

Exercise 21.1

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Question 1: Find the surface area of a sphere of radius: (i) 10.5 cm (ii) 5.6 cm (iii) 14 cm

Solution:

Surface area of a sphere = $4\pi r^2$

Where, r = radius of a sphere

(i) Radius = 10.5 cm

Surface area = $4 \times 22/7 \times (10.5)^2$

= 1386

Surface area is 1386 cm²

(ii) Radius= 5.6 cm

Surface area = $4 \times 22/7 \times (5.6)^2$

= 394.24

Surface area is 394.24 cm²

(iii) Radius = 14 cm

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Surface area = 4 \times 22/7 \times (14)^2
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= 2464
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Surface area is 2464 cm²

Question 2: Find the surface area of a sphere of diameter: (i) 14 cm (ii) 21 cm (iii) 3.5 cm

Solution: Surface area of a sphere = $4\pi r^2$

Where, r = radius of a sphere



- (i) Diameter= 14 cm
- So, Radius = Diameter/2 = 14/2 cm = 7 cm

Surface area = $4 \times 22/7 \times (7)^2$

= 616

Surface area is 616 cm²

(ii) Diameter = 21cm

So, Radius = Diameter/2 = 21/2 cm = 10.5 cm

Surface area= $4 \times 22/7 \times (10.5)^2$

= 1386

Surface area is 1386 cm²

(iii) Diameter= 3.5cm

So, Radius = Diameter/2 = 3.5/2 cm = 1.75 cm

Surface area = $4 \times 22/7 \times (1.75)^2$

= 38.5

Surface area is 38.5 cm²

Question 3: Find the total surface area of a hemisphere and a solid hemisphere each of radius 10 cm. (π =3.14)

Solution: Radius of a hemisphere = Radius of a solid hemisphere = 10 cm (Given)

Surface area of the hemisphere = $2\pi r^2$

 $= 2 \times 3.14 \times (10)^2$ cm²

 $= 628 \text{ cm}^2$



And, surface area of solid hemisphere = $3\pi r^2$

 $= 3 \times 3.14 \times (10)^2$ cm²

 $= 942 \text{ cm}^2$

Question 4: The surface area of a sphere is 5544 cm², find its diameter.

Solution:

Surface area of a sphere is 5544 cm²

Surface area of a sphere = $4\pi r^2$

So, $4\pi r^2 = 5544$

 $4 \times 22/7 \times (r)^2 = 5544$

 $r^2 = (5544 \times 7)/88$

 $r^2 = 441$

or r = 21cm

Now, Diameter=2(radius) = 2(21) = 42cm

Question 5: A hemispherical bowl made of brass has inner diameter 10.5 cm. Find the cost of tin plating it on the inside at the rate of Rs.4 per 100 cm².

Solution:

Inner diameter of hemispherical bowl = 10.5 cm

So, radius = Diameter/2 = 10.5/2 cm = 5.25 cm

Now, Surface area of hemispherical bowl = $2\pi r^2$

 $= 2 \times 3.14 \times (5.25)^2$

= 173.25

So, Surface area of hemispherical bowl is 173.25 cm²



Find the cost: Cost of tin plating 100 cm² area= Rs.4 (given)

Cost of tin plating 173.25cm² area = Rs. 4×173.25100 = Rs. 6.93

Therefore, cost of tin plating the inner side of hemispherical bowl is Rs.6.93.

Question 6: The dome of a building is in the form of a hemisphere. Its radius is 63 dm. Find the cost of painting it at the rate of Rs. 2 per sq m.

Solution:

Radius of hemispherical dome = 63 dm or 6.3 m

Inner surface area of dome = $2\pi r^2$

=2×3.14×(6.3)²

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= 249.48
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So, Inner surface area of dome is 249.48 m²

Now find the cost:

Cost of painting $1m^2 = Rs.2$ (given)

Therefore, cost of painting 249.48 m² = Rs. (249.48×2) = Rs.498.96.



Exercise 21.2

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Question 1: Find the volume of a sphere whose radius is: (i) 2 cm (ii) 3.5 cm (iii) 10.5 cm.

