

JEE Main 2021 Paper

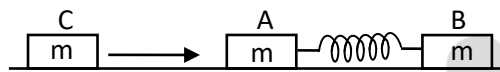


Date: 17th March 2021 (Shift-2)

Subject: Physics

Section - A

1. Two identical blocks A and B each of mass m resting on the smooth horizontal floor are connected by a light spring of natural length L and spring constant K . A third block C of mass m moving with a speed v along the line joining A and B collides elastically with A. The maximum compression in the spring is



a. $\sqrt{\frac{mv}{2K}}$

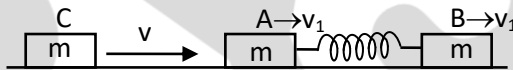
b. $\sqrt{\frac{m}{2K}}$

c. $\sqrt{\frac{mv}{K}}$

d. $v\sqrt{\frac{m}{2K}}$

Answer (d)

Sol.

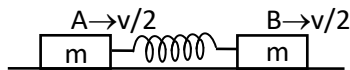


Let v_1 be the common velocity of blocks A and B at the maximum compression of the spring

From conservation of momentum

$$mv = mv_1 + mv_1$$

$$v_1 = \frac{v}{2}$$



& from energy conservation

$$\frac{1}{2}mv^2 = \left(\frac{1}{2} \times m \left(\frac{v}{2}\right)^2\right) \times 2 + \frac{1}{2}Kx^2$$

$$\frac{mv^2}{2} - \frac{mv^2}{4} = \frac{1}{2}Kx^2$$

$$\frac{mv^2}{4} = \frac{1}{2}Kx^2$$

Then the maximum compression in the spring is

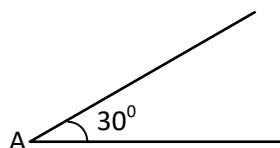
$$x = \sqrt{\frac{mv^2}{2K}}$$

$$x = v\sqrt{\frac{m}{2K}}$$

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B

2. A solid sphere of mass 2 kg radius 0.5 m is rolling with an initial speed of 1 ms^{-1} goes up an inclined plane which makes an angle of 30° with the horizontal plane, without slipping. How long will the sphere take to return to the starting point A ?

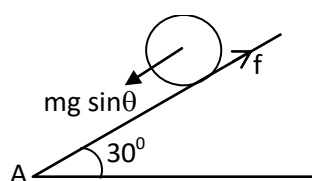


- a. 0.80 s
c. 0.52 s

- b. 0.60 s
d. 0.57 s

Answer (d)

Sol.



$$a = \frac{g \sin \theta}{1 + c}$$

For a solid sphere $c = \frac{2}{5}$

$$a = \frac{9.8 \sin 30^\circ}{1 + \frac{2}{5}}$$

$$a = 3.5\text{ m/sec}^2$$

Time of ascent is given by

$$v = u + at$$

$$0 = 1 - 3.5 t$$

$$t = \frac{1}{3.5}\text{ sec.}$$

Time of decent

$$t = \frac{1}{3.5}\text{ sec. [due to symmetry of motion]}$$

$$\text{Total time } T = \frac{2}{3.5} = 0.57\text{ sec.}$$

3. If one mole of a polyatomic gas has two vibrational modes and β is the ratio of molar specific heats for polyatomic gas ($\beta = \frac{C_p}{C_v}$) then the value of β is :

- a. 1.35
c. 1.25

- b. 1.02
d. 1.2

Answer (d)

Sol.

Degree of freedom of polyatomic gas

Here, no of translational dof = 3,

no of rotational dof = 3

and no of vibrational dof = $2 \times 2 = 4$

Therefore, total no of dof

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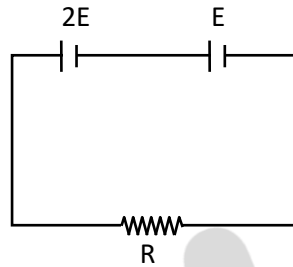


$$f = 3 + 3 + 4 = 10$$

$$\beta = \frac{C_P}{C_V} = 1 + \frac{2}{f} = 1 + \frac{2}{10}$$

$$\beta = \frac{12}{10} = 1.2$$

4. Two cells of emf $2E$ and E with internal resistance r_1 and r_2 respectively are connected in series to an external resistor R (see figure). The value of R , at which the potential difference across the terminals of the first cell becomes zero is



a. $r_1 - r_2$

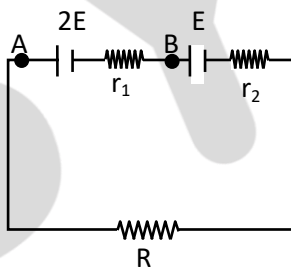
c. $\frac{r_1}{2} + r_2$

b. $r_1 + r_2$

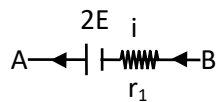
d. $\frac{r_1}{2} - r_2$

Answer (d)

Sol.



$$i = \frac{3E}{R + r_1 + r_2}$$



If potential difference across terminals of first cell is zero

$$V_A = V_B$$

$$2E = i r_1$$

$$2E = \frac{3E}{R + r_1 + r_2} r_1$$

$$2R + 2r_1 + 2r_2 = 3r_1$$

$$R = \frac{r_1}{2} - r_2$$

5. A sound wave of frequency 245 Hz travels with the speed of 300 ms^{-1} along the positive x-axis. Each point of the medium moves to and fro through a total

distance of 6 cm. What will be the mathematical expression of the travelling wave ?

a. $Y(x, t) = 0.03[\sin 5.1x - (0.2 \times 10^3)t]$

b. $Y(x, t) = 0.06[\sin 5.1x - (1.5 \times 10^3)t]$

c. $Y(x, t) = 0.06[\sin 0.8x - (0.5 \times 10^3)t]$

d. $Y(x, t) = 0.03[\sin 5.1x - (1.5 \times 10^3)t]$

Answer (d)

Sol.

