

Exercise 19.2

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Question 1: A soft drink is available in two packs- (i) a tin can with a rectangular base of length 5 cm and width 4 cm, having a height of 15 cm and (ii) a plastic cylinder with circular base of diameter 7 cm and height 10 cm, Which container has greater capacity and by how much?

Solution:

(i) Dimensions of a cubical tin can:

Length (L) = 5 cm

Breadth (B) = 4 cm

Height (H) = 15 cm

Capacity of the tin can = Volume of Tin Can = $l \times b \times h$ cubic units = $(5 \times 4 \times 15) \text{ cm}^3 = 300 \text{ cm}^3$

(ii) Radius of the circular end of the plastic cylinder (R) = $\text{diameter}/2 = 7/2 \text{ cm} = 3.5 \text{ cm}$

Height of plastic cylinder (H) = 10 cm

Capacity of plastic cylinder = Volume of cylindrical container = $\pi R^2 H = 22/7 \times (3.5)^2 \times 10 \text{ cm}^3 = 385 \text{ cm}^3$

From (i) and (ii) results, the plastic cylinder has greater capacity.

Difference in capacity = $(385 - 300) \text{ cm}^3 = 85 \text{ cm}^3$

Question 2: The pillars of a temple are cylindrically shaped. If each pillar has a circular base of radius 20 cm and height 10 m. How much concrete mixture would be required to build 14 such pillars?

Solution:

In this case, we have to find the volume of the cylinders.

Given:

Radius of the base of a cylinder = 20 cm

Height of cylinder = 10 m = 1000 cm

[1m = 100 cm]

Volume of the cylindrical pillar = $\pi R^2 H$

$$= (22/7 \times 20^2 \times 1000) \text{ cm}^3$$

$$= 8800000/7 \text{ cm}^3 \text{ or } 8.87 \text{ m}^3$$

Therefore, volume of 14 pillars = $14 \times 8.87 \text{ m}^3 = 17.6 \text{ m}^3$

Question 3: The inner diameter of a cylindrical wooden pipe is 24 cm and its outer diameter is 28 cm. The length of the pipe is 35 cm. Find the mass of the pipe, if 1 cm³ of wood has a mass of 0.6 gm.

Solution:

Let r and R be the inner and outer radii of cylindrical pipe.

Inner radius of a cylindrical pipe (r) = $24/2 = 12$ cm

Outer radius of a cylindrical pipe (R) = $28/2 = 14$ cm

Height of pipe (h) = length of pipe = 35 cm

Mass of pipe = volume \times density = $\pi(R^2 - r^2)h$

$$= \frac{22}{7}(14^2 - 12^2)35$$

$$= 5720$$

Mass of pipe is 5720 cm³

Mass of 1 cm³ wood = 0.6 gm (Given)

Therefore, mass of 5720 cm³ wood = $5720 \times 0.6 = 3432$ gm = 3.432 kg

Question 4: If the lateral surface of a cylinder is 94.2 cm² and its height is 5 cm, find:

i) radius of its base (ii) volume of the cylinder
[Use $\pi = 3.141$]

Solution:

Lateral surface of the cylinder = 94.2 cm²

Height of the cylinder = 5 cm

Let ' r ' be the radius.

(i) Lateral surface of the cylinder = 94.2 cm²

$$2\pi rh = 94.2$$

$$\text{or } 2 \times 3.14 \times r \times 5 = 94.2$$

$$\text{or } r = 3 \text{ cm}$$

$$\begin{aligned} \text{(ii) Volume of the cylinder} &= \pi r^2 h \\ &= (3.14 \times 3^2 \times 5) \text{ cm}^3 \\ &= 141.3 \text{ cm}^3 \end{aligned}$$

Question 5: The capacity of a closed cylindrical vessel of height 1 m is 15.4 liters. How many square meters of the metal sheet would be needed to make it?

Solution:

Given, The capacity of a closed cylindrical vessel of height 1 m is 15.4 liters.

$$\begin{aligned} \text{Height of the cylindrical vessel} &= 15.4 \text{ litres} = 0.0154 \text{ m}^3 \\ [1\text{m}^3 &= 1000 \text{ litres}] \end{aligned}$$

Let 'r' be the radius of the circular ends of the cylinders, then

$$\begin{aligned} \pi r^2 h &= 0.0154 \text{ m}^3 \\ 3.14 \times r^2 \times 1 &= 0.0154 \text{ m}^3 \\ \text{or } r &= 0.07 \text{ m} \end{aligned}$$

Again,

$$\text{Total surface area of a vessel} = 2\pi r(r+h)$$

$$\begin{aligned} &= 2(3.14)(0.07)(0.07+1) \text{ m}^2 \\ &= 0.470 \text{ m}^2 \end{aligned}$$

Question 6: A patient in a hospital is given soup daily in a cylindrical bowl of diameter 7 cm. If the bowl is filled with soup to a height of 4 cm, how much soup the hospital has to prepare daily to serve 250 patients?