Solution:

Volume of a sphere = $4/3\pi r^3$ Cubic Units Where, r = radius of a sphere

(i) Radius = 2 cm

Volume = $4/3 \times 22/7 \times (2)^3$

= 33.52

Volume = 33.52 cm³

(ii) Radius = 3.5cm

Therefore volume = $4/3 \times 22/7 \times (3.5)^3$ = 179.666

Volume = 179.666 cm³

(iii) Radius = 10.5 cm

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Volume = 4/3 \times 22/7 \times (10.5)^3
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= 4851

Volume = 4851 cm^3

Question 2: Find the volume of a sphere whose diameter is: (i) 14 cm (ii) 3.5 dm (iii) 2.1 m

Solution:

Volume of a sphere = $4/3\pi r^3$ Cubic Units Where, r = radius of a sphere

(i) diameter =14 cm So, radius = diameter/2 = 14/2 = 7cm



Volume = $4/3 \times 22/7 \times (7)^3$

= 1437.33

Volume = 1437.33 cm³

(ii) diameter = 3.5 dm

So, radius = diameter/2 = 3.5/2 = 1.75 dm

Volume = $4/3 \times 22/7 \times (1.75)^3$

= 22.46

Volume = 22.46 dm^{3}

(iii) diameter = 2.1 m

So, radius = diameter/2 = 2.1/2 = 1.05 m

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Volume = 4/3×22/7×(1.05)<sup>3</sup>
= 4.851
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Volume = 4.851 m³

Question 3: A hemispherical tank has the inner radius of 2.8 m. Find its capacity in liters.

Solution:

Radius of hemispherical tank = 2.8 m

Capacity of hemispherical tank = $2/3 \pi r^3$

=2/3×22/7×(2.8)³ m³

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= 45.997 m<sup>3</sup>
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[Using 1m³ = 1000 liters]

Therefore, capacity in litres = 45997 litres



Question 4: A hemispherical bowl is made of steel 0.25 cm thick. The inside radius of the bowl is 5 cm. Find the volume of steel used in making the bowl.

Solution:

Inner radius of a hemispherical bowl = 5 cm

Outer radius of a hemispherical bowl = 5 cm + 0.25 cm = 5.25 cm

Volume of steel used = Outer volume - Inner volume

 $= 2/3 \times \pi \times ((5.25)^3 - (5)^3)$

 $= 2/3 \times 22/7 \times ((5.25)^3 - (5)^3)$

= 41.282

Volume of steel used is 41.282 cm³

Question 5: How many bullets can be made out of a cube of lead, whose edge measures 22 cm, each bullet being 2 cm in diameter?

Solution:

Edge of a cube = 22 cm Diameter of bullet = 2 cm So, radius of bullet (r) = 1 cm

Volume of the cube = $(side)^3 = (22)^3 \text{ cm}^3 = 10648 \text{ cm}^3$

And,

Volume of each bullet which will be spherical in shape = $4/3\pi r^3$

 $= 4/3 \times 22/7 \times (1)^3$ cm³

 $= 4/3 \times 22/7 \text{ cm}^3$

= 88/21 cm³

Number of bullets = (Volume of cube) / (Volume of bullet)



= 10648/88/21 = 2541

Therefore, 2541 bullets can be made.

Question 6: A shopkeeper has one laddoo of radius 5 cm. With the same material, how many laddoos of radius 2.5 cm can be made?

Solution:

Volume of laddoo having radius 5 cm (V1) = $4/3 \times 22/7 \times (5)^3$

= 11000/21 cm³

Also, Volume of laddoo having radius 2.5 cm (V2) = $4/3\pi r^3$

 $= 4/3 \times 22/7 \times (2.5)^3$ cm³

= 1375/21 cm³

Therefore,

Number of laddoos of radius 2.5 cm that can be made = V1/V2 = 11000/1375 = 8

Question 7: A spherical ball of lead 3 cm in diameter is melted and recast into three spherical balls. If the diameters of two balls be 3/2cm and 2 cm, find the diameter of the third ball.