General expression for wave travelling along positive x axis is of the form

$$Y = A \sin (kx - \omega t)$$

Here

$$A = \frac{6}{2} = 3 \text{ cm} = 0.03 \text{ m}$$

$$\omega = 2\pi f = 2\pi \times 245$$

$$\omega = 1.54 \times 10^3 \text{ rad s}^{-1}$$

$$k = \frac{\omega}{v} = \frac{1.54 \times 10^3}{300}$$

$$k = 5.1 \text{ m}^{-1}$$

$$y = 0.03 \sin (5.1x - 1.5 \times 10^3 t)$$

6. A carrier signal $C(t) = 25 \sin (2.512 \times 10^{10} t)$ is amplitude modulated by a message signal $m(t) = 5 \sin (1.57 \times 10^8 t)$ and transmitted through an antenna. What will be bandwidth of the modulated signal ?

a. 1987.5 MHz

b. 2.01 GHz

c. 50 MHz

d. 8 GHz

Answer (c)

Sol.

Bandwidth of modulated signal is given by,

$$\beta = 2f_m(t)$$

$$\beta = 2 \times \frac{1.57 \times 10^8}{2\pi}$$

$$\beta = 50 \text{ MHz}$$

7. Two particles A and B of equal masses are suspended from two massless springs of spring constants K_1 and K_2 respectively. If the maximum velocities during oscillations are equal, the ratio of the amplitude of A and B is :

a. $\frac{K_1}{K_2}$

b. $\sqrt{\frac{K_1}{K_2}}$

c. $\sqrt{\frac{K_2}{K_1}}$

d. $\frac{K_2}{K_1}$

Answer (c)

Sol.

$$\therefore V_{\max} = A\omega$$

Given $\omega_1 A_1 = \omega_2 A_2$

We know that $\omega = \sqrt{\frac{k}{m}}$

$$\sqrt{\frac{k_1}{m}} A_1 = \sqrt{\frac{k_2}{m}} A_2$$

$$\frac{A_1}{A_2} = \sqrt{\frac{k_2}{k_1}}$$

8. Match List I with List II

List I		List II	
(a)	Phase difference between current and voltage in a purely resistive AC circuit	(i)	$\frac{\pi}{2}$; current leads voltage
(b)	Phase difference between current and voltage in a pure inductive AC circuit	(ii)	zero
(c)	Phase difference between current and voltage in a pure capacitive AC circuit	(iii)	$\frac{\pi}{2}$; current lags voltage
(d)	Phase difference between current and voltage in an LCR series circuit	(iv)	$\tan^{-1}\left(\frac{X_C - X_L}{R}\right)$

Choose the most appropriate answer from the options given below :

a. (a)-(ii), (b)-(iii), (c)-(iv), (d)-(i)

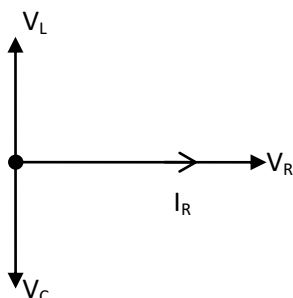
b. (a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

c. (a)-(ii), (b)-(iv), (c)-(iii), (d)-(i)

d. (a)-(ii), (b)-(iii), (c)-(i), (d)-(iv)

Answer (d)

Sol.



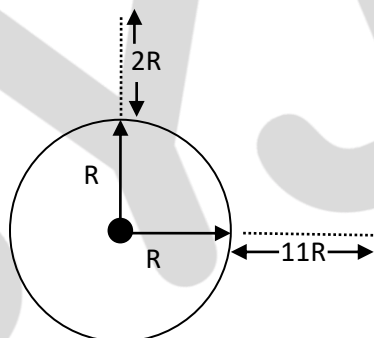
- (a) phase difference b/w current & voltage in a purely resistive AC circuit is zero
- (b) phase difference b/w current & voltage in a pure inductive AC circuit is $\frac{\pi}{2}$; current lags voltage.
- (c) phase different b/w current & voltage in a pure capacitive AC circuit is $\frac{\pi}{2}$; current lead voltage.
- (d) phase difference b/w current & voltage in an LCR series circuit is = $\tan^{-1} \left| \left(\frac{X_C - X_L}{R} \right) \right|$

9. A geostationary satellite is orbiting around an arbitrary planet 'P' at a height of $11R$ above the surface of 'P', R being the radius of 'P'. The time period of another satellite in hours at a height of $2R$ from the surface of 'P' is _____. 'P' has the time period of rotation of 24 hours.

- a. $\frac{6}{\sqrt{2}}$
- b. 3
- c. $6\sqrt{2}$
- d. 5

Answer (b)

Sol.



