Graduate Aptitude Test in Engineering 2017

Question Paper Name: Mathematics 5th Feb 2017

Subject Name: Mathematics

Duration: 180 **Total Marks:** 100



Organizing Institute: Indian Institute of Technology Roorkee

















Correct: 1 Wrong: 0

Correct: 1 Wrong: 0

Consider the vector space $V = \{a_0 + a_1x + a_2x^2 : a_i \in \mathbb{R} \text{ for } i = 0,1,2\}$ of polynomials of degree at most 2. Let $f: V \to \mathbb{R}$ be a linear functional such that f(1+x) = 0, $f(1-x^2) = 0$ and $f(x^2-x)=2$. Then $f(1+x+x^2)$ equals _____.

Question Number: 2

Let A be a 7×7 matrix such that $2A^2 - A^4 = I$, where I is the identity matrix. If A has two distinct eigenvalues and each eigenvalue has geometric multiplicity 3, then the total number of nonzero entries in the Jordan canonical form of A equals ______.

Question Number: 3

Correct: 1 Wrong: -0.33

Let $f(z) = (x^2 + y^2) + i 2xy$ and $g(z) = 2xy + i(y^2 - x^2)$ for $z = x + i y \in \mathbb{C}$. Then, in the complex plane \mathbb{C} ,

- (A) f is analytic and g is NOT analytic
- (B) f is NOT analytic and g is analytic
- (C) neither f nor g is analytic
- (D) both f and g are analytic

Question Number: 4

Correct: 1 Wrong: 0

If $\sum_{n=-\infty}^{\infty} a_n (z-2)^n$ is the Laurent series of the function $f(z) = \frac{z^4 + z^3 + z^2}{\left(z-2\right)^3}$ for $z \in \mathbb{C} \setminus \{2\}$, then a_{-2} equals ______.

Let $f_n: [0,1] \to \mathbb{R}$ be given by $f_n(x) = \frac{2x^2}{x^2 + (1-2nx)^2}$, $n = 1, 2, \ldots$. Then the sequence (f_n)

- (A) converges uniformly on [0,1]
- (B) does NOT converge uniformly on [0,1] but has a subsequence that converges uniformly on [0,1]
- (C) does NOT converge pointwise on [0,1]
- (D) converges pointwise on [0,1] but does NOT have a subsequence that converges uniformly on [0,1]

Question Number: 6

Let $C: x^2 + y^2 = 9$ be the circle in \mathbb{R}^2 oriented positively. Then

$$\frac{1}{\pi} \oint_C \left(3y - e^{\cos x^2}\right) dx + \left(7x + \sqrt{y^4 + 11}\right) dy \quad \text{equals}$$

Question Number: 7

Correct: 1 Wrong: -0.33

Correct: 1 Wrong: 0

Consider the following statements:

- (P): There exists an unbounded subset of $\mathbb R$ whose Lebesgue measure is equal to 5.
- (Q): If $f: \mathbb{R} \to \mathbb{R}$ is continuous and $g: \mathbb{R} \to \mathbb{R}$ is such that f = g almost everywhere on \mathbb{R} , then g must be continuous almost everywhere on \mathbb{R} .

Which of the above statements hold TRUE?

(A) Both P and Q

(B) Only P

(C) Only Q

(D) Neither P nor Q

Question Number: 8

Correct: 1 Wrong: -0.33

If x^3y^2 is an integrating factor of $(6y^2 + axy)dx + (6xy + bx^2)dy = 0$, where $a, b \in \mathbb{R}$, then

(A)
$$3a - 5b = 0$$

(B)
$$2a-b=0$$

(C)
$$3a+5b=0$$

(D)
$$2a+b=0$$

Correct: 1 Wrong: 0

If x(t) and y(t) are the solutions of the system $\frac{dx}{dt} = y$ and $\frac{dy}{dt} = -x$ with the initial conditions x(0) = 1 and y(0) = 1, then $x(\pi/2) + y(\pi/2)$ equals _____.

