

#### **EXERCISE 7.1**

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In each of the following, write the correct answer: 1. Which of the following is not a criterion for congruence of triangles? (A) SAS (B) ASA (C) SSA (D) SSS Solution: (C) SSA **Explanation**: We know that, Two triangles are congruent, if the side(S) and angles (A) of one triangle is equal to another. And criterion for congruence of triangle are SAS, ASA, SSS, and RHS. SSA is not the criterion for congruency of a triangle. Hence, option C is the correct answer. 2. If AB = QR, BC = PR and CA = PQ, then (A)  $\triangle$  ABC  $\cong$   $\triangle$  PQR (B)  $\triangle CBA \cong \triangle PRQ$ (C)  $\triangle BAC \cong \triangle RPQ$ (D)  $\triangle$  POR  $\cong \triangle$  BCA Solution: **(B)**  $\Delta CBA \cong \Delta PRQ$ Explanation: According to the question, AB = QR, BC = PR and CA = PQSince, AB = QR, BC = PR and CA = PQWe can say that, A corresponds to Q, B corresponds to R, C corresponds to P. Ρ А R C Hence, (B)  $\triangle CBA \cong \triangle PRQ$ Hence, option B is the correct answer. 3. In  $\triangle$  ABC, AB = AC and  $\angle$ B = 50°. Then  $\angle$ C is equal to (A) 40° (B) 50° (C) 80° (D) 130° Solution:



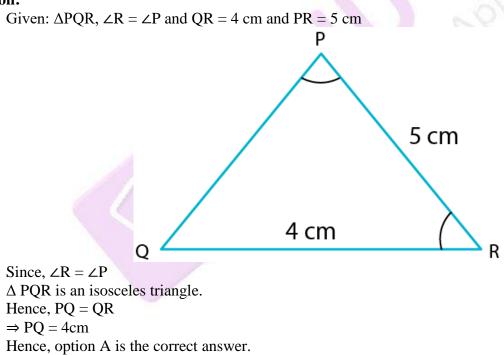
**(B) 50° Explanation**: According to the question,  $\triangle$  ABC, AB = AC and  $\angle$ B = 50°. А 50° В Since, AB = AC $\Delta$  ABC is an isosceles triangle. Hence,  $\angle B = \angle C$  $\angle B = 50^{\circ}$  (given)  $\Rightarrow \angle C = 50^{\circ}$ Hence, option B is the correct option. 4. In  $\triangle$  ABC, BC = AB and  $\angle$ B = 80°. Then  $\angle$ A is equal to (A) 80° (B) 40° (C) 50° (D) 100° Solution: (C) 50° **Explanation**: Given:  $\triangle$  ABC, BC = AB and  $\angle$ B = 80° А 80° В С Since, BC = ABhttps://byjus.com

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#### NCERT Exemplar Solutions For Class 9 Maths Chapter 7-Triangles

 $\triangle$  ABC is an isosceles triangle. Let,  $\angle C = \angle A = x$   $\angle B = 80^{\circ}$  (given) We know that, Using angle sum property, Sum of interior angles of a triangle should be =  $180^{\circ}$   $\angle A + \angle B + \angle C = 180^{\circ}$   $\Rightarrow x + 80^{\circ} + x = 180^{\circ}$   $\Rightarrow 2x = 180^{\circ} - 80^{\circ}$   $\Rightarrow 2x = 100^{\circ}$   $\Rightarrow x = 50^{\circ}$ Therefore,  $\angle C = \angle A = 50^{\circ}$ Hence, option C is the correct answer.

# 5. In $\triangle$ PQR, $\angle$ R = $\angle$ P and QR = 4 cm and PR = 5 cm. Then the length of PQ is (A) 4 cm (B) 5 cm (C) 2 cm (D) 2.5 cm Solution:

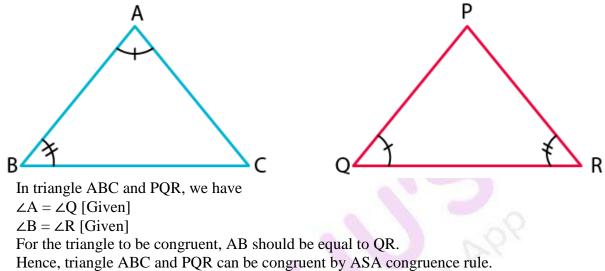




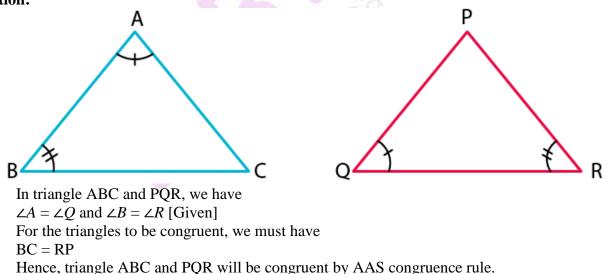
#### EXERCISE 7.2

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**1.** In triangles ABC and PQR,  $\angle A = \angle Q$  and  $\angle B = \angle R$ . Which side of  $\triangle$  PQR should be equal to side AB of  $\triangle$  ABC so that the two triangles are congruent? Give reason for your answer. Solution:



2. In triangles ABC and PQR,  $\angle A = \angle Q$  and  $\angle B = \angle R$ . Which side of  $\triangle$  PQR should be equal to side BC of  $\triangle$  ABC so that the two triangles are congruent? Give reason for your answer. Solution:



# 3. "If two sides and an angle of one triangle are equal to two sides and an angle of another triangle, then the two triangles must be congruent." Is the statement true? Why? Solution:

No, the statement, "if two sides and an angle of one triangle are equal to two sides and an angle of another triangle, then the two triangles must be congruent" is false.

Justification:

Because by the congruent rule,



The two sides and the included angle of one triangle are equal to the two sides and the included angle of the other triangle, i.e., SAS rule.

# 4. "If two angles and a side of one triangle are equal to two angles and a side of another triangle, then the two triangles must be congruent." Is the statement true? Why? Solution:

The statement, "If two angles and a side of one triangle are equal to two angles and a side of another triangle, then the two triangles must be congruent." is true.

Justification:

The statement is true because, the triangles will be congruent either by ASA rule or AAS rule. This is because two angles and one side are enough to construct two congruent triangles.

## 5. Is it possible to construct a triangle with lengths of its sides as 4 cm, 3 cm and 7 cm? Give reason for your answer.

#### Solution:

No, it is not possible to construct a triangle with lengths of sides 4 cm, 3 cm and 7 cm.

Justification:

We know that,

Sum of any two sides of a triangle is always greater than the third side.

Here, the sum of two sides whose lengths are 4 cm and 3 cm = 4 cm + 3 cm = 7 cm,

Which is equal to the length of third side, i.e., 7 cm.

Hence, it is not possible to construct a triangle with lengths of sides 4 cm, 3 cm and 7 cm.

### 6. It is given that $\triangle$ ABC $\cong \triangle$ RPQ. Is it true to say that BC = QR? Why? Solution:

It is False that BC = QR because BC = PQ as  $\triangle ABC \cong \triangle RPQ$ .



#### **EXERCISE 7.3**

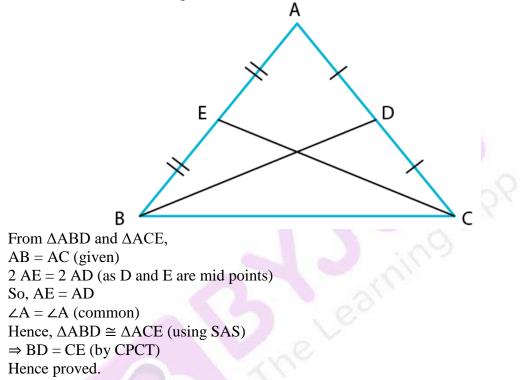
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**1.** ABC is an isosceles triangle with AB = AC and BD and CE are its two medians. Show that BD = CE.

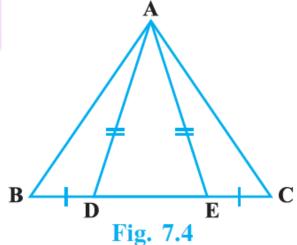
Solution:

According to the question,

 $\triangle$ ABC is an isosceles triangle and AB = AC, BD and CE are two medians



2. In Fig.7.4, D and E are points on side BC of a  $\triangle$  ABC such that BD = CE and AD = AE. Show that  $\triangle$  ABD  $\cong \triangle$  ACE.