From Kepler's law

$$T^2 \propto R^3$$

Since time period of a geostationary satellite is equal to the time period of rotation of planet i.e. 24 hours,

Using Kepler's law

$$\left(\frac{24}{T} \right)^2 = \left(\frac{12R}{3R} \right)^3$$

$$T = 3 \text{ sec}$$

10. The velocity of a particle is $v = v_0 + gt + Ft^2$. Its position is $x = 0$ at $t = 0$; then its displacement after time ($t = 1$) is :

- a. $v_0 + \frac{g}{2} + F$
- b. $v_0 + 2g + 3F$
- c. $v_0 + g + F$
- d. $v_0 + \frac{g}{2} + \frac{F}{3}$

Answer (d)

Sol.

$$v = v_0 + gt + Ft^2$$

$$\frac{dx}{dt} = v_0 + gt + Ft^2$$

$$\int_{x=0}^x dx = \int_{t=0}^{t=1} (v_0 + gt + Ft^2) dt$$

$$x = \left[v_0 t + \frac{gt^2}{2} + \frac{Ft^3}{3} \right]_{t=0}^{t=1}$$

$$x = v_0 + \frac{g}{2} + \frac{F}{3}$$

- 11. A block of mass 1 kg attached to a spring is made to oscillate with an initial amplitude of 12 cm. After 2 minutes the amplitude decreases to 6 cm. Determine the value of the damping constant for this motion. (take $\ln 2 = 0.693$).**

- a. $(1) 3.3 \times 10^2 \text{ kg s}^{-1}$ b. $5.7 \times 10^{-3} \text{ kg s}^{-1}$
 c. $1.16 \times 10^{-2} \text{ kg s}^{-1}$ d. $0.69 \times 10^2 \text{ kg s}^{-1}$

Answer (c)

Sol.

Amplitude of a damped oscillation is given by

$$A = A_0 e^{\frac{-b}{2m}t}$$

$$6 = 12 e^{\frac{-b}{2 \times 1} \times 120}$$

$$6 = 12 e^{-b \times 60}$$

$$\frac{1}{2} = e^{-60b}$$

$$\ln(2) = 60b$$

$$b = \frac{\ln(2)}{60} = 1.16 \times 10^{-2} \text{ Kg/s}$$

- 12. An object is located at 2 km beneath the surface of the water. If the fractional compression $\frac{\Delta V}{V}$ is 1.36%, the ratio of hydraulic stress to the corresponding hydraulic strain will be**

[Given : density of water is 1000 kg m^{-3} and $g = 9.8 \text{ ms}^{-2}$]

- a. $2.26 \times 10^9 \text{ Nm}^{-2}$ b. $1.96 \times 10^7 \text{ Nm}^{-2}$
 c. $1.44 \times 10^7 \text{ Nm}^{-2}$ d. $1.44 \times 10^9 \text{ Nm}^{-2}$

Answer (d)

Sol.

Bulk modulus

$$\beta = \frac{\Delta p}{\frac{\Delta V}{V}}$$

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B

$$\beta = \frac{\rho gh}{\frac{\Delta V}{V}} = \frac{1000 \times 9.8 \times 2 \times 10^3}{\frac{1.36}{100}}$$
$$\beta = 1.44 \times 10^9 \text{ N/m}^2$$

13. Two identical photocathodes receive the light of frequencies f_1 and f_2 respectively. If the velocities of the photo-electrons coming out are v_1 and v_2 respectively, then

a. $v_1 + v_2 = \left[\frac{2h}{m} (f_1 + f_2) \right]^{\frac{1}{2}}$

b. $v_1 - v_2 = \left[\frac{2h}{m} (f_1 - f_2) \right]^{\frac{1}{2}}$

c. $v_1^2 + v_2^2 = \frac{2h}{m} [f_1 + f_2]$

d. $v_1^2 - v_2^2 = \frac{2h}{m} [f_1 - f_2]$

Answer (d)

Sol.

Using expression for K.E of photoelectrons

$$\frac{1}{2} m v_1^2 = h f_1 - \phi \quad (1)$$

$$\frac{1}{2} m v_2^2 = h f_2 - \phi \quad (2)$$

[ϕ is the same for same material of photocathodes]

Subtracting equation (1) by equation (2)

$$\frac{1}{2} m v_1^2 - \frac{1}{2} m v_2^2 = h f_1 - h f_2$$

$$v_1^2 - v_2^2 = \frac{2h}{m} (f_1 - f_2) \quad v_1^2 - v_2^2 = \frac{2h}{m} (f_1 - f_2)$$

14. The atomic hydrogen emits a line spectrum consisting of various series. Which series of hydrogen atomic spectra lies in the visible region ?

a. Balmer series

b. Lyman series

c. Brackett series

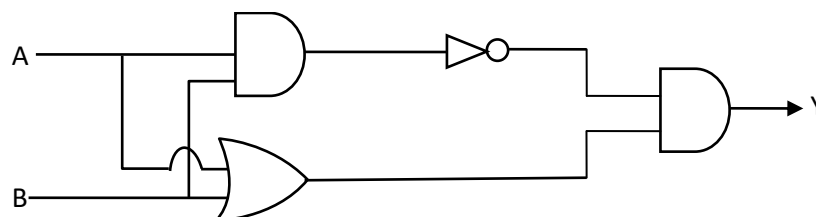
d. Paschen series

Answer (a)

Sol.