Question Number: 10

Correct : 1 Wrong : -0.33

If $y=3e^{2x}+e^{-2x}-\alpha x$ is the solution of the initial value problem

$$\frac{d^2y}{dx^2} + \beta y = 4\alpha x, \ y(0) = 4 \text{ and } \frac{dy}{dx}(0) = 1, \text{ where } \alpha, \beta \in \mathbb{R},$$

then

(A)
$$\alpha = 3$$
 and $\beta = 4$

(B)
$$\alpha = 1$$
 and $\beta = 2$

(C)
$$\alpha = 3$$
 and $\beta = -4$

(D)
$$\alpha = 1$$
 and $\beta = -2$

Question Number: 11

Correct: 1 Wrong: 0

Let G be a non-abelian group of order 125. Then the total number of elements in $Z(G) = \{x \in G : g \mid x = x \mid g \text{ for all } g \in G\}$ equals _____.

Question Number: 12

Correct: 1 Wrong: 0

Let F_1 and F_2 be subfields of a finite field F consisting of 2^9 and 2^6 elements, respectively. Then the total number of elements in $F_1 \cap F_2$ equals _____.

Correct: 1 Wrong: 0

Consider the normed linear space \mathbb{R}^2 equipped with the norm given by ||(x,y)|| = |x| + |y| and the subspace $X = \{(x, y) \in \mathbb{R}^2 : x = y\}$. Let f be the linear functional on X given by f(x,y) = 3x. If $g(x,y) = \alpha x + \beta y$, α , $\beta \in \mathbb{R}$, is a Hahn-Banach extension of f on \mathbb{R}^2 , then $\alpha - \beta$ equals _____.

Question Number: 14

Correct: 1 Wrong: -0.33

For
$$n \in \mathbb{Z}$$
, define $c_n = \frac{1}{\sqrt{2\pi}} \int_{-\pi}^{\pi} e^{i(n-i)x} dx$, where $i^2 = -1$. Then $\sum_{n \in \mathbb{Z}} |c_n|^2$ equals

(A) $\cosh(\pi)$

- (B) $sinh(\pi)$
- (C) $\cosh(2\pi)$ (D) $\sinh(2\pi)$

Question Number: 15

Correct: 1 Wrong: 0

If the fourth order divided difference of $f(x) = \alpha x^4 + 5x^3 + 3x + 2$, $\alpha \in \mathbb{R}$, at the points 0.1, 0.2, 0.3, 0.4, 0.5 is 5, then α equals _____.

Question Number: 16

Correct: 1 Wrong: 0

If the quadrature rule $\int_{1}^{2} f(x) dx \approx c_1 f(0) + 3 f(c_2)$, where $c_1, c_2 \in \mathbb{R}$, is exact for all polynomials of degree ≤ 1 , then $c_1 + 3c_2$ equals _____.

Correct : 1 Wrong : -0.33

If u(x, y) = 1 + x + y + f(xy), where $f: \mathbb{R}^2 \to \mathbb{R}$ is a differentiable function, then u satisfies

(A)
$$x \frac{\partial u}{\partial x} - y \frac{\partial u}{\partial y} = x^2 - y^2$$

(B)
$$x \frac{\partial u}{\partial x} - y \frac{\partial u}{\partial y} = 0$$

(C)
$$x \frac{\partial u}{\partial x} - y \frac{\partial u}{\partial y} = x - y$$

(D)
$$y \frac{\partial u}{\partial x} - x \frac{\partial u}{\partial y} = x - y$$

Question Number: 18

Correct : 1 Wrong : -0.33

The partial differential equation $x \frac{\partial^2 u}{\partial x^2} + (x - y) \frac{\partial^2 u}{\partial x \partial y} - y \frac{\partial^2 u}{\partial y^2} + \frac{1}{4} \left(\frac{\partial u}{\partial y} - \frac{\partial u}{\partial x} \right) = 0$ is

- (A) hyperbolic along the line x+y=0
- (B) elliptic along the line x-y=0
- (C) elliptic along the line x+y=0
- (D) parabolic along the line x+y=0

Question Number: 19

Correct: 1 Wrong: -0.33

Let X and Y be topological spaces and let $f: X \to Y$ be a continuous surjective function. Which one of the following statements is TRUE?