Solution:

$$\text{Radius of cylindrical bowl (R)} = \text{diameter}/2 = 7/2 \text{ cm} = 3.5 \text{ cm}$$

$$\text{Height} = 4 \text{ cm}$$

Now,

$$\text{Volume of soup in 1 bowl} = \pi r^2 h$$

$$\begin{aligned} &= 22/7 \times 3.5^2 \times 4 \text{ cm}^3 \\ &= 154 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of soup in 250 bowls} &= (250 \times 154) \text{ cm}^3 \\ &= 38500 \text{ cm}^3 \\ &= 38.5 \text{ liters} \end{aligned}$$

Thus, hospital has to prepare 38.5 liters of soup daily in order to serve 250 patients.

Question 7: A hollow garden roller, 63 cm wide with a girth of 440 cm, is made of 4 cm thick iron. Find the volume of the iron.

Solution:

The outer circumference of the roller = 440 cm

Thickness of the roller = 4 cm and

Its height (h) = 63 cm

Let 'R' be the external radius and 'r' be the inner radius of the roller.

Circumference of roller = $2\pi R = 440$

Or $2\pi R = 440$

$2 \times \frac{22}{7} \times R = 440$

or $R = 70$

And, inner radius 'r' is given as

$\Rightarrow r = R - 4$

$\Rightarrow r = 70 - 4$

$\Rightarrow r = 66$

Inner radius is 66 cm

Now, volume of the iron is given as

$V = \pi(R^2 - r^2)h$

$V = \frac{22}{7} (70^2 - 66^2)63$

$V = 107712$

Therefore, required volume is 107712 cm^3 .

Question 8: A solid cylinder has a total surface area of 231 cm^2 . Its curved surface area is $\frac{2}{3}$ of the total surface area. Find the volume of the cylinder.

Solution:

Total surface area = 231 cm^2

As per given statement: Curved surface area = $\frac{2}{3}(\text{Total surface area})$

Curved surface area = $\frac{2}{3} \times 231 = 154$

So, Curved surface area = $154 \text{ cm}^2 \dots(1)$

We know, Curved surface area of cylinder = $2\pi rh + 2\pi r^2$

Or $2\pi rh + 2\pi r^2 = 231 \dots\dots(2)$

Here $2\pi rh$ is the curved surface area, so using (1), we have

$$\Rightarrow 154 + 2\pi r^2 = 231$$

$$\Rightarrow 2\pi r^2 = 231 - 154$$

$$\Rightarrow 2 \times \frac{22}{7} \times r^2 = 77$$

$$\Rightarrow r^2 = \frac{49}{4}$$

$$\text{or } r = \frac{7}{2}$$

Find the value of h:

$$\text{CSA} = 154 \text{ cm}^2$$

$$\Rightarrow 2\pi rh = 154$$

$$\Rightarrow 2 \times \frac{22}{7} \times \frac{7}{2} \times h = 154$$

$$\Rightarrow h = \frac{154}{22}$$

$$\Rightarrow h = 7$$

Now,

Find Volume of the cylinder:

$$V = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 7$$

$$= 269.5$$

The volume of the cylinder is 269.5 cm^3

Question 9: The cost of painting the total outside surface of a closed cylindrical oil tank at 50 paise per square decimetre is Rs 198. The height of the tank is 6 times the radius of the base of the tank. Find the volume corrected to 2 decimal places.

Solution:

Let 'r' be the radius of the tank.

As per given statement: Height (h) = 6(Radius) = 6r dm

Cost of painting for 50 paise or Rs $\frac{1}{2}$ per dm^2 = Rs 198 (Given)

$$\Rightarrow 2\pi r(r+h) \times \frac{1}{2} = 198$$

$$\Rightarrow 2 \times \frac{22}{7} \times r(r+6r) \times \frac{1}{2} = 198$$

$$\Rightarrow r = 3 \text{ dm}$$

$$\text{And, } h = (6 \times 3) \text{ dm} = 18 \text{ dm}$$

Now,

$$\text{Volume of the tank} = \pi r^2 h = \frac{22}{7} \times 9 \times 18 = 509.14 \text{ dm}^3$$

Question 10: The radii of two cylinders are in the ratio 2 : 3 and their heights are in the ratio 5 : 3. Calculate the ratio of their volumes and the ratio of their curved surfaces.

Solution:

Let the radius of the cylinders be 2x and 3x and the height of the cylinders be 5y and 3y.

$$\frac{\text{(Volume of cylinder 1)}}{\text{(Volume of cylinder 2)}} = \frac{\pi(2x)^2 5y}{\pi(3x)^2 3y} = \frac{20}{27}$$

$$\frac{\text{Surface area of cylinder 1}}{\text{Surface area of cylinder 2}} = \frac{2\pi \times 2x \times 5y}{2\pi \times 3x \times 3y} = \frac{10}{9}$$

Question 11: The ratio between the curved surface area and the total surface area of a right circular cylinder is 1:2. Find the volume of the cylinder, if its total surface area is 616 cm^2 .