Balmer series of hydrogen atomic spectrum is lying in the visible region, when electron jumps from a higher energy level to $n = 2$ orbit.

15. Which one of the following will be the output of the given circuit ?



a. NAND Gate

b. AND Gate

c. XOR Gate

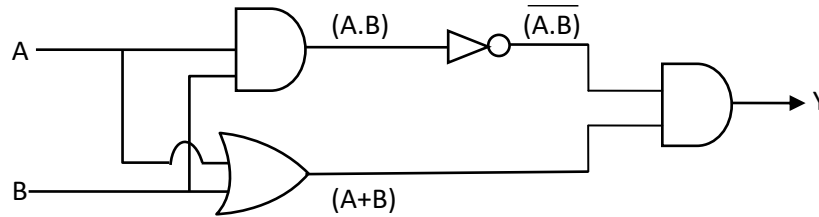
d. NOR Gate

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Answer (c)

Sol.

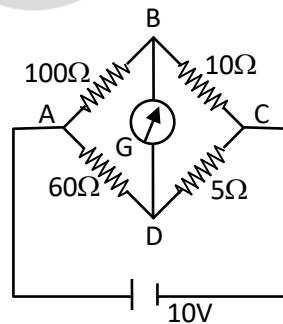


Output of the above circuit can be obtained as

$$\begin{aligned}
 y &= (\overline{A \cdot B}) \cdot (A + B) \\
 &= (\overline{A} + \overline{B}) \cdot (A + B) \quad [\text{De Morgan's law}] \\
 &= \overline{A} A + \overline{A} B + A \overline{B} + \overline{B} B \\
 &= 0 + \overline{A} B + A \overline{B} + 0 \\
 y &= \overline{A} B + A \overline{B}
 \end{aligned}$$

which is XOR gate

16. The four arms of a wheatstone bridge have resistances as shown in the figure. A galvanometer of 15Ω resistance is connected across BD . Calculate the current through the galvanometer when a potential difference of $10 V$ is maintained across AC .

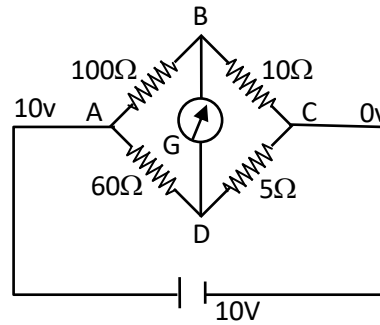


- | | |
|-----------------|-----------------|
| a. 4.87 mA | b. 4.87 μ A |
| c. 2.44 μ A | d. 2.44 mA |

Answer (a)

Sol.

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Applying KCL for point B,

$$\frac{V_B - 10}{100} + \frac{V_B - V_D}{15} + \frac{V_B - 0}{10} = 0$$

$$\frac{V_B - 10}{20} + \frac{V_B - V_D}{3} + \frac{V_B}{2} = 0$$

$$3V_B - 30 + 20V_B - 20V_D + 30V_B = 0$$

$$53V_B - 20V_D = 30 \quad (1)$$

Similarly applying KCL for point D,

$$\frac{V_D - 10}{60} + \frac{V_D - V_B}{15} + \frac{V_D - 0}{5} = 0$$

$$V_D - 10 + 4V_D - 4V_B + 12V_D = 0$$

$$-4V_B + 17V_D = 10 \quad (2)$$

after solving equation (1) & (2)

$$V_D = 0.792 \text{ volt}$$

$$V_B = 0.865 \text{ volt}$$

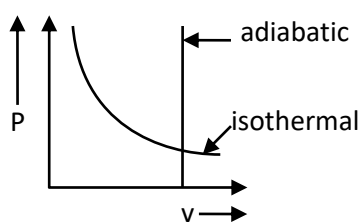
Then the current through the galvanometer

$$= \frac{V_B - V_D}{R}$$

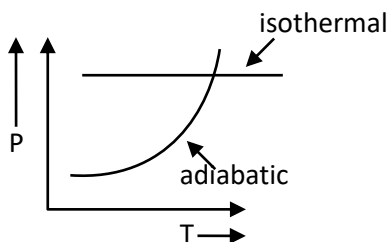
$$= \frac{0.865 - 0.792}{15}$$

$$= 4.67 \text{ mA}$$

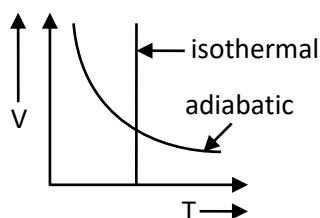
17. Which one is the correct option depicting the two different thermodynamic processes ?



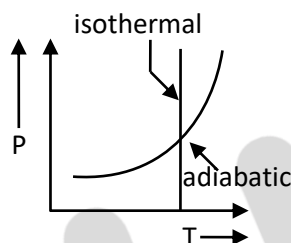
(a)



(b)



(c)



(d)

a. (c) and (d)

c. (a) only

b. (b) and (c)

d. (c) and (a)

Answer (a)

Sol.

