 3) = 8\frac{1}{3}$



$$\Rightarrow \frac{2x(x-3) + (x-4)(2x-5)}{(x-4)(x-3)} = \frac{25}{3}$$

$$\Rightarrow \frac{2x^2 - 6x + 2x^2 - 5x - 8x + 20}{x^2 - 3x - 4x + 12} = \frac{25}{3}$$

$$\Rightarrow \frac{4x^2 - 19x + 20}{x^2 - 7x + 12} = \frac{25}{3}$$

$$25x^2 - 175x + 300 = 12x^2 - 57x + 60$$

$$13x^2 - 118x + 240 = 0$$

Here, a = 13, b = -118 and c = 240
By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-118) \pm \sqrt{(-118)^2 - 4(13)(240)}}{2(13)}$$

$$x = \frac{118 \pm \sqrt{13924 - 12480}}{26}$$

$$x = \frac{118 \pm \sqrt{1444}}{26}$$

$$x = \frac{118 \pm 38}{26}$$

$$x = \frac{118 \pm 38}{26}$$

$$x = \frac{156}{26} \quad x = \frac{80}{26}$$

$$x = 6 \quad x = \frac{40}{13}$$
Therefore, x = 6 or x = 40/13

(xiv)
$$\frac{x-1}{x-2} + \frac{x-3}{x-4} = 3\frac{1}{3}$$

Solution:

From the given equation,



 $\Rightarrow \frac{(x-1)(x-4) + (x-2)(x-3)}{(x-2)(x-4)} = \frac{10}{3}$ $\Rightarrow \frac{x^2 - 4x - x + 4 + x^2 - 3x - 2x + 6}{x^2 - 4x - 2x + 8} = \frac{10}{3}$ $\Rightarrow \frac{2x^2 - 10x + 10}{x^2 - 6x + 8} = \frac{10}{3}$ $10x^2 - 60x + 80 = 6x^2 - 30x + 30$ $4x^2 - 30x + 50 = 0$ $2x^2 - 15x + 25 = 0$ Here, a = 2, b = -15 and c = 25 $x=rac{-b\pm\sqrt{b^2-4ac}}{2a}$ $x = rac{-(-15)\pm\sqrt{(-15)^2-4(2)(25)}}{2(2)}$ $x=rac{15\pm\sqrt{225-200}}{4}$ $x = rac{15 \pm \sqrt{25}}{4}$ $x = rac{15 \pm 5}{4}$ $x = \frac{20}{4}$ $x = \frac{10}{4}$ x = 5 $x = \frac{5}{2}$ Therefore, x = 5 or x = 5/2

2. Solve each of the following equations for x and give, in each case, your answer correct to one decimal place:
(i) x² - 8x +5 = 0
(ii) 5x² + 10x - 3 = 0

Solution:

(i) $x^2 - 8x + 5 = 0$ Here, a = 1, b = -8 and c = 5By quadratic formula, we have



(ii)

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$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(5)}}{2(1)}$$

$$x = \frac{8 \pm \sqrt{64 - 20}}{2}$$

$$x = \frac{8 \pm \sqrt{44}}{2}$$

$$x = \frac{8 \pm \sqrt{44}}{2}$$

$$x = \frac{8 \pm 2\sqrt{11}}{2}$$

$$x = \frac{8}{2} \pm \frac{2\sqrt{11}}{2}$$

$$x = 4 \pm \sqrt{11}$$

$$x = 4 \pm 3.3$$
Thus, x = 7.7 or x = 0.7

$$5x^2 + 10x - 3 = 0$$
Here, a = 5, b = 10 and c = -3
By quadratic formula, we have

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-10 \pm \sqrt{10^2 - 4(5)(-3)}}{2(5)}$$

$$x = \frac{-10 \pm \sqrt{100 - -60}}{10}$$

$$x = \frac{-10 \pm \sqrt{160}}{10}$$

$$x=\frac{-10\pm 4\sqrt{10}}{10}$$

$$x = rac{-10}{10} \pm rac{4\sqrt{10}}{10}$$
 $x = -1 \pm rac{2\sqrt{10}}{5}$



Thus, x = 0.3 or x = -2.3

3. Solve each of the following equations for x and give, in each case, your answer correct to 2 decimal places: (i) $2x^2 - 10x + 5 = 0$ Solution:

