

Instructions:

- All the questions are compulsory.
- The question paper consists of 16 questions divided into 4 sections A,B,C and D.
- Section A comprises of 3 questions :
 - Q.No.1 consists of 16 Multiple Choice Questions carrying 1 mark each.
 - Q.No.2 consists of 8 Fill in the Blank type questions with options carrying 1 mark each.
 - Q.No.3 consists of 8 True/False type questions carrying 1 mark each.
- Section B comprises of 5 questions of 2 marks each.
- Section C comprises of 5 questions of 4 marks each.
- Section D comprises of 3 questions of 6 marks each.
- There is no overall choice. However, an internal choice has been provided in three questions of 2 marks, three questions of 4 marks and three questions of 6 marks each. You have to attempt only one of the alternatives in all such questions.
- Use of calculator is not permitted.

Section – A

Q1 Choose the correct options in the following questions :

- (i) Function $f: R \rightarrow R$, $f(x) = 3x - 5$ is :
 (a) one-one only (b) onto only (c) one-one and onto (d) none of these 1
- (ii) Relation given by $R = \{(1, 1), (2, 2), (1, 2), (2, 1)\}$ is
 (a) reflexive only (b) symmetric only (c) transitive only (d) equivalence relation 1
- (iii) $\cos^{-1}(-\cos \frac{2\pi}{3})$ is equal to :
 (a) $\frac{\pi}{5}$ (b) $\frac{2\pi}{3}$ (c) $\frac{\pi}{2}$ (d) $\frac{\pi}{3}$ 1
- (iv) If $\begin{bmatrix} 1 & -x \\ 4 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 8 \\ 4 & -3 \end{bmatrix}$ then value of x is:
 (a) 8 (b) -4 (c) 3 (d) -8 1
- (v) If order of matrix A is 2×3 and order of matrix B is 3×5 then order of matrix $B'A'$ is :
 (a) 5×2 (b) 2×5 (c) 5×3 (d) 3×2 1
- (vi) If $f(x) = \begin{cases} kx + 1, & x \leq 5 \\ 3x - 5, & x > 5 \end{cases}$ is continuous then value of k is :
 (a) $\frac{9}{5}$ (b) $\frac{5}{9}$ (c) $\frac{5}{3}$ (d) $\frac{3}{5}$ 1
- (vii) $\frac{d}{dx} \{\tan^{-1}(e^x)\}$ is equal to :
 (a) $e^x \tan^{-1} e^x$ (b) $\frac{e^x}{1+e^{2x}}$ (c) 0 (d) $e^x \sec^{-1} x$ 1
- (viii) Slope of tangent to the curve $y = x^2 - 2x + 1$ at $x = 3$ is:
 (a) 4 (b) 6 (c) 0 (d) 2 1
- (ix) $\int 3x^2 dx$ is equal to :
 (a) $x + c$ (b) $x^2 + c$ (c) $x^3 + c$ (d) $x^4 + c$ 1
- (x) $\int_0^{\pi/2} \frac{\sin^{1/2} x}{\sin^{1/2} x + \cos^{1/2} x} dx$ is equal to :
 (a) 0 (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{3}$ (d) $\frac{\pi}{4}$ 1
- (xi) Degree of differential equation $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 3y = 0$ is :
 (a) 3 (b) 2 (c) 1 (d) 0 1
- (xii) If $\vec{a} \cdot \vec{b} = |\vec{a} \times \vec{b}|$ then angle between vector \vec{a} and vector \vec{b} is :
 (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{6}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{3}$ 1
- (xiii) If $\vec{a} \cdot \vec{b} = 0$ then angle between vectors \vec{a} and \vec{b} is :
 (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{6}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{3}$ 1
- (xiv) Direction ratios of line given by $\frac{x-1}{3} = \frac{2y+6}{12} = \frac{1-z}{-7}$ are :
 (a) $\langle 3, 12, -7 \rangle$ (b) $\langle 3, -6, 7 \rangle$ (c) $\langle 3, 6, 7 \rangle$ (d) $\langle 3, 6, -7 \rangle$ 1

- (xv) Maximum value of $Z = 3x + y$ for the constraints $x + y \leq 4, x \geq 0, y \geq 0$ is: 1
 (a)12 (b)16 (c)4 (d)10
- (xvi) If $P(A) = \frac{1}{2}, P(B) = \frac{3}{8}$ and $P(A \cap B) = \frac{1}{5}$ then $P(A|B)$ is equal to : 1
 (a) $\frac{2}{5}$ (b) $\frac{8}{15}$ (c) $\frac{2}{3}$ (d) $\frac{5}{8}$

Q2 Fill in the blanks from the given options

0, 1, $\langle 3, -1, 2 \rangle$, $\frac{\pi}{2}$, 6, 2, 5, 4, $-\sin x$, $\tan x$