Isothermal process means constant temperature which is only possible in graph (c) & (d)

for adiabatic process

$$pv^\gamma = \text{constant} \dots(1)$$

$$\because PV = nRT$$

$$p \propto \frac{T}{v}$$

$$\text{So } \frac{T}{v} v^\gamma = \text{constant}$$

$$Tv^{\gamma-1} = \text{constant} \dots(2)$$

Similarly,

$$v \propto \frac{T}{p}$$

$$P \left(\frac{T}{P}\right)^\gamma = \text{constant}$$

$$P^{1-\gamma} T^\gamma = \text{constant} \dots(3)$$

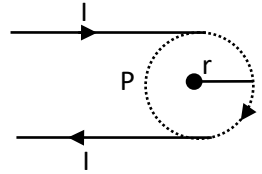
\because differentiating equation (3) w.r.to temp.

$$(P)^{1-\gamma} \gamma (T)^{\gamma-1} dT + (T)^\gamma (1-\gamma) (P)^{1-\gamma-1} dP = 0$$

$$\frac{dP}{dT} = -\left(\frac{\gamma}{1-\gamma}\right) \left(\frac{P}{T}\right)$$

$$\frac{dP}{dT} = \left(\frac{\gamma}{\gamma-1}\right)\left(\frac{P}{T}\right), \quad \text{It gives (+ve) slope.}$$

18. A hairpin like shape as shown in figure is made by bending a long current carrying wire. What is the magnitude of a magnetic field at point P which lies on the centre of the semicircle ?



- a. $\frac{\mu_0 I}{4\pi r} (2 - \pi)$ b. $\frac{\mu_0 I}{4\pi r} (2 + \pi)$
 c. $\frac{\mu_0 I}{2\pi r} (2 + \pi)$ d. $\frac{\mu_0 I}{2\pi r} (2 - \pi)$

Answer (b)

Sol.

Magnetic field due to each of the straight wire = $\frac{\mu_0 I}{4\pi r}$

Magnetic field due to semicircular arc = $\frac{\mu_0 I}{4r}$

Thus, total magnetic field at point P

$$B = \frac{\mu_0 I}{4\pi r} + \frac{\mu_0 I}{4\pi r} + \frac{\mu_0 I}{4r}$$

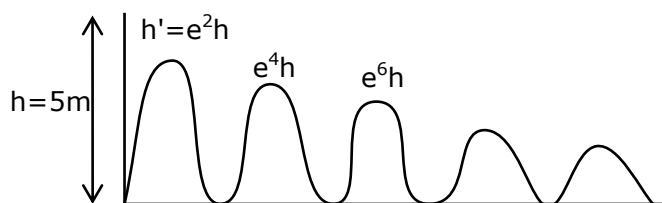
$$= \frac{\mu_0 I}{2\pi r} + \frac{\mu_0 I}{4r}$$

$$B = \frac{\mu_0 I}{4\pi r} (2 + \pi)$$

19. A rubber ball is released from a height of 5 m above the floor. It bounces back repeatedly, always rising to $\frac{81}{100}$ of the height through which it falls. Find the average speed of the ball. (Take $g = 10 \text{ ms}^{-2}$)
- a. 2.50 ms^{-1} b. 3.50 ms^{-1}
 c. 3.0 ms^{-1} d. 2.0 ms^{-1}

Answer (a)

Sol.



$$\text{Total distance } d = h + 2e^2 h + 2e^4 h + 2e^6 h + 2e^8 h + \dots$$

$$d = h + 2e^2 h (1 + e^2 + e^4 + e^6 + \dots)$$

$$d = h + 2e^2 h \left(\frac{1}{1 - e^2}\right)$$

$$d = \frac{(1-e^2)h + 2e^2h}{1-e^2} = \frac{h(1+e^2)}{1-e^2}$$

$$\text{Total time} = T + 2eT + 2e^2T + 2e^3T + \dots$$

$$\text{Total time} = T + 2eT(1+e+e^2+e^3+\dots)$$

$$= T + 2eT \left(\frac{1}{1-e} \right)$$

$$\text{Total time} = \frac{T(1+e)}{1-e}$$

Average speed of the ball

$$V_{\text{avg}} = \frac{h \frac{(1+e^2)}{(1-e^2)}}{T \frac{(1+e)}{(1-e)}}$$

$$= \frac{5}{1} \left(\frac{1+e^2}{(1+e)(1-e)} \frac{(1-e)}{(1+e)} \right)$$

$$V_{\text{avg}} = \frac{5(1+e^2)}{(1+e)^2}$$

$$\therefore h' = e^2h$$

$$\frac{81}{100} = e^2$$

$$e = \frac{9}{10} = 0.9$$

$$V_{\text{avg}} = \frac{5 \left(1 + \frac{81}{100} \right)}{(1+0.9)^2}$$

$$= 2.50 \text{ m/sec.}$$

20. What happens to the inductive reactance and the current in a purely inductive circuit if the frequency is halved ?

- a. Both, including reactance and current will be doubled
- c. Inductive reactance will be halved and current will be doubled

- b. Both, inductive reactance and current will be halved
- d. Inductive reactance will be doubled and current will be halved.

Answer (c)

Sol.

$$X_L = \omega L$$

$$\text{If frequency is halved, } X'_L = \left(\frac{X_L}{2} \right)$$

[inductive reactance is halved]

$$\therefore I = \frac{V}{X_L}$$

$$\& I' = \frac{2V}{X_L} = 2I \text{ [current will be doubled]}$$

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B

SECTION -B

1. The electric field intensity produced by the radiation coming from a 100 W bulb at a distance of 3 m is E . The electric field intensity produced by the radiation coming from 60 W at the same distance is $\sqrt{\frac{x}{5}}E$. Where the value of $x =$ _____

Answer (3)

Sol.