- (A) If X is separable, then Y is separable
- (B) If X is first countable, then Y is first countable
- (C) If X is Hausdorff, then Y is Hausdorff
- (D) If X is regular, then Y is regular

Question Number: 20

Correct : 1 Wrong : -0.33

Consider the topology $T = \{U \subseteq \mathbb{Z} : \mathbb{Z} \setminus U \text{ is finite} \text{ or } 0 \notin U\}$ on \mathbb{Z} . Then, the topological space $(\mathbb{Z}, \mathcal{T})$ is

- (A) compact but NOT connected
- (B) connected but NOT compact
- (C) both compact and connected

(D) neither compact nor connected

Let F(x) be the distribution function of a random variable X. Consider the functions:

$$G_1(x) = (F(x))^3, x \in \mathbb{R}$$

$$G_2(x) = 1 - (1 - F(x))^5, x \in \mathbb{R}$$
.

Which of the above functions are distribution functions?

(A) Neither G_1 nor G_2

(B) Only G₁

(C) Only G₂

(D) Both G_1 and G_2

Question Number: 22

Correct: 1 Wrong: -0.33

Let X_1, X_2, \ldots, X_n $(n \ge 2)$ be independent and identically distributed random variables with finite variance σ^2 and let $\overline{X} = \frac{1}{n} \sum_{i=1}^n X_i$. Then the covariance between \overline{X} and $X_1 - \overline{X}$ is

(A) 0

- (B) $-\sigma^2$
- (C) $\frac{-\sigma^2}{n}$
- (D) $\frac{\sigma^2}{n}$

Question Number: 23

Correct: 1 Wrong: 0

Let $X_1, X_2, ..., X_n$ ($n \ge 2$) be a random sample from a $N(\mu, \sigma^2)$ population, where $\sigma^2 = 144$. The smallest n such that the length of the shortest 95% confidence interval for μ will not exceed 10 is _____.

Consider the linear programming problem (LPP):

Maximize
$$4x_1 + 6x_2$$

Subject to
$$x_1 + x_2 \le 8$$
,

$$2x_1 + 3x_2 \ge 18$$
,

$$x_1 \ge 6$$
, x_2 is unrestricted in sign.

Then the LPP has

- (A) no optimal solution
- (B) only one basic feasible solution and that is optimal
- (C) more than one basic feasible solution and a unique optimal solution
- (D) infinitely many optimal solutions





For a linear programming problem (LPP) and its dual, which one of the following is NOT TRUE?

- (A) The dual of the dual is primal
- (B) If the primal LPP has an unbounded objective function, then the dual LPP is infeasible
- (C) If the primal LPP is infeasible, then the dual LPP must have unbounded objective function
- (D) If the primal LPP has a finite optimal solution, then the dual LPP also has a finite optimal solution

Question Number: 26 Correct: 2 Wrong: 0

If U and V are the null spaces of $\begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}$ and $\begin{bmatrix} 1 & 2 & 3 & 2 \\ 0 & 1 & 2 & 1 \end{bmatrix}$, respectively, then the dimension of the subspace U+V equals ______.

Given two $n \times n$ matrices A and B with entries in \mathbb{C} , consider the following statements:

- (P): If A and B have the same minimal polynomial, then A is similar to B.
- (Q): If A has n distinct eigenvalues, then there exists $u \in \mathbb{C}^n$ such that $u, Au, ..., A^{n-1}u$ are linearly independent.

Which of the above statements hold TRUE?

(A) Both P and Q

(B) Only P

(C) Only Q

(D) Neither P nor Q

Question Number: 28

Correct: 2 Wrong: 0

Let $A = (a_{ij})$ be a 10×10 matrix such that $a_{ij} = 1$ for $i \neq j$ and $a_{ii} = \alpha + 1$, where $\alpha > 0$. Let λ and μ be the largest and the smallest eigenvalues of A, respectively. If $\lambda + \mu = 24$, then α equals ______.