Given equation, $2x^2 - 10x + 5 = 0$ Here, a = 2, b = -10 and c = 5 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(2)(5)}}{2(2)}$ $x = \frac{10 \pm \sqrt{100 - 40}}{4}$ $x = \frac{10 \pm \sqrt{100 - 40}}{4}$ $x = \frac{10 \pm 2\sqrt{15}}{4}$ $x = \frac{10 \pm 2\sqrt{15}}{4}$ $x = \frac{10}{4} \pm \frac{2\sqrt{15}}{4}$ $x = \frac{5}{2} \pm \frac{\sqrt{15}}{2}$ x = 4.43649x = 0.563508

Therefore, x = 4.44 or x = 0.56

(ii) 4x + 6/x + 13 = 0Solution:

Given equation, 4x + 6/x + 13 = 0Multiplying by x both sides, we get $4x^2 + 13x + 6 = 0$ Here, a = 4, b = 13 and c = 6



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-13 \pm \sqrt{13^2 - 4(4)(6)}}{2(4)}$$

$$x = \frac{-13 \pm \sqrt{169 - 96}}{8}$$

$$x = \frac{-13 \pm \sqrt{73}}{8}$$

$$x = \frac{-13 \pm \sqrt{73}}{8}$$

$$x = \frac{-13 \pm \sqrt{73}}{8}$$

$$x = -\frac{13}{8} \pm \frac{\sqrt{73}}{8}$$

$$x = -\frac{13}{8} \pm \frac{\sqrt{73}}{8}$$

$$x = -0.557$$

$$x = -2.693$$
Therefore, x = -0.56 or x = -2.70

(iii) $4x^2 - 5x - 3 = 0$ Solution:

Given equation, $4x^2 - 5x - 3 = 0$ Here, a = 4, b = -5 and c = -3



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(4)(-3)}}{2(4)}$$

$$x = \frac{5 \pm \sqrt{25 - -48}}{8}$$

$$x = \frac{5 \pm \sqrt{73}}{8}$$

$$x = \frac{5 \pm \sqrt{73}}{8}$$

$$x = \frac{5 \pm \sqrt{73}}{8}$$

$$x = 1.693$$

$$x = -0.443$$
Therefore, $x = 1.70$ or $x = -0.44$
(iv) $x^2 - 3x - 9 = 0$
Solution:
Given equation, $x^2 - 3x - 9 = 0$
Here, $a = 1, b = -3$ and $c = -9$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-9)}}{2(1)}$$

$$x = \frac{3 \pm \sqrt{9 - -36}}{2}$$

$$x = \frac{3 \pm 3\sqrt{5}}{2}$$

$$x = \frac{3 \pm 3\sqrt{5}}{2}$$

$$x = 4.8541$$

$$x = -1.8541$$



Therefore, x = 4.85 or x = -1.85

(v) $x^2 - 5x - 10 = 0$ Solution:

Given equation, $x^2 - 5x - 10 = 0$ Here, a = 1, b = -5 and c = -10 $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(-10)}}{2(1)}$ $x = \frac{5 \pm \sqrt{25 - -40}}{2}$ $x = \frac{5 \pm \sqrt{65}}{2}$ $x = \frac{5 \pm \sqrt{65}}{2}$ $x = \frac{5 \pm \sqrt{65}}{2}$ x = 6.53113x = -1.53113

Therefore, x = 6.53 or x = -1.53

4. Solve each of the following equations for x and give, in each case, your answer correct to 3 decimal places:

(i) $3x^2 - 12x - 1 = 0$ (ii) $x^2 - 16x + 6 = 0$ (iii) $2x^2 + 11x + 4 = 0$ Solution:

(i) Given equation, $3x^2 - 12x - 1 = 0$ Here, a = 3, b = -12 and c = -1



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(3)(-1)}}{2(3)}$$

$$x = \frac{12 \pm \sqrt{144 - -12}}{6}$$

$$x = \frac{12 \pm \sqrt{156}}{6}$$

$$x = \frac{12 \pm 2\sqrt{39}}{6}$$

$$x = \frac{12}{6} \pm \frac{2\sqrt{39}}{6}$$

$$x = 2 \pm rac{\sqrt{39}}{3}$$

 $x = 4.08167$

$$x = -0.081666$$

Therefore, x = 4.082 or x = -0.082

(ii) Given equation,
$$x^2 - 16x + 6 = 0$$

Here, $a = 1$, $b = -16$ and $c = 6$



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-16) \pm \sqrt{(-16)^2 - 4(1)(6)}}{2(1)}$$

