

EXERCISE 11(A)

1. Express each of the following ratios in its simplest form

(a) (i) 4: 6

(ii) 48: 54

(iii) 200: 250

(b) (i) 5 kg: 800 gm

(ii) 30 cm: 2 m

(iii) 3m: 90 cm

(iv) 2 years: 9 months

(v) 1 hour: 45 minutes

(c) (i) $1\frac{1}{2} : 2\frac{1}{2}$

(ii) $3\frac{1}{2} : 7$

(iii) $2\frac{1}{3} : 3\frac{1}{2} : 1\frac{1}{4}$

(iv) $x^2 : 4x$

(v) 2.5: 1.5

Solution:

(a) (i) Given ratio

4: 6

This can be written as

$4 / 6$

$= 2 / 3$

$= 2: 3$

Hence, 2: 3 is the simplest form of 4: 6

(ii) Given

48: 54

This can be written as

$48 / 54$

$= 8 / 9$

$= 8: 9$

Hence, 8: 9 is the simplest form of 48: 54

(iii) Given

200: 250

This can be written as

$200 / 250$

$= 4 / 5$

$= 4: 5$

Hence, 4: 5 is the simplest form of 200: 250

(b) (i) Given

5 kg: 800 gm

$$5 \text{ kg} = 5 \times 1000 \text{ gm} = 5000 \text{ gm}$$

[\because 1 kg = 1000 gm]

This can be written as

$$5000 \text{ gm} / 800 \text{ gm}$$

$$= 25 \text{ gm} / 4 \text{ gm}$$

$$= 25 \text{ gm} : 4 \text{ gm}$$

Hence, 25 gm: 4 gm is the simplest form of 5 kg: 800 gm

(ii) 30 cm: 2 m

We know that, 1 m = 100 cm

$$2 \text{ m} = 2 \times 100 \text{ cm}$$

$$= 200 \text{ cm}$$

Given

30 cm: 2 m

This can be written as

$$30 \text{ cm} / 200 \text{ cm}$$

$$= 3 \text{ cm} / 20 \text{ cm}$$

$$= 3 \text{ cm} : 20 \text{ cm}$$

Hence, 3 cm: 20 cm is the simplest form of 30 cm: 2 m

(iii) 3 m: 90 cm

We know that, 1 m = 100 cm

$$3 \text{ m} = 3 \times 100 \text{ cm}$$

$$= 300 \text{ cm}$$

Given

3 m: 90 cm

This can be written as

$$300 \text{ cm} / 90 \text{ cm}$$

$$= 10 \text{ cm} / 3 \text{ cm}$$

$$= 10 \text{ cm} : 3 \text{ cm}$$

Hence, 10 cm: 3 cm is the simplest form of 3 m: 90 cm

(iv) 2 years: 9 months

We know that, 1 year = 12 months

$$2 \text{ years} = 2 \times 12 \text{ months}$$

$$= 24 \text{ months}$$

Given

2 years: 9 months

This can be written as

$$24 \text{ months} / 9 \text{ months}$$

$$= 8 \text{ months} / 3 \text{ months}$$

= 8 months: 3 months

Hence, 8 months: 3 months is the simplest form of 2 years: 9 months

(v) 1 hour: 45 minutes

We know that, 1 hour = 60 minutes

Given

1 hour: 45 minutes

This can be written as

60 minutes / 45 minutes

= 4 minutes / 3 minutes

= 4 minutes: 3 minutes

Hence, 4 minutes: 3 minutes is the simplest form of 1 hour: 45 minutes

(c) (i) $1\frac{1}{2} : 2\frac{1}{2}$

This can be written as

$3/2 : 5/2$

By further calculation, we get

$3/2 \times 2/5$

= $3/5$

= 3: 5

Hence, the simplest form of $1\frac{1}{2} : 2\frac{1}{2}$ is 3: 5

(ii) $3\frac{1}{2} : 7$

This can be written as

$7/2 : 7/1$

On further calculation, we get

$7/2 \times 1/7$

= $1/2$

= 1: 2

Hence, the simplest form of $3\frac{1}{2} : 7$ is 1: 2

(iii) $2\frac{1}{3} : 3\frac{1}{2} : 1\frac{1}{4}$

This can be written as

$7/3 : 7/2 : 5/4$

Now, taking L.C.M of 3, 2 and 4 we get

$7/3 \times 12 : 7/2 \times 12 : 5/4 \times 12$

= 28: 42: 15

Hence, the simplest form of $2\frac{1}{3} : 3\frac{1}{2} : 1\frac{1}{4}$ is 28: 42: 15