Question Number: 29

Correct: 2 Wrong: 0

Let C be the simple, positively oriented circle of radius 2 centered at the origin in the complex plane. Then

$$\frac{2}{\pi i} \int_{C} \left(z e^{(1/z)} + \tan\left(\frac{z}{2}\right) + \frac{1}{(z-1)(z-3)^2} \right) dz \quad \text{equals} \underline{\qquad}.$$

Correct : 2 Wrong : -0.66

Let $\operatorname{Re}(z)$ and $\operatorname{Im}(z)$, respectively, denote the real part and the imaginary part of a complex number z. Let $T:\mathbb{C}\cup\{\infty\}\to\mathbb{C}\cup\{\infty\}$ be the bilinear transformation such that T(6)=0, T(3-3i)=i and $T(0)=\infty$. Then, the image of $D=\{z\in\mathbb{C}:|z-3|<3\}$ under the mapping w=T(z) is

(A) $\{w \in \mathbb{C} : \operatorname{Im}(w) < 0\}$

(B) $\{w \in \mathbb{C} : \operatorname{Re}(w) < 0\}$

(C) $\{w \in \mathbb{C} : \operatorname{Im}(w) > 0\}$

(D) $\{w \in \mathbb{C} : \operatorname{Re}(w) > 0\}$

Question Number: 31

Correct: 2 Wrong: -0.66

Let (x_n) and (y_n) be two sequences in a complete metric space (X,d) such that $d(x_n,x_{n+1}) \leq \frac{1}{n^2}$ and $d(y_n,y_{n+1}) \leq \frac{1}{n}$ for all $n \in \mathbb{N}$. Then

- (A) both (x_n) and (y_n) converge
- (B) (x_n) converges but (y_n) need NOT converge
- (C) (y_n) converges but (x_n) need NOT converge
- (D) neither (x_n) nor (y_n) converges

Question Number: 32

Correct: 2 Wrong: 0

Let $f:[0,1] \to \mathbb{R}$ be given by f(x) = 0 if x is rational, and if x is irrational then $f(x) = 9^n$, where n is the number of zeroes immediately after the decimal point in the decimal representation of x. Then the Lebesgue integral $\int_0^1 f(x) \, dx$ equals ______.

Let
$$f: \mathbb{R}^2 \to \mathbb{R}$$
 be defined by $f(x, y) = \begin{cases} \sin\left(\frac{y^2}{x}\right) \sqrt{x^2 + y^2}, & x \neq 0, \\ 0, & x = 0. \end{cases}$

Then, at (0,0),

- (A) f is continuous and the directional derivative of f does NOT exist in some direction
- (B) f is NOT continuous and the directional derivatives of f exist in all directions
- (C) f is NOT differentiable and the directional derivatives of f exist in all directions
- (D) f is differentiable

Question Number: 34

Correct: 2 Wrong: 0

Let D be the region in \mathbb{R}^2 bounded by the parabola $y^2 = 2x$ and the line y = x. Then $\iint_D 3xy \ dx \ dy \text{ equals } \underline{\hspace{1cm}}$.

Question Number: 35

Correct : 2 Wrong : -0.66

Let $y_1(x) = x^3$ and $y_2(x) = x^2 |x|$ for $x \in \mathbb{R}$.

Consider the following statements:

- (P): $y_1(x)$ and $y_2(x)$ are linearly independent solutions of $x^2 \frac{d^2y}{dx^2} 4x \frac{dy}{dx} + 6y = 0$ on \mathbb{R} .
- (Q): The Wronskian $y_1(x) \frac{dy_2}{dx}(x) y_2(x) \frac{dy_1}{dx}(x) = 0$ for all $x \in \mathbb{R}$.

Which of the above statements hold TRUE?

(A) Both P and Q

(B) Only P

(C) Only Q

(D) Neither P nor Q

Correct: 2 Wrong: 0

Let α and β with $\alpha > \beta$ be the roots of the indicial equation of

$$(x^2-1)^2 \frac{d^2y}{dx^2} + (x+1)\frac{dy}{dx} - y = 0$$
 at $x = -1$. Then $\alpha - 4\beta$ equals _____.

Question Number: 37

Correct: 2 Wrong: 0

Let S_9 be the group of all permutations of the set $\{1, 2, 3, 4, 5, 6, 7, 8, 9\}$. Then the total number of elements of S_9 that commute with $\tau = (1\ 2\ 3)(4\ 5\ 6\ 7)$ in S_9 equals ______.