Intensity of electromagnetic radiation

$$I = \frac{1}{2} C \epsilon_0 E^2$$

where E is electric field intensity at a point

$$E^2 \propto I$$

$$I = \frac{\text{Power}}{\text{Area}}$$

$$E^2 \propto \frac{P}{A}$$

$$E \propto \sqrt{P}$$

[at the same distance, A will be the same]

$$\frac{E'}{E} = \sqrt{\frac{60}{100}}$$

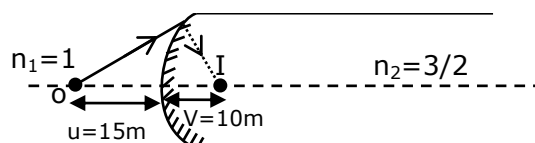
$$E' = \sqrt{\frac{3}{5}} E$$

So the value of $x = 3$

2. The image of an object placed in air formed by convex refracting surface is at a distance of 10 m behind the surface. The image is real and is at $\frac{2^{\text{nd}}}{3}$ of the distance of the object from the surface. The wavelength of light inside the surface is $\frac{2}{3}$ times the wavelength in air, The radius of the curved surface is $\frac{x}{13}$ m. The value of 'x' is _____

Answer: (30)

Sol.



$$\frac{n_2}{v} - \frac{n_1}{u} = \left(\frac{n_2 - n_1}{R} \right)$$

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Since wavelength of light inside the surface is $\frac{3}{2}$ times the wavelength in air, $n_2 =$

$$\frac{3}{2} \times n_1 = \frac{3}{2}$$

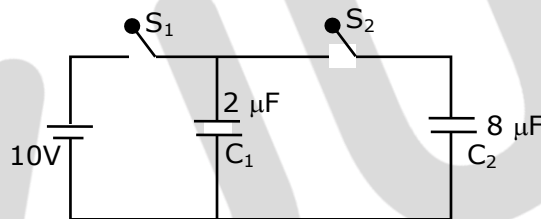
$$\frac{\frac{3}{2}}{10} - \frac{1}{(-15)} = \frac{(\frac{3}{2}-1)}{R}$$

$$\frac{3}{20} + \frac{1}{15} = \frac{1}{2R}$$

$$R = \frac{150}{65}$$

$$R = \frac{30}{13} m, \text{ Thus, the value of } x = 30$$

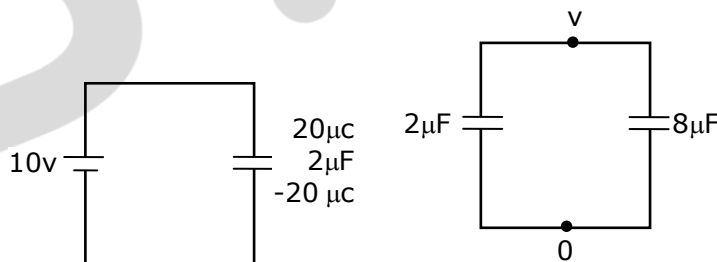
3. A $2\mu F$ capacitor C_1 is first charged to a potential difference of $10V$ using a battery. Then the battery is removed and the capacitor is connected to an uncharged capacitor C_2 of $8\mu F$. The charge in C_2 on equilibrium condition is _____ μC . (Round off to the Nearest Integer)



Answer (16)

Sol.

After capacitor C_1 is fully charged,



When battery is removed & the capacitor is connected

At equilibrium condition, let voltage across each capacitor be V .

Then, using conservation of charge

$$2V + 8V = 20$$

$$10V = 20$$

$$V = 2 \text{ volt}$$

$$Q = CV$$

$$Q = 8 \times 2 = 16\mu C$$

4. A particle of mass m moves in a circular orbit in a central potential field $U(r) = U_0 r^4$. If Bohr's quantization conditions are applied, radii of possible orbital r_n vary with $n^{\frac{1}{\alpha}}$, where α is ____

Answer (3)

Sol.

$$F \rightarrow = -\frac{du}{dr}$$

$$= -\frac{d}{dr}(U_0 r^4)$$

$$F \rightarrow = -4U_0 r^3$$

$$\therefore \frac{mv^2}{r} = 4U_0 r^3$$

$$mv^2 = 4U_0 r^4$$

$$\text{Then } v \propto r^2$$

$$\therefore mvr = \frac{nh}{2\pi}$$

$$\text{Thus, } r^3 \propto n$$

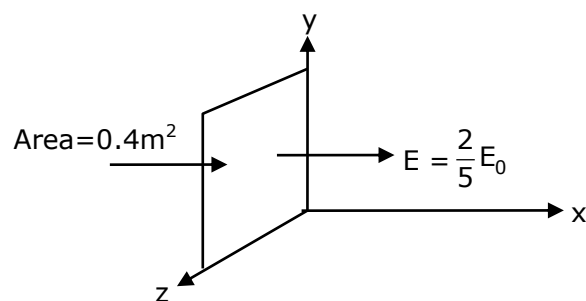
$$r \propto (n)^{\frac{1}{3}}$$

So the value of $\alpha = 3$

5. The electric field in a region is given by $E \rightarrow = \frac{2}{5}E_0 i \hat{+} + \frac{3}{5}E_0 j \hat{+}$ with $E_0 = 4.0 \times 10^3 \frac{N}{C}$. The flux of this field through a rectangular surface are 0.4 m^2 parallel to $Y-Z$ plane is ____ Nm^2C^{-1} .