Solution:

Volume of lead ball with radius $3/2 \text{ cm} = 4/3\pi r^3$

 $= 4/3 \times \pi \times (3/2)^3$

Let, Diameter of first ball (d1) = 3/2cm

Radius of first ball (r1) = 3/4 cm

Diameter of second ball (d2) = 2 cm

Radius of second ball $(r_2) = 2/2 \text{ cm} = 1 \text{ cm}$

Diameter of third ball (d3) = d

Radius of third ball (r3) = d/2 cm



Now,

Volume of lead ball=
$$\frac{4}{3} \times \pi \times \left(\frac{3}{4}\right)^3 + \frac{4}{3} \times \pi \times \left(1\right)^3 + \frac{4}{3} \times \pi \times \left(\frac{d}{2}\right)^3$$

 $\frac{4}{3} \times \pi \times \left(\frac{3}{2}\right)^3 = \frac{4}{3} \times \pi \times \left(\frac{3}{4}\right)^3 + \frac{4}{3} \times \pi \times \left(1\right)^3 + \frac{4}{3} \times \pi \times \left(\frac{d}{2}\right)^3$
 $\frac{4}{3} \pi \left[\left(\frac{3}{2}\right)^3 \right] = \frac{4}{3} \pi \left[\left(\frac{3}{4}\right)^3 + \left(1\right)^3 + \left(\frac{d}{2}\right)^3 \right]$
 $\frac{27}{8} = \frac{27}{64} + 1 + \frac{d^3}{8}$
 $d^3 = 8 \left[\frac{27}{8} - \frac{27}{64} - 1 \right]$
 $\frac{d^3}{8} = \frac{125}{64}$
 $\frac{d}{2} = \frac{5}{4}$
 $d = \frac{10}{4}$
 $d = 2.5$

So, diameter of third ball is 2.5 cm.

Question 8: A sphere of radius 5 cm is immersed in water filled in a cylinder, the level of water rises 5/3 cm. Find the radius of the cylinder.

Solution:

Radius of sphere = 5 cm (Given) Let 'r' be the radius of cylinder. We know, Volume of sphere = $4/3\pi r^3$

By putting values, we get

 $= 4/3 \times \pi \times (5)^3$

Height (h) of water rises is 5/3 cm (Given)

Volume of water rises in cylinder = $\pi r^2 h$

Therefore, Volume of water rises in cylinder = Volume of sphere

So, $\pi r^2 h = 4/3\pi r^3$

 $\pi r^2 \times 5/3 = 4/3 \times \pi \times (5)^3$



or $r^2 = 100$

or r = 10

Therefore, radius of the cylinder is 10 cm.

Question 9: If the radius of a sphere is doubled, what is the ratio of the volume of the first sphere to that of the second sphere?

Solution:

Let r be the radius of the first sphere then 2r be the radius of the second sphere.

Now,

Volume of first sphere Volume of second sphere $=\frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi (2r)^3} =$

Ratio of volume of the first sphere to the second sphere is 1:8.

Question 10: A cone and a hemisphere have equal bases and equal volumes. Find the ratio of their heights.

Solution:

Volume of the cone = Volume of the hemisphere (Given)

 $1/3\pi r^2 h = 2/3 \pi r^3$ (Using respective formulas)

 $r^{2}h = 2r^{3}$

or h = 2r

Since, cone and a hemisphere have equal bases which implies they have the same radius. h/r = 2



or h : r = 2 : 1

Therefore, Ratio of their heights is 2:1

Question 11: A vessel in the form of a hemispherical bowl is full of water. Its contents are emptied in a right circular cylinder. The internal radii of the bowl and the cylinder are 3.5 cm and 7 cm respectively. Find the height to which the water will rise in the cylinder.

Solution:

Volume of water in the hemispherical bowl = Volume of water in the cylinder ... (Given)

Inner radius of the bowl (r_1) = 3.5cm

Inner radius of cylinder $(r_2) = 7$ cm

Volume of water in the hemispherical bowl = Volume of water in the cylinder

 $2/3\pi r_1^3 = \pi r_2^2 h$ [Using respective formulas]

Where h be the height to which water rises in the cylinder.

 $2/3\pi(3.5)^3 = \pi(7)^2h$

or h = 7/12

Therefore, 7/12 cm be the height to which water rises in the cylinder.