Question Number: 38

Correct: 2 Wrong: 0

Let $\mathbb{Q}[x]$ be the ring of polynomials over \mathbb{Q} . Then the total number of maximal ideals in the quotient ring $\mathbb{Q}[x]/(x^4-1)$ equals _____.

Question Number: 39

Correct: 2 Wrong: -0.66

Let $\{e_n : n \in \mathbb{N}\}$ be an orthonormal basis of a Hilbert space H. Let $T : H \to H$ be given by $Tx = \sum_{n=1}^{\infty} \frac{1}{n} \langle x, e_n \rangle e_n$. For each $n \in \mathbb{N}$, define $T_n : H \to H$ by $T_n x = \sum_{j=1}^n \frac{1}{j} \langle x, e_j \rangle e_j$.

Then

(A)
$$||T_n - T|| \to 0$$
 as $n \to \infty$

(B)
$$||T_n - T|| \to 0$$
 as $n \to \infty$ but for each $x \in H$, $||T_n x - Tx|| \to 0$ as $n \to \infty$

(C) for each
$$x \in H$$
, $||T_n x - Tx|| \to 0$ as $n \to \infty$ but the sequence $(||T_n||)$ is unbounded

(D) there exist
$$x, y \in H$$
 such that $\langle T_n x, y \rangle \longrightarrow \langle Tx, y \rangle$ as $n \to \infty$

Consider the subspace $V = \{(x_n) \in \ell^2 : \sum_{n=1}^{\infty} |x_n| < \infty \}$ of the Hilbert space ℓ^2 of all square

summable real sequences. For $n \in \mathbb{N}$, define $T_n : V \to \mathbb{R}$ by $T_n((x_k)) = \sum_{i=1}^n x_i$.

Consider the following statements:

- (P): $\{T_n : n \in \mathbb{N}\}$ is pointwise bounded on V.
- (Q): $\{T_n : n \in \mathbb{N}\}\$ is uniformly bounded on $\{x \in V : ||x||_2 = 1\}$.

Which of the above statements hold TRUE?

- (A) Both P and Q
- (C) Only Q

- (B) Only P
- (D) Neither P nor Q

Question Number: 41

Let p(x) be the polynomial of degree at most 2 that interpolates the data (-1,2), (0,1) and (1,2). If q(x) is a polynomial of degree at most 3 such that p(x)+q(x) interpolates the data

Question Number: 42

Correct : 2 Wrong : -0.66

Correct: 2 Wrong: 0

Let J be the Jacobi iteration matrix of the linear system $\begin{bmatrix} 1 & 2 & 1 & x \\ 2 & 1 & 2 & y \\ -4 & 2 & 1 & z \end{bmatrix} = \begin{bmatrix} 1 & 2 & 1 & x \\ 2 & 1 & 2 & y \\ 3 & 1 & 2 & 3 \end{bmatrix}$.

Consider the following statements:

- (P): One of the eigenvalues of J lies in the interval [2, 3].
- (Q): The Jacobi iteration converges for the above system.

(-1,2), (0,1), (1,2) and (2,11), then q(3) equals _____.

Which of the above statements hold TRUE?

(A) Both P and Q

(B) Only P

(C) Only Q

(D) Neither P nor Q

Let u(x, y) be the solution of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 4u$ satisfying the condition u(x, y) = 1 on the circle $x^2 + y^2 = 1$. Then u(2, 2) equals ______.

Question Number: 44

Correct: 2 Wrong: -0.66

Let $u(r,\theta)$ be the bounded solution of the following boundary value problem in polar coordinates:

$$r^{2} \frac{\partial^{2} u}{\partial r^{2}} + r \frac{\partial u}{\partial r} + \frac{\partial^{2} u}{\partial \theta^{2}} = 0, \quad 0 < r < 2 \quad \text{and} \quad 0 \le \theta \le 2\pi,$$
$$u(2, \theta) = \cos^{2} \theta, \quad 0 \le \theta \le 2\pi.$$

Then $u(1, \pi/2) + u(1, \pi/4)$ equals

(A) 1

(B) $\frac{9}{8}$

- (C) $\frac{7}{8}$
- (D) $\frac{3}{8}$

Question Number: 45

Correct: 2 Wrong: -0.66

Let T_u and T_d denote the usual topology and the discrete topology on $\mathbb R$, respectively. Consider the following three topologies:

 $T_1 = \text{Usual topology on } \mathbb{R}^2 = \mathbb{R} \times \mathbb{R}$,

 T_2 = Topology generated by the basis $\{U \times V : U \in T_d, V \in T_u\}$ on $\mathbb{R} \times \mathbb{R}$,

 T_3 = Dictionary order topology on $\mathbb{R} \times \mathbb{R}$.