Answer (640)

Sol.



From Gauss' law

$$\phi = \oint E \rightarrow \cdot dA \rightarrow$$

$$= \frac{2}{5}E_0 \times (0.4)$$

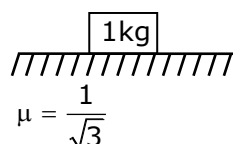
$$= \frac{2}{5} \times 4 \times 10^3 \times 0.4$$

$$\phi = 640 \text{ Nm}^2 \text{ c}^{-1}$$

6. A body of mass 1 kg rests on a horizontal floor with which it has a coefficient of static friction $\frac{1}{\sqrt{3}}$. It is desired to make the body move by applying the minimum possible force $F \text{ N}$. The value of F will be _____. (Round off to the Nearest Integer)
[Take $g = 10 \text{ ms}^{-2}$]

Answer (5)

Sol.



Minimum possible force \Rightarrow

$$F = \frac{\mu mg}{\sqrt{1+\mu^2}}$$

$$F_{\min} = \frac{\frac{1}{\sqrt{3}} \times 1 \times 10}{\sqrt{1+\frac{1}{3}}}$$

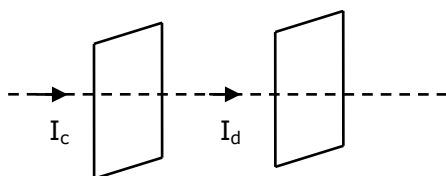
$$F_{\min} = 5 \text{ N}$$

7. Seawater at a frequency $f = 9 \times 10^2 \text{ Hz}$, has permittivity $\epsilon = 80\epsilon_0$ and resistivity $\rho = 0.25 \Omega \text{ m}$. Imagine a parallel plate capacitor is immersed in seawater and is driven by an alternating voltage source $V(t) = V_0 \sin(2\pi ft)$. Then the conduction current density becomes $10x$ times the displacement current density after time $t = \frac{1}{800}$. The value of x is _____.

(Given : $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}$)

Answer (6)

Sol.



Given:-

$$f = 9 \times 10^2 \text{ Hz}$$

$$\epsilon = \epsilon_0 \epsilon_r$$

$$\epsilon = 80 \epsilon_0$$

$$\text{So, } \epsilon_r = 80$$

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$$\rho = 0.25 \Omega m$$

$$V(t) = V_0 \sin(2\pi ft)$$

$$\text{Displacement current, } I_d = \frac{dq}{dt} = \frac{cdv}{dt}$$

$$I_d = \frac{\epsilon_0 \epsilon_r A}{d} \frac{d}{dt} (v_0 \sin(2\pi ft))$$

$$I_d = \frac{\epsilon_0 \epsilon_r A}{d} V_0 (2\pi f) \cos(2\pi ft) \dots\dots\dots(1)$$

Where d is the distance between plates & conduction current $I_c = \frac{V}{R}$

$$I_c = \frac{V_0 \sin(2\pi ft)}{\rho \frac{d}{A}} = \frac{Av_0 \sin(2\pi ft)}{\rho d} \dots\dots(2)$$

Divide equation (1) and (2)

$$\frac{I_d}{I_c} = \epsilon_0 \epsilon_r 2\pi f(\rho) \cot(2\pi ft)$$

$$\frac{I_d}{I_c} = \frac{1}{4\pi \times 9 \times 10^9} \times 80 \times 2\pi \times 9 \times 10^2 \times (0.25) \times \cot\left(2\pi \times 9 \times 10^2 \times \frac{1}{800}\right)$$

$$= \frac{10^3}{10^9} \left(\cot\left(\frac{9\pi}{4}\right)\right)$$

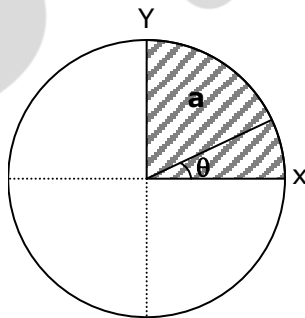
$$= \frac{10^3}{10^9}$$

$$\frac{I_d}{I_c} = \frac{1}{10^6}$$

$$I_c = 10^6 I_d$$

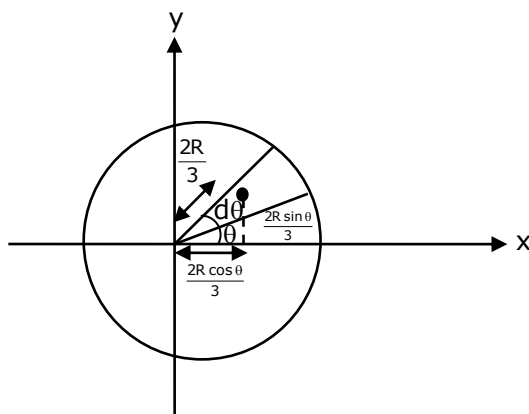
$$\text{So } x = 6$$

8. The disc of mass M with uniform surface mass density σ is shown in the figure. The centre of mass of the quarter disc (the shaded area) is at the position $\frac{xR}{3\pi}, \frac{xR}{3\pi}$. x is ____ (Round off to the Nearest Integer)
[a is an area as shown in the figure]



Answer (4)

Sol.