$$x = \frac{16 \pm \sqrt{256 - 24}}{2}$$

$$x = \frac{16 \pm \sqrt{232}}{2}$$

$$x = \frac{16 \pm 2\sqrt{58}}{2}$$

$$x = \frac{16 \pm 2\sqrt{58}}{2}$$

$$x = \frac{16}{2} \pm \frac{2\sqrt{58}}{2}$$

$$x = 8 \pm \sqrt{58}$$

$$x = 15.6158$$

$$x = 0.384227$$

Therefore, x = 15.616 or x = 0.384

(iii) Given equation, $2x^2 + 11x + 4 = 0$ Here, a = 2, b = 11 and c = 4



$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-11 \pm \sqrt{11^2 - 4(2)(4)}}{2(2)}$$

$$x = \frac{-11 \pm \sqrt{121 - 32}}{4}$$

$$x = \frac{-11 \pm \sqrt{89}}{4}$$

$$x = \frac{-11 \pm \sqrt{89}}{4}$$

$$x = \frac{-11 \pm \sqrt{89}}{4}$$

$$x = -\frac{11}{4} \pm \frac{\sqrt{89}}{4}$$

$$x = -\frac{11}{4} \pm \frac{\sqrt{89}}{4}$$

$$x = -0.391505$$

$$x = -5 \cdot 1085$$

Therefore, x = -0.392 or x = -5.110

5. Solve: (i) $x^4 - 2x^2 - 3 = 0$ Solution:

Given equation, $x^4 - 2x^2 - 3 = 0$ $x^4 - 3x^2 + x^2 - 3 = 0$ $x^2(x^2 - 3) + 1(x^2 - 3) = 0$ $(x^2 + 1) (x^2 - 3) = 0$ So, $x^2 + 1 = 0$ (which is not possible) or $x^2 - 3 = 0$ Hence, $x^2 - 3 = 0$ $x = \pm \sqrt{3}$

(ii) $x^4 - 10x^2 + 9 = 0$ Solution:

Given equation, $x^4 - 10x^2 + 9 = 0$ $x^4 - x^2 - 9x^2 + 9 = 0$ $x^2(x^2 - 1) - 9(x^2 - 1) = 0$ $(x^2 - 9)(x^2 - 1) = 0$



So, we have $x^2 - 9 = 0$ or $x^2 - 1 = 0$ Hence, $x = \pm 3$ or $x = \pm 1$





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Exercise 5(E)

1. Solve each of the following equations: $\frac{2x}{x-3} + \frac{1}{2x+3} + \frac{3x+9}{(x-3)(2x+3)} = 0; x \neq 3, x \neq -\frac{3}{2}$

Solution:

Given equation, $\frac{2x}{x-3} + \frac{1}{2x+3} + \frac{3x+9}{(x-3)(2x+3)} = 0$ $\Rightarrow \frac{2x(2x+3) + 1(x-3) + 3x+9}{(x-3)(2x-3)} = 0$

 $\Rightarrow \frac{2x(2x+3) + 1(x-3) + 3x + 9}{(x-3)(2x+3)} = 0$ $4x^{2} + 6x + x - 3 + 3x + 9 = 0$ $4x^{2} + 10x + 6 = 0$ $4x^{2} + 4x + 6x + 6 = 0$ 4x(x+1) + 6(x+1) = 0 (4x+6) (x+1) = 0So, 4x + 6 = 0 or x + 1 = 0 x = -1 or x = -6/4 = -3/2 (rejected as this value is excluded in the domain) Therefore, x = -1 is the only solution

2. $(2x + 3)^2 = 81$ Solution:

Given, $(2x + 3)^2 = 81$ Taking square root on both sides we have, $2x + 3 = \pm 9$ $2x = \pm 9 - 3$ $x = (\pm 9 - 3)/2$ So, x = (9 - 3)/2 or (-9 - 3)/2Therefore, x = 3 or x = -6

3. $a^2x^2 - b^2 = 0$ Solution:

Given equation, $a^2x^2 - b^2 = 0$ $(ax)^2 - b^2 = 0$ (ax + b)(ax - b) = 0So, ax + b = 0 or ax - b = 0Therefore, x = -b/a or b/a



4. $x^2 - 11/4 x + 15/8 = 0$ Solution:

Given equation, $x^2 - 11/4 x + 15/8 = 0$ Taking L.C.M we have, $(8x^2 - 22x + 15)/8 = 0$ $8x^2 - 22x + 15 = 0$ $8x^2 - 12x - 10x + 15 = 0$ 4x(2x - 3) - 5(2x - 3) = 0 (4x - 5)(2x - 3) = 0So, 4x - 5 = 0 or 2x - 3 = 0Therefore, x = 5/4 or x = 3/2

5. x + 4/x = -4; $x \neq 0$ Solution:

Given equation, x + 4/x = -4 $(x^{2} + 4)/x = -4$ $x^{2} + 4 = -4x$ $x^{2} + 4x + 4 = 0$ $x^{2} + 2x + 2x + 4 = 0$ x(x + 2) + 2(x + 2) = 0 (x + 2)(x + 2) = 0 $(x + 2)^{2} = 0$ Taking square - root we have, x + 2 = 0Therefore, x = -2

6. $2x^4 - 5x^2 + 3 = 0$ Solution:

Given equation, $2x^4 - 5x^2 + 3 = 0$ Let's take $x^2 = y$ Then, the equation becomes $2y^2 - 5y + 3 = 0$ $2y^2 - 2y - 3y + 3 = 0$ 2y(y - 1) - 3(y - 1) = 0(2y - 3) (y - 1) = 0So, 2y - 3 = 0 or y - 1 = 0y = 3/2 or y = 1And, we have taken $y = x^2$ Thus, $x^2 = 3/2$ or $x^2 = 1$ $x = \pm \sqrt{(3/2)}$ or $x = \pm 1$



7. $x^4 - 2x^2 - 3 = 0$ Solution:

Given equation, $x^4 - 2x^2 - 3 = 0$ Let's take $x^2 = y$ Then, the equation becomes $y^2 - 2y - 3 = 0$ $y^2 - 3y + y - 3 = 0$ y(y - 3) + 1(y - 3) = 0(y + 1)(y - 3) = 0So, y + 1 = 0 or y - 3 = 0y = -1 or y = 3And, we have taken $y = x^2$ Thus, $x^2 = -1$ (impossible, no real solution) $x^2 = 3$ $x = \pm \sqrt{3}$

$$9\left(x^{2} + \frac{1}{x^{2}}\right) - 9\left(x + \frac{1}{x}\right) - 52 = 0$$

8.

Solution:

Let us take (x + 1/x) = y (1)Now, squaring it on both sides $(x + 1/x)^2 = y^2$ $x^2 + 1/x^2 + 2 = y^2$ So. $x^2 + 1/x^2 = y^2 - 2 \dots (2)$ Using (1) and (2) in the given equation, we have $9(y^2 - 2) - 9(y) - 52 = 0$ $9y^2 - 18 - 9y - 52 = 0$ $9y^2 - 9y - 70 = 0$ $9y^2 - 30y + 21y - 70 = 0$ 3y(3y - 10) + 7(3y - 10) = 0(3y + 7)(3y - 10) = 0So, 3y + 7 = 0 or 3y - 10 = 0y = -7/3 or y = 10/3Now, x + 1/x = -7/3x + 1/x = 10/3or $(x^2 + 1)/x = -7/3$ $(x^2 + 1)/x = 10/3$ or $3x^2 - 10x + 3 = 0$ $3x^2 + 7x + 3 = 0$ or



$$3x^{2} - 9x - x + 3 = 0 \text{ or } x = \frac{-7 \pm \sqrt{(-7)^{2} - 4(3)(3)}}{2(3)}$$

$$(3x - 1)(x - 3) = 0 \text{ so, } x = \frac{1/3 \text{ or } 3}{5}$$

$$x = \frac{-7 \pm \sqrt{(-7)^{2} - 4(3)(3)}}{2(3)}$$

$$9. \frac{2\left(x^{2} + \frac{1}{x^{2}}\right) - \left(x + \frac{1}{x}\right) = 11}{2}$$

