

EXERCISE 5.1

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1. Add the following rational numbers:

(i) $(-5/7)$ and $(3/7)$

(ii) $(-15/4)$ and $(7/4)$

(iii) $(-8/11)$ and $(-4/11)$

(iv) $(6/13)$ and $(-9/13)$

Solution:

(i) Given $(-5/7)$ and $(3/7)$

$$= (-5/7) + (3/7)$$

Here denominators are same so add the numerator

$$= ((-5+3)/7)$$

$$= (-2/7)$$

(ii) Given $(-15/4)$ and $(7/4)$

$$= (-15/4) + (7/4)$$

Here denominators are same so add the numerator

$$= ((-15 + 7)/4)$$

$$= (-8/4)$$

On simplifying

$$= -2$$

(iii) Given $(-8/11)$ and $(-4/11)$

$$= (-8/11) + (-4/11)$$

Here denominators are same so add the numerator

$$= (-8 + (-4))/11$$

$$= (-12/11)$$

(iv) Given $(6/13)$ and $(-9/13)$

$$= (6/13) + (-9/13)$$

Here denominators are same so add the numerator

$$= (6 + (-9))/13$$

$$= (-3/13)$$

2. Add the following rational numbers:

(i) $(3/4)$ and $(-3/5)$

(ii) -3 and $(3/5)$

(iii) $(-7/27)$ and $(11/18)$

(iv) $(31/-4)$ and $(-5/8)$

Solution:

(i) Given $(3/4)$ and $(-3/5)$

If p/q and r/s are two rational numbers such that q and s do not have a common factor other than one, then

$$(p/q) + (r/s) = (p \times s + r \times q) / (q \times s)$$

$$(3/4) + (-3/5) = (3 \times 5 + (-3) \times 4) / (4 \times 5)$$

$$= (15 - 12) / 20$$

$$= (3/20)$$

(ii) Given -3 and $(3/5)$

If p/q and r/s are two rational numbers such that q and s do not have a common factor other than one, then

$$(p/q) + (r/s) = (p \times s + r \times q) / (q \times s)$$

$$(-3/1) + (3/5) = (-3 \times 5 + 3 \times 1) / (1 \times 5)$$

$$= (-15 + 3) / 5$$

$$= (-12/5)$$

(iii) Given $(-7/27)$ and $(11/18)$

LCM of 27 and 18 is 54

$$(-7/27) = (-7/27) \times (2/2) = (-14/54)$$

$$(11/18) = (11/18) \times (3/3) = (33/54)$$

$$(-7/27) + (11/18) = (-14 + 33) / 54$$

$$= (19/54)$$

(iv) Given $(31/-4)$ and $(-5/8)$

LCM of -4 and 8 is 8

$$(31/-4) = (31/-4) \times (2/2) = (62/-8)$$

$$(31/-4) + (-5/8) = (-62 - 5) / 8$$

$$= (-67/8)$$

3. Simplify:

(i) $(8/9) + (-11/6)$

(ii) $(-5/16) + (7/24)$

(iii) $(1/-12) + (2/-15)$

(iv) $(-8/19) + (-4/57)$

Solution:

(i) Given $(8/9) + (-11/6)$

The LCM of 9 and 6 is 18

$$(8/9) = (8/9) \times (2/2) = (16/18)$$

$$(-11/6) = (-11/6) \times (3/3) = (-33/18)$$

$$= (16 - 33)/18$$

$$= (-17/18)$$

(ii) Given $(-5/16) + (7/24)$

The LCM of 16 and 24 is 48

$$\text{Now } (-5/16) = (-5/16) \times (3/3) = (-15/48)$$

$$\text{Consider } (7/24) = (7/24) \times (2/2) = (14/48)$$

$$(-5/16) + (7/24) = (-15/48) + (14/48)$$

$$= (14 - 15)/48$$

$$= (-1/48)$$

(iii) Given $(1/-12) + (2/-15)$

The LCM of 12 and 15 is 60

$$\text{Consider } (-1/12) = (-1/12) \times (5/5) = (-5/60)$$

$$\text{Now } (2/-15) = (-2/15) \times (4/4) = (-8/60)$$

$$(1/-12) + (2/-15) = (-5/60) + (-8/60)$$

$$= (-5 - 8)/60$$

$$= (-13/60)$$

(iv) Given $(-8/19) + (-4/57)$

The LCM of 19 and 57 is 57

$$\text{Consider } (-8/57) = (-8/57) \times (3/3) = (-24/57)$$

$$(-8/19) + (-4/57) = (-24/57) + (-4/57)$$

$$= (-24 - 4)/57$$

$$= (-28/57)$$

4. Add and express the sum as mixed fraction:

(i) $(-12/5) + (43/10)$

(ii) $(24/7) + (-11/4)$

(iii) $(-31/6) + (-27/8)$

Solution:

(i) Given $(-12/5) + (43/10)$

The LCM of 5 and 10 is 10

Consider $(-12/5) = (-12/5) \times (2/2) = (-24/10)$

$(-12/5) + (43/10) = (-24/10) + (43/10)$

$= (-24 + 43)/10$

$= (19/10)$

Now converting it into mixed fraction

$= 1 \frac{9}{10}$

(ii) Given $(24/7) + (-11/4)$

The LCM of 7 and 4 is 28

Consider $(24/7) = (24/7) \times (4/4) = (96/28)$

Again $(-11/4) = (-11/4) \times (7/7) = (-77/28)$

$(24/7) + (-11/4) = (96/28) + (-77/28)$

$= (96 - 77)/28$

$= (19/28)$

(iii) Given $(-31/6) + (-27/8)$

The LCM of 6 and 8 is 24

Consider $(-31/6) = (-31/6) \times (4/4) = (-124/24)$

Again $(-27/8) = (-27/8) \times (3/3) = (-81/24)$

$(-31/6) + (-27/8) = (-124/24) + (-81/24)$

$= (-124 - 81)/24$

$= (-205/24)$

Now converting it into mixed fraction

$= -8 \frac{13}{24}$