Each segment of disc subtending angle $d\theta$ can be considered as a triangle of height R and base $Rd\theta$

Mass of a segment of disc subtending angle $d\theta$

$$dm = \sigma \frac{1}{2} R \times Rd\theta$$

$$dm = \frac{\sigma R^2 d\theta}{2}$$

Therefore, x coordinate of COM of quarter disc

$$x_{cm} = \frac{\int x dm}{\int dm} = \frac{\int_0^{\pi/2} \frac{\sigma R^2}{2} d\theta \left(\frac{2R}{3} \cos\theta\right)}{\int_0^{\pi/2} \frac{\sigma R^2}{2} d\theta}$$

Here, x is the x -coordinate of COM of dm mass. And for a triangular section its COM is at cross section of median which will be at a distance $2R/3$ from vertex.

That's why they have taken x -coordinate as $\frac{2R}{3} \cos\theta$

$$= \frac{2R}{3} \frac{\int_0^{\pi/2} \cos\theta d\theta}{\int_0^{\pi/2} d\theta}$$

$$= \frac{2R}{3} \left(\frac{2}{\pi}\right)$$

$$= \frac{4R}{3\pi}$$

So the value of $x = \frac{4R}{3\pi}$

9. Suppose you have taken a dilute solution of oleic acid in such a way that its concentration becomes 0.01 cm^3 of oleic acid per cm^3 of the solution. Then you make a thin film of this solution (monomolecular thickness) of area 4 cm^2 by considering 100 spherical drops of radius $\left(\frac{3}{40\pi}\right)^{\frac{1}{3}} \times 10^{-3} \text{ cm}$. Then the thickness of oleic acid layer will be $x \times 10^{-14} \text{ m}$ where x is _____.

Answer (25)

Sol.

Volume of film = Area of film \times thickness

Also, we know : Volume of film = Volume of 100 spherical drops

$$4t_T = 100 \times \frac{4}{3} \pi r^3$$

$$= 100 \times \frac{4\pi}{3} \times \frac{3}{40\pi} \times 10^{-9}$$

$$= 10^{-8} \text{ cm}^3$$

Hence, thickness of film

$$t_T = 25 \times 10^{-10} \text{ cm}$$

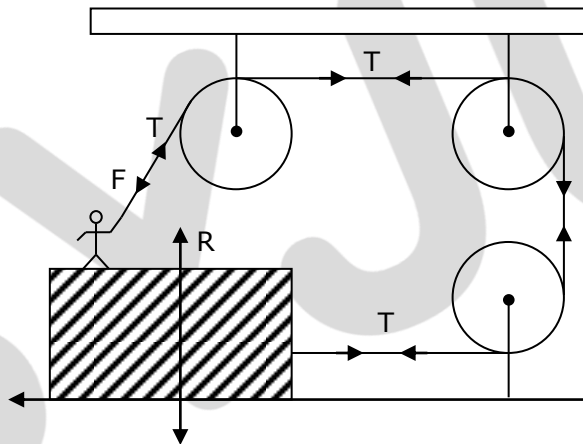
$$= 25 \times 10^{-12} \text{ m}$$

& Thickness of oleic acid layer

$$t_0 = 0.01 t_T = 25 \times 10^{-14} \text{ m}$$

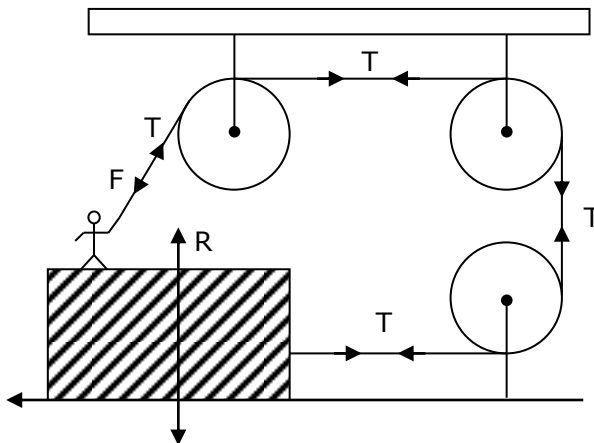
So, $x = 25$

10. A boy of mass 4 kg is standing on a piece of wood having mass 5 kg . If the coefficient of friction between the wood and the floor is 0.5 , the maximum force that the boy can exert on the rope so that the piece of wood does not move from its place is _____ N . (Round off to the Nearest Integer)
[Take $g = 10 \text{ ms}^{-2}$]

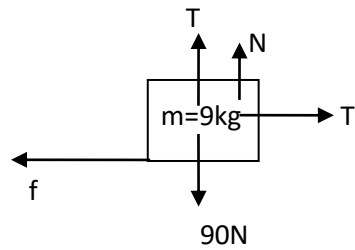


Answer (30)

Sol.



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[R is the reaction force between man and block while

N from ground to block]

From FBD of [man + wooden block] system

$$\therefore f = T \text{ [horizontal direction]}$$

$$\mu N = T$$

$$\mu(90 - T) = T$$

[Because $T + N = 90$ (in vertical direction)]

$$0.5(90 - T) = T$$

$$90 - T = 2T$$

$$3T = 90 \Rightarrow T = 30 \text{ N}$$