Let us take (x + 1/x) = y (1)Now, squaring it on both sides $(x + 1/x)^2 = y^2$ $\dot{x}^2 + 1/\dot{x}^2 + 2 = y^2$ So. $x^{2} + 1/x^{2} = y^{2} - 2 \dots (2)$ Using (1) and (2) in the given equation, we have $2(y^2 - 2) - (y) = 11$ $2y^2 - 4 - y = 11$ $2y^2 - y - 15 = 0$ $2y^2 - 6y + 5y - 15 = 0$ 2y(y - 3) + 5(y - 3) = 0(2y + 5) (y - 3) = 0So, 2y + 5 = 0 or y - 3 = 0y = -5/2 or y = 3Now, x + 1/x = 3x + 1/x = -5/2or $(x^2 + 1)/x = 3$ $(x^2 + 1)/x = -5/2$ or $2(x^2 + 1) = -5x$ $x^2 + 1 = 3x$ or $2x^2 + 5x + 2 = 0$ $x^2 - 3x + 1 = 0$ or $2x^2 + 4x + x + 2 = 0$ or - 4(1)(1) 2x(x+2) + 1(x+2) = 02(1)(2x + 1)(x + 2) = 0Hence, x = -1/2 or -2 $x = \frac{-3 \pm \sqrt{5}}{2}$

$$\left(x^{2} + \frac{1}{x^{2}}\right) - 3\left(x - \frac{1}{x}\right) - 2 = 0$$

Solution:

Let us take $(x - 1/x) = y \dots (1)$ Now, squaring it on both sides



So,

Now,

 $x^2 = 1$

 $\mathbf{x} = \pm 1$

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 $(x - 1/x)^2 = y^2$ $x^2 + 1/x^2 - 2 = y^2$ $x^2 + 1/x^2 = y^2 + 2 \dots (2)$ Using (1) and (2) in the given equation, we have $(y^2 + 2) - 3(y) - 2 = 0$ $y^2 - 3y = 0$ y(y - 3) = 0So, y = 0 or y - 3 = 0(x - 1/x) = 0 or (x - 1/x) = 3 $x^2 - 1 = 0$ $x^{2} - 1 = 3x$ $x^{2} - 3x - 1 = 0$ or or Therefore, $x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-1)}}{\sqrt{(-3)^2 - 4(1)(-1)}}$ or 2(1) $x = \frac{3 \pm \sqrt{13}}{2}$



Exercise 5(F)

1. Solve: (i) (x + 5) (x - 5) = 24 Solution:

Given equation, (x + 5) (x - 5) = 24 $x^{2} - 25 = 24$ $x^{2} = 49$ Thus, $x = \pm 7$

(ii) $3x^2 - 2\sqrt{6x} + 2 = 0$ Solution:

Given equation, $3x^2 - 2\sqrt{6x} + 2 = 0$ $3x^2 - \sqrt{6x} - \sqrt{6x} + 2 = 0$ $\sqrt{3x}(\sqrt{3x} - \sqrt{2}) - \sqrt{2}(\sqrt{3x} - \sqrt{2}) = 0$ $(\sqrt{3x} - \sqrt{2})(\sqrt{3x} - \sqrt{2}) = 0$ So, $\sqrt{3x} - \sqrt{2} = 0$ or $\sqrt{3x} - \sqrt{2} = 0$ Therefore, $x = \sqrt{(2/3)}, \sqrt{(2/3)}$ (equal roots)

(iii) $3\sqrt{2x^2 - 5x} - \sqrt{2} = 0$ Solution:

Given equation, $3\sqrt{2x^2} - 5x - \sqrt{2} = 0$ $3\sqrt{2x^2} - 6x + x - \sqrt{2} = 0$ $3\sqrt{2x(x - \sqrt{2})} + 1(x - \sqrt{2}) = 0$ $(3\sqrt{2x} + 1) (x - \sqrt{2}) = 0$ So, $3\sqrt{2x} + 1 = 0$ or $x - \sqrt{2} = 0$ Therefore, $x = -1/3\sqrt{2}$ or $x = \sqrt{2}$

(iv) $2x - 3 = \sqrt{2x^2 - 2x + 21}$ Solution:

Given equation, $2x - 3 = \sqrt{2x^2 - 2x + 21}$ On squaring on both sides, we have $(2x - 3)^2 = 2x^2 - 2x + 21$ $4x^2 + 9 - 12x = 2x^2 - 2x + 21$ $2x^2 - 10x - 12 = 0$ Dividing by 2, we get $x^2 - 5x - 6 = 0$ $x^2 - 6x + x - 6 = 0$ x(x - 6) + 1(x - 6) = 0 Page No: 67



(x + 1) (x - 6) = 0So, x + 1 = 0 or x - 6 = 0Thus, we get x = -1 or x = 6But, putting x = -1 the L.H.S become negative. And we know that the square root function always gives a positive value. Therefore, x = 6 is the only solution.