- (i) Value of $\sin^{-1}(1)$ is _____ 1
- (ii) If $A = [a_{ij}]_{2 \times 3}$ such that $a_{ij} = i + j$ then $a_{11} =$ _____ 1
- (iii) If $\begin{vmatrix} x & 0 \\ 7 & 1 \end{vmatrix} = \begin{vmatrix} 3 & 0 \\ 7 & 2 \end{vmatrix}$ then $x =$ _____ 1
- (iv) If $y = \cos x$ then at $x = 0, \frac{dy}{dx} =$ _____ 1
- (v) $\int_0^5 dx =$ _____ 1
- (vi) Order of the differential equation $\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^3 + y = 0$ is _____ 1
- (vii) Direction ratios of a line which is perpendicular to the plane $3x - y + 2z = 9$ are _____ 1
- (viii) Probability of occurrence of impossible event = _____ 1

Q3 State true or false for the following statements :

- (i) If A is a square matrix then $(A + A')$ is a skew-symmetric matrix. 1
- (ii) If $y = 10x$ then $\frac{dy}{dx} = 0$. 1
- (iii) If $y = \tan x$ then $\frac{dy}{dx} = \sec^2 x$ 1
- (iv) $\int dx = x^2 + c$ 1
- (v) $xdy - ydx = 0$ is a variable separable type of differential equation. 1
- (vi) Scalar product of two perpendicular vectors is zero. 1
- (vii) Point $(3, -4, 2)$ lies in the plane $2x + y - z = 0$ 1
- (viii) If $P(E) = 0.4$ then $P(\text{not } E) = 0.6$ 1

Section – B

- Q4 If $A = \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix}$ and $f(x) = x^2 + 2x + 3$ then find $f(A)$. 2
- Q5 Find the interval in which function $f(x) = x^2 + 2x - 7$ is increasing. 2
 OR
 Find the slope of the normal to the curve $y = x^3 - x + 1$ at the point whose x -coordinate is 2. 2
- Q6 Evaluate $\int e^x \left(\log x + \frac{1}{x} \right) dx$. 2
 OR
 Evaluate $\int x \sin x dx$ 2
- Q7 Using integration find the area bounded by the parabola $y^2 = 4x$ straight lines $x = 1, x = 4$ in the first quadrant. 2
- Q8 Find the unit vector in the direction of diagonal of the parallelogram whose sides are given by the vectors $\vec{a} = 2\hat{i} - \hat{j} - 3\hat{k}, \vec{b} = 5\hat{i} + 2\hat{j} - \hat{k}$ 2
 OR
 If $\vec{a} = 2\hat{i} + 3\hat{j} - 5\hat{k}, \vec{b} = 7\hat{i} - 2\hat{j} - 4\hat{k}$ then find $\vec{a} \times \vec{b}$. 2

Section – C

- Q9 Find the value of: $2 \tan^{-1}(1) - \cos^{-1}\left(\frac{-1}{2}\right) + 3 \sin^{-1}\left(\frac{1}{\sqrt{2}}\right) + 2 \sec^{-1}\left(\frac{2}{\sqrt{3}}\right)$ 4

- Q10** If $y = x^{\sin x} + (\sin x)^x$ then find $\frac{dy}{dx}$. 4
- OR
- If $y = (\tan^{-1} x)^2$, show that $(x^2 + 1)^2 y_2 + 2x(x^2 + 1)y_1 = 2$ 4
- Q11** Evaluate $\int \frac{dx}{(x-1)(x-2)(x-3)}$. 4
- OR
- Evaluate $\int \frac{\sec^2 x}{\tan^2 x - 4 \tan x + 7} dx$ 4
- Q12** Find the general solution of the differential equation $x^2 dy - (x^2 + xy + y^2) dx = 0$. 4
- OR
- Find the general solution of the differential equation $\sec^2 x \tan y dx - \sec^2 y \tan x dy = 0$. 4
- Q13** Bag I contains 3 red and 4 white balls. Bag II contains 7 red and 5 white balls. A bag is selected at random and a ball is drawn from it, which is found to be red. Find the probability that ball is drawn from bag II.

Section – D

- Q14** Solve the following system of linear equations by matrix method : 6
- $$2x + 3y - 5z = 13 \quad , \quad x - y + z = -2 \quad , \quad 3x + 2y - z = 8$$
- OR
- Express $A = \begin{bmatrix} 2 & 3 & 5 \\ 0 & 2 & 9 \\ 3 & 2 & 8 \end{bmatrix}$ as the sum of a symmetric matrix and a skew-symmetric matrix. 6
- Q15** Find the shortest distance between the lines 6
- $$\vec{r} = 6i - j + 3k + \lambda(i + 3j + 2k) \quad \text{and} \quad \vec{r} = 9i + j - 4k + \mu(i - 2j + k)$$
- OR
- Find the foot of perpendicular drawn from the point $(2, -3, 5)$ on the plane $3x + 4y - 2z = 20$ 6
- Q16** Solve the following linear programming problem graphically: 6
- Maximize and minimize $Z = 4x + 3y$ subject to the constraints
- $$x + y \leq 8, \quad 4x + y \geq 8, \quad x - y \geq 0, \quad x \geq 0, \quad y \geq 0$$
- OR
- Solve the following linear programming problem graphically: 6
- Maximize and minimize $Z = 5x + 2y - 2$ subject to the constraints
- $$x + y \leq 10, \quad x + y \geq 3, \quad x \leq 8, \quad y \leq 8, \quad x \geq 0, \quad y \geq 0$$