(iv) $x^2: 4x$

This can be written as

$$x^2 / 4x$$

$$= (x \times x) / (4 \times x)$$

$$= x / 4$$

$$= x: 4$$

Hence, the simplest form of $x^2: 4x$ is $x: 4$

(v) $2.5: 1.5$

This can be written as

$$25 / 10: 15 / 10$$

On further calculation, we get

$$= 25 / 10 \times 10 / 15$$

$$= 25 / 15$$

$$= 5 / 3$$

$$= 5: 3$$

Hence, the simplest form of $2.5: 1.5$ is $5: 3$

2. A field is 80 m long and 60 m wide. Find the ratio of its width to its length.

Solution:

Given

Width of the field = 60 m

Length of the field = 80 m

Ratio of its width to its length = 60: 80

On further simplification, we get

$$= 60 / 80$$

$$= 3 / 4$$

$$= 3: 4$$

Hence, the ratio of its width to its length is 3: 4

3. State, true or false:

(i) A ratio equivalent to 7: 9 is 27: 21

(ii) A ratio equivalent to 5: 4 is 240: 192

(iii) A ratio of 250 gm and 3 kg is 1: 12

Solution:

(i) False

Correct statement: A ratio equivalent to 7: 9 is 9: 7

(ii) True

(iii) True

4. Is the ratio of 15 kg and 35 kg same as the ratio of 6 years and 14 years?

Solution:

Ratio of 15 kg and 35 kg = 15 kg : 35 kg

We get

$$15 \text{ kg} / 35 \text{ kg}$$

On simplification, we get

$$= 3 \text{ kg} / 7 \text{ kg}$$

$$= 3 : 7$$

Now, the ratio of 6 years and 14 years = 6 years : 14 years

We get

$$6 \text{ years} / 14 \text{ years}$$

On simplification, we get

$$= 3 \text{ years} / 7 \text{ years}$$

$$= 3 : 7$$

Since both the ratios = 3 : 7

Hence, the ratios are same in both the cases

5. Is the ratio of 6 g and 15 g same as the ratio of 36 cm and 90 cm?**Solution:**

Ratio of 6 g and 15 g = 6 g : 15 g

On calculating further, we get

$$= 6 / 15$$

$$= 2 / 5$$

$$= 2 : 5$$

Now, the ratio of 36 cm and 90 cm = 36cm : 90 cm

By calculating further, we get

$$= 36 / 90$$

$$= 18 / 45$$

$$= 6 / 15$$

$$= 2 / 5$$

$$= 2 : 5$$

Since both the ratios = 2 : 5

Hence, the ratios are same in both the cases

6. Find the ratio between 3.5 m, 475 cm and 2.8 m**Solution:**

Given

3.5 m, 475 cm and 2.8 m

Now, convert all the values into cm

$$1 \text{ m} = 100 \text{ cm}$$

Hence,

$$3.5 \times 100 = 350 \text{ cm}$$

$$2.8 \times 100 = 280 \text{ cm}$$

Hence,

$$350 \text{ cm}: 475 \text{ cm}: 280 \text{ cm}$$

The H.C.F. of 350, 475 and 280 is 5

So, the ratio will be

$$350 / 5: 475 / 5: 280 / 5$$

$$= 70: 95: 56$$

Therefore, the ratio between 3.5 m, 475 cm and 2.8 m is 70: 95: 56

7. Find the ratio between 5 dozen and 2 scores. [1 score = 20]

Solution:

Given

5 dozens and 2 scores

We know that,

$$1 \text{ dozen} = 12 \text{ and } 1 \text{ score} = 20$$

Hence,

$$5 \text{ dozens} = 12 \times 5$$

$$= 60$$

$$2 \text{ scores} = 2 \times 20$$

$$= 40$$

So, the ratio will be

$$60: 40 = 60 / 40$$

$$= 3 / 2$$

$$= 3: 2$$

Hence, the ratio between 5 dozens and 2 scores is 3: 2