Solution:

Total surface area (T.S.A) = 616 cm^2 (given)

Let r be the radius of cylinder and h be the radius of cylinder.

As per given statement:

(curved surface area / (total surface area)) = $1/2$

or CSA = $1/2$ TSA

CSA = $1/2 \times 616 = 308$

\Rightarrow CSA = 308 cm^2

Now,

TSA = $2\pi rh + 2\pi r^2$

$\Rightarrow 616 = \text{CSA} + 2\pi r^2$

$\Rightarrow 616 = 308 + 2\pi r^2$

$\Rightarrow 2\pi r^2 = 616 - 308$

$\Rightarrow 2\pi r^2 = 308/2\pi$

$\Rightarrow r^2 = 49$

or $r = 7 \text{ cm}$... (1)

As, CSA = 308 cm^2

$2\pi rh = 308$

$\Rightarrow 2 \times 22/7 \times 7 \times h = 308$

(using (1))

$\Rightarrow h = 7 \text{ cm}$

Now,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 7 \times 7 \times 7$$

$$= 1078$$

Therefore, Volume of cylinder is 1078 cm^3 .

Question 12: The curved surface area of a cylinder is 1320 cm^2 and its base had diameter 21 cm. Find the height and volume of the cylinder.

Solution:

$$\text{Curved surface area of a cylinder} = 1320 \text{ cm}^2$$

Let, r be the radius of the cylinder and h be the height of the cylinder.

$$\Rightarrow r = \text{diameter}/2 = 21/2 \text{ cm} = 10.5 \text{ cm}$$

$$\text{We know, Curved surface area(CSA)} = 2\pi r h$$

$$\text{So, } 2\pi r h = 1320$$

$$\Rightarrow 2 \times \frac{22}{7} \times 10.5 \times h = 1320$$

$$\text{or } h = 20 \text{ cm}$$

Now,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 10.5 \times 10.5 \times 20$$

$$= 6930$$

Thus, Volume of cylinder is 6930 cm^3 .

Question 13: The ratio between the radius of the base and the height of a cylinder is 2:3. Find the total surface area of the cylinder, if its volume is 1617 cm^3 .

Solution:

Let, r be the radius of the cylinder and h be the height of the cylinder.

As per statement: $r:h = 2:3$

Then, radius = $2x$ cm and height = $3x$ cm

Volume of cylinder = $\pi r^2 h$

And Volume of cylinder = 1617 cm^3 (given)

So, $1617 = \frac{22}{7} (2x)^2 3x$

$1617 = \frac{22}{7} (12 x^3)$

$x^3 = \frac{343}{8}$

or $x = \frac{7}{2}$

or $x = 3.5$ cm

Now, radius, $r = 2 \times 3.5 = 7$ cm and

Height = $3x = 3 \times 3.5 = 10.5$ cm

Now,

Total surface area of cylinder = $2\pi r(h+r)$

= $2 \times \frac{22}{7} \times 7(10.5+7)$

= 770

Thus, Total surface area of cylinder is 770 cm^2 .

Question 14: A rectangular sheet of paper, 44 cm x 20 cm, is rolled along its length of form cylinder. Find the volume of the cylinder so formed.

Solution:

Length of a rectangular sheet = 44 cm

Height of a rectangular sheet = 20 cm

Now, $2\pi r = 44$

$r = \frac{44}{2\pi}$

$r = 44 \times \frac{1}{2} \times \frac{7}{22}$

or $r = 7$ cm

Now,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 7 \times 7 \times 20$$

$$= 3080$$

So, Volume of cylinder is 3080 cm^3 .

Question 15: The curved surface area of cylindrical pillar is 264 m^2 and its volume is 924 m^3 . Find the diameter and the height of the pillar.

Solution:

Let, r be the radius of the cylindrical pillar and h be the height of the cylindrical pillar

$$\text{Curved surface area of cylindrical pillar} = \text{CSA} = 264 \text{ m}^2 \quad (\text{Given})$$

$$\text{So, } 2\pi r h = 264$$

$$\text{or } \pi r h = 132 \quad \dots(1)$$

Again,

$$\text{Volume of the cylinder} = 924 \text{ m}^3 \quad (\text{given})$$

$$\pi r^2 h = 924$$

$$\text{or } \pi r h(r) = 924$$

Using equation (1)

$$132 r = 924$$

$$\text{or } r = 924/132$$

$$\text{or } r = 7 \text{ m}$$

Substitute value of r value in equation (1)

$$\frac{22}{7} \times 7 \times h = 132$$

$$\text{Or } h = 6 \text{ m}$$

Therefore, diameter = $2r = 2(7) = 14 \text{ m}$ and height = 6 m