Question 12: A cylinder whose height is two thirds of its diameter, has the same volume as a sphere of radius 4 cm. Calculate the radius of the base of the cylinder.

Solution: Radius of a sphere (R)= 4 cm (Given) Height of the cylinder = 2/3 diameter (given)

We know, Diameter = 2(Radius)

Let h be the height and r be the base radius of a cylinder, then

 $h = 2/3 \times (2r) = 4r/3$



Volume of the cylinder = Volume of the sphere

 $\pi r^2 h = 4/3\pi R^3$

 $\pi \times r^2 \times (4r/3) = 4/3 \pi (4)^3$

 $(r)^3 = (4)^3$

or r = 4

Therefore, radius of the base of the cylinder is 4 cm.

Question 13: A vessel in the form of a hemispherical bowl is full of water. The contents are emptied into a cylinder. The internal radii of the bowl and cylinder are respectively 6 cm and 4 cm. Find the height of water in the cylinder.

Solution:

Radius of a bowl (R)= 6 cm (Given)

Radius of a cylinder (r) = 4 cm (given)

Let h be the height of a cylinder. Now, Volume of water in hemispherical bowl = Volume of cylinder

 $2/3 \pi R^3 = \pi r^2 h$

 $2/3 \pi (6)^3 = \pi (4)^2 h$

or h = 9

Therefore, height of water in the cylinder 9 cm.

Question 14: A cylindrical tub of radius 16 cm contains water to a depth of 30 cm. A spherical iron ball is dropped into the tub and thus level of water is raised by 9 cm. What is the radius of the ball?

Solution:

Let r be the radius of the iron ball.



Radius of the cylinder (R) = 16 cm (Given)

A spherical iron ball is dropped into the cylinder and thus the level of water is raised by 9 cm. So, height (h) = 9 cm

From statement,

Volume of iron ball = Volume of water raised in the hub

 $4/3\pi r^3 = \pi R^2 h$ $4/3 r^3 = (16)^2 \times 9$ or $r^3 = 1728$ or r = 12Therefore, radius of the ball = 12cm.





Exercise VSAQs

Page No: 21.25

Question 1: Find the surface area of a sphere of radius 14 cm.

Solution:

Radius of a sphere (r) = 14 cm

Surface area of a sphere = $4\pi r^2$

 $= 4 \times (22/7) \times 14^2 \text{ cm}^2$

 $= 2464 \text{ cm}^2$

Question 2: Find the total surface area of a hemisphere of radius 10 cm.

Solution:

Radius of a hemisphere (r) = 10 cm

Total surface area of a hemisphere = $3\pi r^2$

 $= 3 \times (22/7) \times 10^2 \text{ cm}^2$

 $= 942 \text{ cm}^2$

Question 3: Find the radius of a sphere whose surface area is 154 cm². Solution:

Surface area of a sphere = 154 cm^2

We know, Surface area of a sphere = $4\pi r^2$

So, $4\pi r^2 = 154$

4 x 22/7 x r² = 154

 $r^2 = 49/4$

or r = 7/2 = 3.5

Radius of a sphere is 3.5 cm.



Question 4: The hollow sphere, in which the circus motor cyclist performs his stunts, has a diameter of 7 m. Find the area available to the motorcyclist for riding.

Solution:

Diameter of hollow sphere = 7 m

So, radius of hollow sphere = 7/2 m = 3.5 cm

Now,

Area available to the motorcyclist for riding = Surface area of a sphere = $4\pi r^2$

$$= 4 \times (22/7) \times 3.5^2 \text{ m}^2$$

= 154 m²

Question 5: Find the volume of a sphere whose surface area is 154 cm².

Solution:

Surface area of a sphere = 154 cm²

We know, Surface area of a sphere = $4\pi r^2$

So, $4\pi r^2 = 154$

 $4 \times 22/7 \times r^2 = 154$

or $r^2 = 49/4$

or r = 7/2 = 3.5

Radius (r) = 3.5 cm

Now, Volume of sphere = $4/3 \pi r^3$

 $= (4/3) \pi \times 3.5^3$

= 179.66

Therefore, Volume of sphere is 179.66 cm³.