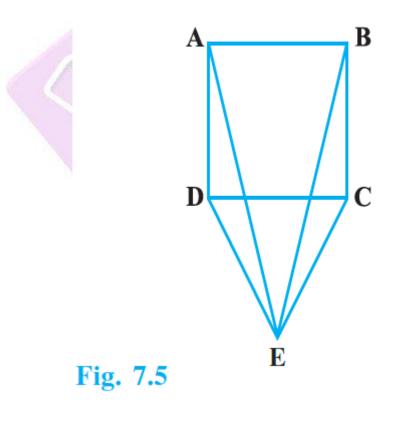
#### Solution:

According to the question,



In  $\triangle ABC$ , BD = CE and AD = AE.In  $\triangle ADE$ , AD = AESince opposite angles to equal sides are equal, We have,  $\angle ADE = \angle AED \dots (1)$ Now,  $\angle ADE + \angle ADB = 180^{\circ}$  (linear pair)  $\angle ADB = 180^{\circ} - \angle ADE \dots (2)$ Also,  $\angle AED + \angle AEC = 180^{\circ}$  (linear pair)  $\angle AEC = 180^{\circ} - \angle AED$ Since,  $\angle ADE = \angle AED$  $\angle AEC = 180^{\circ} - \angle ADE \dots (3)$ From equation (2) and (3)  $\angle ADB = \angle AEC \dots (4)$ Now, In  $\triangle$ ADB and  $\triangle$ AEC, AD = AE (given) BD = EC (given)  $\angle ADB = \angle AEC$  (from (4) Hence,  $\triangle ABD \cong \triangle ACE$  (by SAS)

3. CDE is an equilateral triangle formed on a side CD of a square ABCD (Fig.7.5). Show that  $\Delta$  ADE  $\cong \Delta$  BCE.



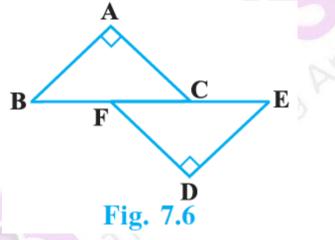
Solution:

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### NCERT Exemplar Solutions For Class 9 Maths Chapter 7-Triangles

According to the question, CDE is an equilateral triangle formed on a side CD of a square ABCD. In  $\triangle$ ADE and  $\triangle$ BCE, DE = CE (sides of equilateral triangle) Now,  $\angle$ ADC =  $\angle$ BCD = 90° And,  $\angle$ EDC =  $\angle$ ECD = 60° Hence,  $\angle$ ADE =  $\angle$ ADC +  $\angle$ CDE = 90° + 60° = 150° And  $\angle$ BCE =  $\angle$ BCD +  $\angle$ ECD = 90° + 60° = 150°  $\Rightarrow \angle$ ADE =  $\angle$ BCE AD = BC (sides of square) Hence,  $\triangle$ ADE  $\cong \triangle$ BCE (by SAS)

4. In Fig.7.6, BA  $\perp$  AC, DE  $\perp$  DF such that BA = DE and BF = EC. Show that  $\triangle$  ABC  $\cong \triangle$  DEF.



#### Solution:

According to the question,  $BA \perp AC$ ,  $DE \perp DF$  such that BA = DE and BF = EC. In  $\triangle ABC$  and  $\triangle DEF$  BA = DE (given) BF = EC (given)  $\angle A = \angle D$  (both 90°) BC = BF + FC EF = EC + FC = BF + FC ( $\because EC = BF$ )  $\Rightarrow EF = BC$ Hence,  $\triangle ABC \cong \triangle DEF$  (by RHS)

## 5. Q is a point on the side SR of a $\Delta$ PSR such that PQ = PR. Prove that PS > PQ. Solution:

Given: in  $\triangle PSR$ , Q is a point on the side SR such that PQ = PR. In  $\triangle PRQ$ , PR = PQ (given)  $\Rightarrow \angle PRQ = \angle PQR$  (opposite angles to equal sides are equal) But  $\angle PQR > \angle PSR$  (exterior angle of a triangle is greater than each of opposite interior angle)