Then

(A)
$$T_3 \subsetneq T_1 \subseteq T_2$$

(C)
$$T_3 \subseteq T_2 \subsetneq T_1$$

(B)
$$T_1 \subsetneq T_2 \subsetneq T_3$$

(D)
$$T_1 \subsetneq T_2 = T_3$$

Question Number: 46

Correct: 2 Wrong: 0

Let X be a random variable with probability mass function

$$p(n) = \left(\frac{3}{4}\right)^{n-1} \left(\frac{1}{4}\right)$$
 for $n = 1, 2, ...$ Then $E(X - 3 \mid X > 3)$ equals _____.

Correct: 2 Wrong: 0

Let X and Y be independent and identically distributed random variables with probability mass function $p(n) = 2^{-n}$, n = 1, 2, ...

Then $P(X \ge 2Y)$ equals (rounded to 2 decimal places) _____.

Question Number: 48

Correct: 2 Wrong: 0

Let X_1, X_2, \ldots be a sequence of independent and identically distributed Poisson random variables

with mean 4. Then $\lim_{n\to\infty} P\left(4-\frac{2}{\sqrt{n}}<\frac{1}{n}\sum_{i=1}^n X_i<4+\frac{2}{\sqrt{n}}\right)$ equals _____.

Question Number: 49

Correct: 2 Wrong: 0

Let X and Y be independent and identically distributed exponential random variables with probability density function

$$f(x) = \begin{cases} e^{-x}, & x > 0, \\ 0, & \text{otherwise.} \end{cases}$$

Then $P(\max(X,Y)<2)$ equals (rounded to 2 decimal places) _____.

Question Number: 50

Correct: 2 Wrong: 0

Let E and F be any two events with P(E)=0.4, P(F)=0.3 and $P(F\mid E)=3$ $P(F\mid E^c)$. Then $P(E\mid F)$ equals (rounded to 2 decimal places) _____.

Correct : 2 Wrong : -0.66

Let X_1, X_2, \ldots, X_m $(m \ge 2)$ be a random sample from a binomial distribution with parameters n=1 and p, $p \in (0,1)$, and let $\overline{X}=\frac{1}{m}\sum_{i=1}^m X_i$. Then a uniformly minimum variance unbiased estimator for p(1-p) is

(A) $\frac{m}{m-1} \overline{X}(1-\overline{X})$

(B) $\overline{X}(1-\overline{X})$

(C) $\frac{m-1}{m}\,\bar{X}(1-\bar{X})$

(D) $\frac{1}{m} \bar{X} (1 - m\bar{X})$

Question Number: 52

Correct: 2 Wrong: 0

Let X_1, X_2, \ldots, X_9 be a random sample from a $N(0, \sigma^2)$ population. For testing $H_0: \sigma^2 = 2$ against $H_1: \sigma^2 = 1$, the most powerful test rejects H_0 if $\sum_{i=1}^9 X_i^2 < c$, where c is to be chosen such that the level of significance is 0.1. Then the power of this test equals ______.

Question Number: 53

Correct : 2 Wrong : -0.66

Let X_1, X_2, \dots, X_n $(n \ge 2)$ be a random sample from a $N(\theta, \theta)$ population, where $\theta > 0$, and let $W = \frac{1}{n} \sum_{i=1}^n X_i^2$. Then the maximum likelihood estimator of θ is

(A)
$$\frac{1}{2} + \frac{1}{2}\sqrt{1 - 4W}$$

(B)
$$\frac{1}{2} + \frac{1}{2}\sqrt{1+4W}$$

(C)
$$\frac{-1}{2} + \frac{1}{2}\sqrt{1-4W}$$

(D)
$$\frac{-1}{2} + \frac{1}{2}\sqrt{1+4W}$$

Correct: 2 Wrong: 0

Consider the following transportation problem. The entries inside the cells denote per unit cost of transportation from the origins to the destinations.

