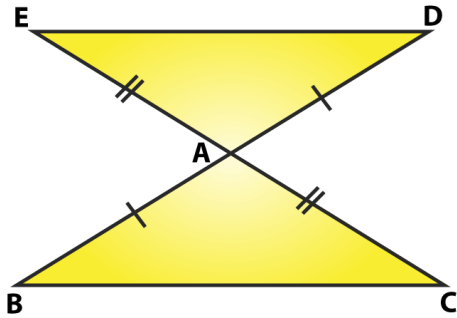


### Exercise 10.1

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**Question 1:** In figure, the sides BA and CA have been produced such that  $BA = AD$  and  $CA = AE$ . Prove that segment  $DE \parallel BC$ .



**Solution:**

Sides BA and CA have been produced such that  $BA = AD$  and  $CA = AE$ .

To prove:  $DE \parallel BC$

Consider  $\triangle BAC$  and  $\triangle DAE$ ,

$BA = AD$  and  $CA = AE$  (Given)

$\angle BAC = \angle DAE$  (vertically opposite angles)

By SAS congruence criterion, we have

$\triangle BAC \cong \triangle DAE$

We know, corresponding parts of congruent triangles are equal

So,  $BC = DE$  and  $\angle DEA = \angle BCA$ ,  $\angle EDA = \angle CBA$

Now, DE and BC are two lines intersected by a transversal DB s.t.

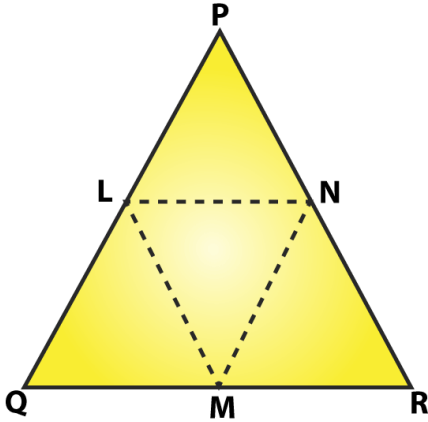
$\angle DEA = \angle BCA$  (alternate angles are equal)

Therefore,  $DE \parallel BC$ . Proved.

**Question 2:** In a  $\triangle PQR$ , if  $PQ = QR$  and  $L, M$  and  $N$  are the mid-points of the sides  $PQ, QR$  and  $RP$  respectively. Prove that  $LN = MN$ .

**Solution:**

Draw a figure based on given instruction,



In  $\triangle PQR$ ,  $PQ = QR$  and  $L, M, N$  are midpoints of the sides  $PQ, QR$  and  $RP$  respectively (Given)

To prove :  $LN = MN$

As two sides of the triangle are equal, so  $\triangle PQR$  is an isosceles triangle

$PQ = QR$  and  $\angle QPR = \angle QRP$  ..... (i)

Also,  $L$  and  $M$  are midpoints of  $PQ$  and  $QR$  respectively

$PL = LQ = QM = MR = QR/2$

Now, consider  $\triangle LPN$  and  $\triangle MRN$ ,

$LP = MR$

$\angle LPN = \angle MRN$  [From (i)]

$\angle QPR = \angle LPN$  and  $\angle QRP = \angle MRN$

$PN = NR$  [ $N$  is midpoint of  $PR$ ]

By SAS congruence criterion,

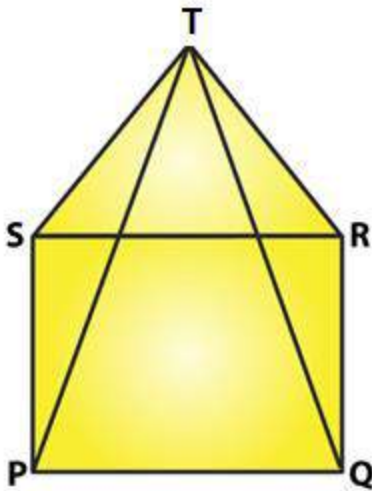
$\triangle LPN \cong \triangle MRN$

We know, corresponding parts of congruent triangles are equal.

So  $LN = MN$

Proved.

**Question 3:** In figure, PQRS is a square and SRT is an equilateral triangle. Prove that  
(i)  $PT = QT$  (ii)  $\angle TQR = 15^\circ$



**Solution:**

Given: PQRS is a square and SRT is an equilateral triangle.

To prove:

(i)  $PT = QT$  and (ii)  $\angle TQR = 15^\circ$

Now,

**PQRS is a square:**

$PQ = QR = RS = SP$  ..... (i)

And  $\angle SPQ = \angle PQR = \angle QRS = \angle RSP = 90^\circ$

**Also,  $\triangle SRT$  is an equilateral triangle:**

$SR = RT = TS$  .....(ii)

And  $\angle TSR = \angle SRT = \angle RTS = 60^\circ$

From (i) and (ii)

$PQ = QR = SP = SR = RT = TS$  .....(iii)

From figure,

$$\angle TSP = \angle TSR + \angle RSP = 60^\circ + 90^\circ = 150^\circ \quad \text{and}$$

$$\angle TRQ = \angle TRS + \angle SRQ = 60^\circ + 90^\circ = 150^\circ$$

$$\Rightarrow \angle TSP = \angle TRQ = 150^\circ \quad \dots\dots\dots (iv)$$

By SAS congruence criterion,  $\Delta TSP \cong \Delta TRQ$

We know, corresponding parts of congruent triangles are equal  
So,  $PT = QT$

Proved part (i).