2. One root of the quadratic equation $8x^2 + mx + 15 = 0$ is ³/₄. Find the value of m. Also, find the other root of the equation. Solution:

Given equation, $8x^2 + mx + 15 = 0$ One of the roots is ³/₄, and hence it satisfies the given equation So, $8(3/4)^2 + m(3/4) + 15 = 0$ 8(9/16) + m(3/4) + 15 = 018/4 + 3m/4 + 15 = 0Taking L.C.M, we have (18 + 3m + 60)/4 = 018 + 3m + 60 = 03m = -78m = -26Now, putting the value of m in the given equation, we get $8x^2 + (-26)x + 15 = 0$ $8x^2 - 26x + 15 = 0$ $8x^2 - 20x - 6x + 15 = 0$ 4x(2x - 5) - 3(2x - 5) = 0(4x - 3)(2x - 5) = 0So, 4x - 3 = 0 or 2x - 5 = 0Therefore. $x = \frac{3}{4}$ or $x = \frac{5}{2}$

3. Show that one root of the quadratic equation $x^2 + (3 - 2a)x - 6a = 0$ is -3. Hence, find its other root. Solution:

Given quadratic equation, $x^2 + (3 - 2a)x - 6a = 0$ Now, putting x = -3 we have $(-3)^2 + (3 - 2a)(-3) - 6a = 0$ 9 - 9 + 6a - 6a = 00 = 0Since, x = -3 satisfies the given equation -3 is one of the root of the quadratic equation. $x^2 + (3 - 2a)x - 6a = 0$ $x^2 + 3x - 2ax - 6a = 0$



x(x + 3) - 2a(x + 3) = 0(x - 2a) (x + 3) = 0 So, x - 2a = 0 or x + 3 = 0 x = 2a or x = -3 Hence, the other root is 2a.

4. If p - 15 = 0 and $2x^2 + px + 25 = 0$: find the values of x. Solution:

Given equations, p - 15 = 0 and $2x^2 + px + 25 = 0$ Thus, p = 15Now, using p in the quadratic equation, we get $2x^2 + (15)x + 25 = 0$ $2x^2 + 10x + 5x + 25 = 0$ 2x(x + 5) + 5(x + 5) = 0 (2x + 5) (x + 5) = 0So, 2x + 5 = 0 or x + 5 = 0Hence, x = -5/2 or x = -5

5. Find the solution of the quadratic equation $2x^2 - mx - 25n = 0$; if m + 5 = 0 and n - 1 = 0. Solution:

```
Given,

m + 5 = 0 and n - 1 = 0

so,

m = -5 and n = 1

Now, putting these values in the given quadratic equation 2x^2 - mx - 25n = 0, we get

2x^2 - (-5)x - 25(1) = 0

2x^2 + 5x - 25 = 0

2x^2 + 10x - 5x - 25 = 0

2x(x + 5) -5(x + 5) = 0

(2x - 5) (x + 5) = 0

So, 2x - 5 = 0 or x + 5 = 0

Hence,

x = 5/2 or x = -5
```

6. If m and n are roots of the equation: 1/x - 1/(x-2) = 3: where $x \neq 0$ and $x \neq 2$; find m x n. Solution:

Given equation, 1/x - 1/(x-2) = 3(x - 2 - x)/ (x(x - 2)) = 3 -2 = 3(x² - 2x) $3x^{2} - 6x + 2 = 0$ Solving by using quadratic formula, we get



$$\Rightarrow x = \frac{6 \pm \sqrt{6^2 - 4(3)(2)}}{2 \times 3}$$
$$\Rightarrow x = \frac{6 \pm \sqrt{12}}{2 \times 3}$$
$$\Rightarrow x = \frac{\sqrt{3} \pm 1}{\sqrt{3}}$$

And, since m and n are roots of the equation, we have $m = (\sqrt{3} + 1)/\sqrt{3}$ $n = (\sqrt{3} - 1)/\sqrt{3}$ So, $m \ge n = (\sqrt{3} + 1)/\sqrt{3} \ge ((\sqrt{3} - 1)/\sqrt{3} = [(\sqrt{3})^2 - 1]/(\sqrt{3})^2$ Thus, $m \ge n = 2/3$