		Destination					
	200	1	2	3	Supply		
Origin	1	4	3	6	20		
	2	7	10	5	30		
	3	8	9	7	50		
	Demand	10	30	60	_		

The optimal cost of transportation equals ______.



Correct: 2 Wrong: 0

Consider the linear programming problem (LPP):

Maximize $k x_1 + 5 x_2$

Subject to $x_1 + x_2 \le 1$,

$$2x_1 + 3x_2 \le 1$$
,

$$x_1, x_2 \ge 0.$$

If $x^* = (x_1^*, x_2^*)$ is an optimal solution of the above LPP with k = 2, then the largest value of k (rounded to 2 decimal places) for which x^* remains optimal equals _____.

The ninth and the tenth of this month are Monday and Tuesday (A) figuratively (B) retrospectively (C) respectively (D) rightfully Question Number: 57	
Question Number: 57 Correct: 1 Wrong It is to read this year's textbook the last year's.	
It isto read this year's textbookthe last year's.	У
	: -0.33
(A) easier, than (B) most easy, than (C) easier, from (D) easiest, f	
	rom
Question Number: 58 A rule states that in order to drink beer, one must be over 18 years old. In a bar, there are 4 p. P is 16 years old, Q is 25 years old, R is drinking milkshake and S is drinking a beer. What is checked to ensure that the rule is being followed? (A) Only P's drink (B) Only P's drink and S's age (C) Only S's age (D) Only P's drink, Q's drink and S's age	oeople. must be
Question Number: 59 Correct: 1 Wrong:	-0.33
Fatima starts from point P, goes North for 3 km, and then East for 4 km to reach point Q. Sh turns to face point P and goes 15 km in that direction. She then goes North for 6 km. How fa from point P, and in which direction should she go to reach point P?	
(A) 8 km, East (B) 12 km, North (C) 6 km, East (D) 10 km, North	
Question Number: 60 Correct: 1 Wrong	: -0.33

500 students are taking one or more courses out of Chemistry, Physics, and Mathematics. Registration records indicate course enrolment as follows: Chemistry (329), Physics (186),

and Mathematics (63). How many students are taking all 3 subjects?

(B) 43

(A) 37

Mathematics (295), Chemistry and Physics (83), Chemistry and Mathematics (217), and Physics

(C) 47

(D) 53

Correct: 1 Wrong: -0.33

Question Number: 56

Question Number: 61 Correct: 2 Wrong: -0.66

"If you are looking for a history of India, or for an account of the rise and fall of the British Raj, or for the reason of the cleaving of the subcontinent into two mutually antagonistic parts and the effects this mutilation will have in the respective sections, and ultimately on Asia, you will not find it in these pages; for though I have spent a lifetime in the country, I lived too near the seat of events, and was too intimately associated with the actors, to get the perspective needed for the impartial recording of these matters."

Which of the following statements best reflects the author's opinion?

- (A) An intimate association does not allow for the necessary perspective.
- (B) Matters are recorded with an impartial perspective.
- (C) An intimate association offers an impartial perspective.
- (D) Actors are typically associated with the impartial recording of matters.

Question Number: 62

Correct: 2 Wrong: -0.66

Each of P, Q, R, S, W, X, Y and Z has been married at most once. X and Y are married and have two children P and Q. Z is the grandfather of the daughter S of P. Further, Z and W are married and are parents of R. Which one of the following must necessarily be FALSE?

(A) X is the mother-in-law of R

(B) P and R are not married to each other

(C) P is a son of X and Y

(D) Q cannot be married to R

Question Number: 63

Correct : 2 Wrong : -0.66

1200 men and 500 women can build a bridge in 2 weeks. 900 men and 250 women will take 3 weeks to build the same bridge. How many men will be needed to build the bridge in one week?