- $\Rightarrow \angle PRQ > \angle PSR$
- $\Rightarrow$  PS > PR (opposite sides to greater angle is greater)
- $\Rightarrow$  PS > PQ (as PR = PQ)





### **EXERCISE 7.4**

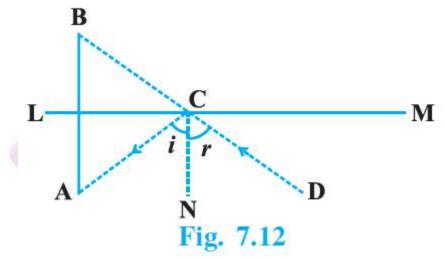
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## **1. Find all the angles of an equilateral triangle.** Solution:

In equilateral triangle, All the sides are equal. Therefore, all angles are also equal Let the angles of an equilateral triangle = x According to angle sum property, We know that the sum of the interior angles is equal to  $180^{\circ}$ .  $x+x+x=180^{\circ}$ 3x=180 $x=60^{\circ}$ Therefore, all the angles of an equilateral triangle are  $60^{\circ}$ 

2. The image of an object placed at a point A before a plane mirror LM is seen at the point B by an observer at D as shown in Fig. 7.12. Prove that the image is as far behind the mirror as the object is in front of the mirror.

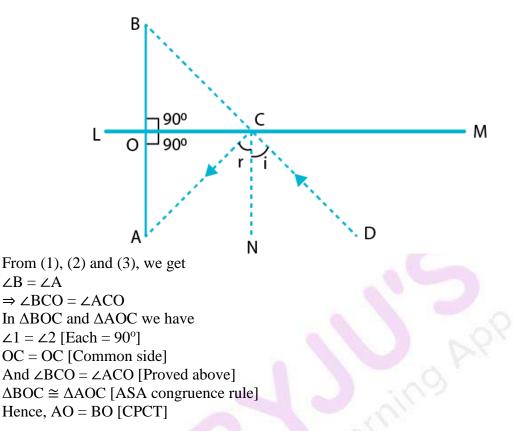
[Hint: CN is normal to the mirror. Also, angle of incidence = angle of reflection].



#### Solution:

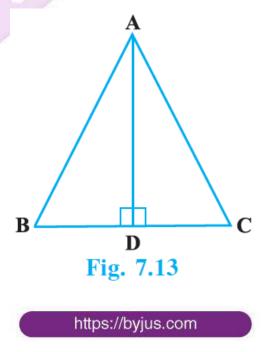
Let AB intersect LM at O. We have to prove that AO = BO. Now,  $\angle i = \angle r \dots (1)$ [::Angle of incidence = Angle of reflection]  $\angle B = \angle i$  [Corresponding angles] ...(2) And  $\angle A = \angle r$  [Alternate interior angles] ...(3)





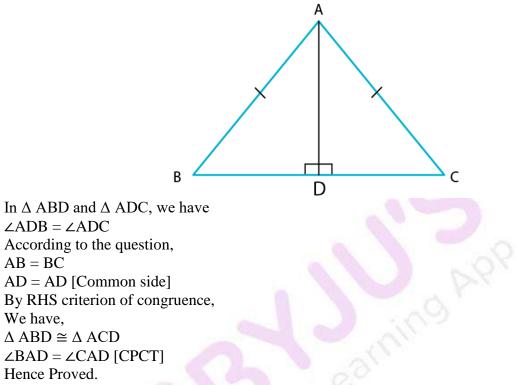
3. ABC is an isosceles triangle with AB = AC and D is a point on BC such that AD  $\perp$  BC (Fig. 7.13). To prove that  $\angle$ BAD =  $\angle$ CAD, a student proceeded as follows: In  $\triangle$  ABD and  $\triangle$  ACD, AB = AC (Given)

 $\angle B = \angle C$  (because AB = AC) And  $\angle ADB = \angle ADC$ Therefore,  $\triangle ABD \land \triangle ACD$  (AAS) So,  $\angle BAD = \angle CAD$  (CPCT)

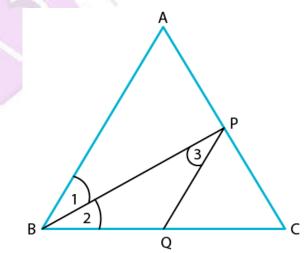




What is the defect in the above arguments? [Hint: Recall how  $\angle B = \angle C$  is proved when AB = AC]. Solution:



**4.** P is a point on the bisector of ∠ABC. If the line through P, parallel to BA meet BC at Q, prove that BPQ is an isosceles triangle. Solution:

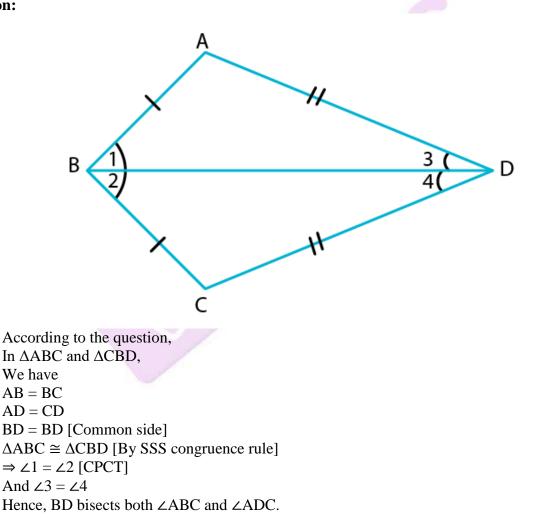


To prove: BPQ is an isosceles triangle. According to the question, Since, BP is the bisector of  $\angle ABC$ ,  $\angle 1 = \angle 2 \dots (1)$ Now, PQ is parallel to BA and BP cuts them



 $\angle 1 = \angle 3$  [Alternate angles] ... (2) From equations, (1) and (2), We get  $\angle 2 = \angle 3$ In  $\triangle$  BPQ, We have  $\angle 2 = \angle 3$ PQ = BQ Hence, BPQ is an isosceles triangle.

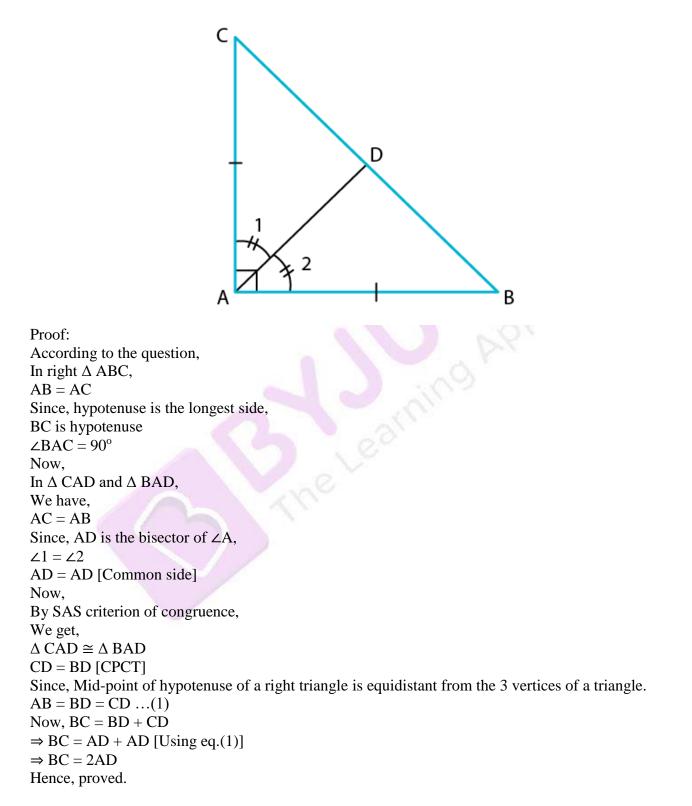
5. ABCD is a quadrilateral in which AB = BC and AD = CD. Show that BD bisects both the angles ABC and ADC. Solution:



6. ABC is a right triangle with AB = AC. Bisector of ∠A meets BC at D. Prove that BC = 2 AD. Solution:

Given: A right angles triangle with AB = AC bisector of  $\angle A$  meets BC at D. To prove: BC = 2AD