Now, consider  $\Delta TQR$ .

$$QR = TR \quad [\text{From (iii)}]$$

$\Delta TQR$  is an isosceles triangle.

$$\angle QTR = \angle TQR \quad [\text{angles opposite to equal sides}]$$

$$\text{Sum of angles in a triangle} = 180^\circ$$

$$\Rightarrow \angle QTR + \angle TQR + \angle TRQ = 180^\circ$$

$$\Rightarrow 2 \angle TQR + 150^\circ = 180^\circ \quad [\text{From (iv)}]$$

$$\Rightarrow 2 \angle TQR = 30^\circ$$

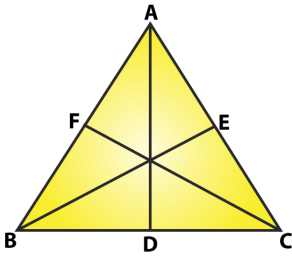
$$\Rightarrow \angle TQR = 15^\circ$$

Hence proved part (ii).

**Question 4: Prove that the medians of an equilateral triangle are equal.**

**Solution:**

Consider an equilateral  $\triangle ABC$ , and Let D, E, F are midpoints of BC, CA and AB.



Here, AD, BE and CF are medians of  $\triangle ABC$ .

Now,

D is midpoint of BC  $\Rightarrow$   $BD = DC$

Similarly,  $CE = EA$  and  $AF = FB$

Since  $\triangle ABC$  is an equilateral triangle

$AB = BC = CA$  .....(i)

$BD = DC = CE = EA = AF = FB$  .....(ii)

And also,  $\angle ABC = \angle BCA = \angle CAB = 60^\circ$  .....(iii)

Consider  $\triangle ABD$  and  $\triangle BCE$

$AB = BC$  [From (i)]

$BD = CE$  [From (ii)]

$\angle ABD = \angle BCE$  [From (iii)]

By SAS congruence criterion,

$\triangle ABD \cong \triangle BCE$

$\Rightarrow AD = BE$  .....(iv)

[Corresponding parts of congruent triangles are equal in measure]

Now, consider  $\Delta BCE$  and  $\Delta CAF$ ,

$$BC = CA \quad [\text{From (i)}]$$

$$\angle BCE = \angle CAF \quad [\text{From (iii)}]$$

$$CE = AF \quad [\text{From (ii)}]$$

By SAS congruence criterion,

$$\Delta BCE \cong \Delta CAF$$

$$\Rightarrow BE = CF \quad \dots\dots\dots(v)$$

[Corresponding parts of congruent triangles are equal]

From (iv) and (v), we have

$$AD = BE = CF$$

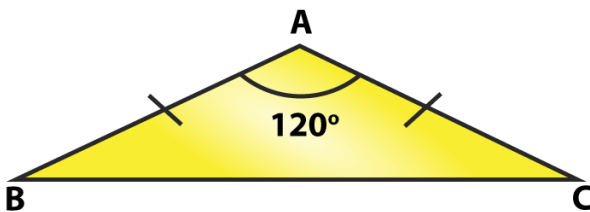
$$\text{Median } AD = \text{Median } BE = \text{Median } CF$$

The medians of an equilateral triangle are equal.

Hence proved

**Question 5:** In a  $\Delta ABC$ , if  $\angle A = 120^\circ$  and  $AB = AC$ . Find  $\angle B$  and  $\angle C$ .

**Solution:**



To find:  $\angle B$  and  $\angle C$ .

Here,  $\Delta ABC$  is an isosceles triangle since  $AB = AC$

$$\angle B = \angle C \quad \dots\dots\dots(i)$$

[Angles opposite to equal sides are equal]

We know, sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle B + \angle B = 180^\circ \text{ (using (i))}$$

$$120^\circ + 2\angle B = 180^\circ$$

$$2\angle B = 180^\circ - 120^\circ = 60^\circ$$

$$\angle B = 30^\circ$$

$$\text{Therefore, } \angle B = \angle C = 30^\circ$$

**Question 6:** In a  $\triangle ABC$ , if  $AB = AC$  and  $\angle B = 70^\circ$ , find  $\angle A$ .

**Solution:**

Given: In a  $\triangle ABC$ ,  $AB = AC$  and  $\angle B = 70^\circ$

$\angle B = \angle C$  [Angles opposite to equal sides are equal]

Therefore,  $\angle B = \angle C = 70^\circ$

Sum of angles in a triangle =  $180^\circ$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 70^\circ + 70^\circ = 180^\circ$$

$$\angle A = 180^\circ - 140^\circ$$

$$\angle A = 40^\circ$$