(A) 3000

(B) 3300

(C) 3600

(D) 3900

Question Number: 64

Correct : 2 Wrong : -0.66

The number of 3-digit numbers such that the digit 1 is never to the immediate right of 2 is

(A) 781

(B) 791

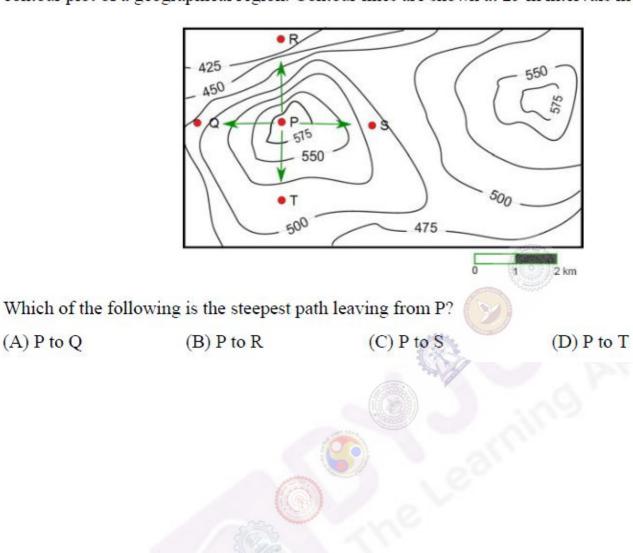
(C) 881

(D) 891

Question Number: 65 Correct: 2 Wrong: -0.66

(A) P to Q

A contour line joins locations having the same height above the mean sea level. The following is a contour plot of a geographical region. Contour lines are shown at 25 m intervals in this plot.



Q. No.	Туре	Section	Key	Marks
1	NAT	MA	1 to 1	1
2	NAT	MA	8 to 8	1
3	MCQ	MA	В	1
4	NAT	MA	48 to 48	1
5	MCQ	MA	D	1
6	NAT	MA	36 to 36	1
7	MCQ	MA	В	1
8	MCQ	MA	А	1
9	NAT	MA	0 to 0	1
10	MCQ	MA	С	1
11	NAT	MA	5 to 5	1
12	NAT	MA	8 to 8	1
13	NAT	MA	0 to 0	1
14	MCQ	MA	D	1
15	NAT	MA	5 to 5	1
16	NAT	MA	1 to 1	1
17	MCQ	MA	С	1
18	MCQ	MA	D	1
19	MCQ	MA	Α	1
20	MCQ	MA	Α	1
21	MCQ	MA	D	1
22	MCQ	MA	Α	1
23	NAT	MA	23 to 23	1
24	MCQ	MA	В	1
25	MCQ	MA	С	1
26	NAT	MA	3 to 3	2
27	MCQ	MA	С	2
28	NAT	MA	7 to 7	2
29	NAT	MA	3 to 3	2
30	MCQ	MA	D	2
31	MCQ	MA	В	2
32	NAT	MA	9 to 9	2
33	MCQ	MA	С	2
34	NAT	MA	2 to 2	2
35	MCQ	MA	А	2
36	NAT	MA	2 to 2	2

37	NAT	MA	24 to 24	2
38	NAT	MA	3 to 3	2
39	MCQ	MA	Α	2
40	MCQ	MA	В	2
41	NAT	MA	24 to 24	2
42	MCQ	MA	В	2
43	NAT	MA	64 to 64	2
44	MCQ	MA	С	2
45	MCQ	MA	D	2
46	NAT	MA	4 to 4	2
47	NAT	MA	0.27 to 0.30	2
48	NAT	MA	0.67 to 0.70	2
49	NAT	MA	0.73 to 0.77	2
50	NAT	MA	0.65 to 0.68	2
51	MCQ	MA	Α	2
52	NAT	MA	0.49 to 0.51	2
53	MCQ	MA	D	2
54	NAT	MA	590 to 590	2
55	NAT	MA	3.32 to 3.34	2
56	MCQ	GA	С	1
57	MCQ	GA	Α	1
58	MCQ	GA	В	1
59	MCQ	GA	Α	1
60	MCQ	GA	D	1
61	MCQ	GA	Α	2
62	MCQ	GA	D	2
63	MCQ	GA	С	2
64	MCQ	GA	С	2
65	MCQ	GA	В	2