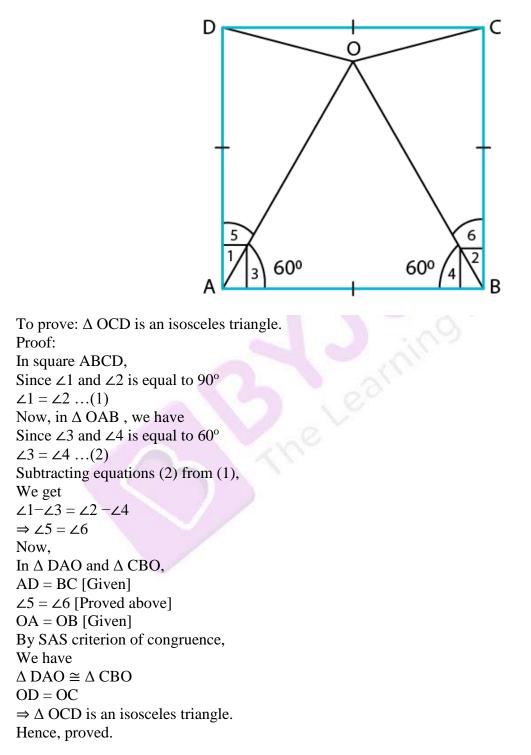




7. O is a point in the interior of a square ABCD such that OAB is an equilateral triangle. Show that  $\Delta$  OCD is an isosceles triangle. Solution:



According to the question, It is given that: A square ABCD and OA = OB = AB.



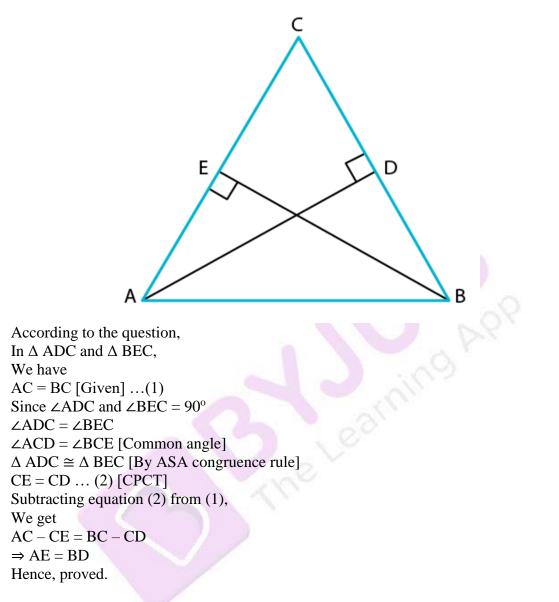
**8.** ABC and DBC are two triangles on the same base BC such that A and D lie on the opposite sides of BC, AB = AC and DB = DC. Show that AD is the perpendicular bisector of BC. Solution:



Given:  $\triangle$  ABC and  $\triangle$  DBC on the same base BC. Also, AB = AC and BD = DC. To prove: AD is the perpendicular bisector of BC i.e., OB = OCProof: In  $\triangle$  BAD and  $\triangle$  CADwe have AB = AC [Given]BD = CD [Given] AD = AD [common side] So, by SSS criterion of congruence, we have  $\Delta BAD \cong \Delta CAD$  $\angle 1 = \angle 2$  [CPCT] Now, in  $\triangle$  BAO and  $\triangle$  CAO, we have AB = AC [Given] $\angle 1 = \angle 2$  [Proved above] AO = AO [Common side] So, by SAS criterion of congruence, we have  $\Delta BAO \cong \Delta CAO$ BO = CO [CPCT]And,  $\angle 3 = \angle 4$  [CPCT] But,  $\angle 3 + \angle 4 = 180^{\circ}$  [Linear pair axiom]  $\Rightarrow \angle 3 + \angle 3 = 180$  $\Rightarrow 2 \angle 3 = 180$  $\Rightarrow \angle 3 = 180/2$  $\Rightarrow \angle 3 = 90^{\circ}$ Since BO = CO and  $\angle 3 = 90^{\circ}$ , AD is perpendicular bisector of BC. Hence, proved.

9. ABC is an isosceles triangle in which AC = BC. AD and BE are respectively two altitudes to sides BC and AC. Prove that AE = BD. Solution:





10. Prove that sum of any two sides of a triangle is greater than twice the median with respect to the third side. Solution:

According to the question, We have,  $\triangle$  ABC with median AD. To prove: AB + AC > 2AD AB + BC > 2AD BC + AC > 2AD Construction: Extend AD to E such that DE = AD Join EC. Proof:



