

Exercise

**Question 1.** 

State which of the following are polygons:



If the given figure is a polygon, name it as convex or concave.

# Solution:

In given Fig. (ii), (iii) and (v) are polygons.

Fig. (ii) and (iii) are concave polygons while

Fig. (v) is convex.

# Question 2.

# Calculate the sum of angles of a polygon with:

# (i) 10 sides

### Solution:-

No. of sides n=10

Sum of angles of polygon  $=(n-2) imes180^\circ=(10-2) imes180^\circ=1440^\circ$ 

### (ii) 12 sides

### Solution:-

No. of sides n=12

Sum of angles  $=(n-2) imes180^\circ=(12-2) imes180^\circ=10 imes180^\circ=1800^\circ$ 

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# (iii) 20 sides

### Solution:-

n =20

Sum of angles of Polygon  $=(n-2) imes180^\circ=(20-2) imes180^\circ=3240^\circ$ 

### (iv) 25 sides

### Solution:-

n = 25

Sum of angles of polygon  $=(n-2) imes180^\circ=(25-2) imes180^\circ=4140^\circ$ 

# **Question 3.**

Find the number of sides in a polygon if the sum of its interior angles is:

(i) 900°

### Solution:-

Let no. of sides = n

Sum of angles of polygon= 900°

 $(n-2) imes180\degree=900$ 

 $n-2=rac{900}{180}$ n-2=5

n=5+2

n=7

(ii) 1620°

# Solution:-

Let no. of sides = n

Sum of angles of polygon = 1620°

 $(n-2) imes 180^\circ = 1620^\circ$ 

 $n-2 = rac{1620}{180}$ n-2=9 n=9+2 n=11



(iii) 16 right-angles

### Solution:-

Let no. of sides =n

Sum of angles of polygon =16

 $right angles = 16 \times 90 = 1440^{\circ}$ 

 $(n-2) \times 180^{\circ} = 1440^{\circ}$ 

 $n-2 = rac{1440}{180}$ n-2=8

n=8+2

n=10

(iv) 32 right-angles.

# Solution:-

Let no. of sides =n

Sum of angles of polygon =32

 $rightangles = 32 \times 90 = 2880^{\circ}$ 

 $(n-2) imes180^\circ=2880$ 

 $n-2=rac{2880}{180}$ n-2=16

n=16+2

n=18

# Question 4.

Is it possible to have a polygon; whose sum of interior angles is?

(i) 870°

# Solution:-

(i) Let no. of sides = n

Sum of angles =870°

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$$(\mathrm{n-2}) imes 180^\circ = 870^\circ$$

$$n-2 = rac{870}{180}$$

$$n-2 = \frac{20}{6}$$

$$n=rac{29}{6}+2$$

$$\mathbf{n}=rac{41}{6}$$
  
Which is not a whole number

Hence it is not possible to have a polygon, the sum of whose interior angles is 870°

# (ii) 2340°

# Solution:

Let no. of sides =n

Sum of angles =2340°

$$(n-2) imes 180^\circ=2340^\circ$$

 $n-2=rac{2340}{180}$ n-2=13

n=13+2=15 Which is a whole number.

Hence it is possible to have a polygon, the sum of whose interior angles is 2340°.

# (iii) 7 right-angles

# Solution:-

Let no. of sides =n

Sum of angles =  $7rightangles = 7 imes 90 = 630^\circ$ 

# $(n-2) imes180^\circ=630^\circ$

$$n-2 = \frac{630}{180}$$



$$n-2 = \frac{7}{2}$$

$$n = rac{7}{2} + 2$$

 $n = \frac{11}{2}$ 

Which is not a whole number. Hence it is not possible to have a polygon, the sum of whose interior angles is 7 right-angles.

### (iv) 4500°

#### Solution:-

Let no. of sides = n

$$(n-2) \times 180^\circ = 4500^\circ$$

 $n-2=rac{4500}{180}$ n-2=25

n=27

Which is a whole number.

Hence it is possible to have a polygon, the sum of whose interior angles is 4500°.

### Question 5.

(i) If all the angles of a hexagon are equal; find the measure of each angle.

### Solution:-

No. of sides of hexagon, n=6

Let each angle be  $=x^{\circ}$ 

Sum of angles =6x°

 $(n-2) imes 180\,^\circ$ = Sum of angles

$$(6-2) imes180\degree=6x\degree$$

 $4 \times 180 = 6x$ 

 $x=rac{4 imes180}{6}$ x=120°



: Each angle of hexagon =120°

(ii) If all the angles of a 14 – sided figure are equal; find the measure of each angle.

# Solution:-

No. of sides of polygon, n=14

Let each angle  $=x^{\circ}$ 

Sum of angles = $14x^{\circ}$ 

 $\because (n-2) imes 180\degree$  =Sum of angles of polygon

 $\therefore (14-2) imes 180^\circ = 14x$ 

 $12 imes 180^{\circ} = 14x$ 

 $x=rac{12 imes180}{14}$ 

 $x = \frac{1080}{7}$ 

$$x = \left(154rac{2}{7}
ight)$$
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# Question 6.

Find the sum of exterior angles obtained on producing, in order, the sides of a polygon with:

(i) 7 sides

(ii) 10 sides

(iii) 250 sides.

(i) Solution:

# No. of sides n=7

Sum of interior exterior angles at one vertex =180°

Sum of all interior exterior angles  $= 7 imes 180^\circ$ 

=1260°

Sum of interior angles =  $(n-2) \times 180^\circ = (7-2) \times 180^\circ = (7-2) \times 180^\circ$ =900°

∴Sum of exterior angles =1260°-900°

=360°

(ii)Solution

No. of sides n=10





Sum of interior and exterior angles  $= 10^{\circ} imes 180^{\circ}$ 

=1800°

But sum of interior angles  $=(n-2) imes180^\circ=(10-2) imes180^\circ$ 

=1440°

 $\therefore$ Sum of exterior angles = 1800 - 1440

Sum of exterior angles = 360°

(iii) Solution:

# No. of side n=250

Sum of all interior and exterior angles

 $= 250 \times 180^{\circ}$ =45000°

But sum of interior angles =  $(n-2) \times 180^{\circ} = (250-2) \times 180^{\circ} = 248 \times 180^{\circ}$  =44640°

∴ Sum of exterior angles =45000-44640

=360°

**Question 7 :** 

The sides of a hexagon are produced in order. If the measures of exterior angles so obtained are

(6x-1)°, (10 x+2)°,(8 x+2)°( 9 x-3)°,(5 x+4)° and (12 x+6)°;Find each exterior angle.

# Solution:-

Sum of exterior angles of hexagon formed by producing sides of order =360°

 $\therefore (6x-1)^{\circ} + (10x+2)^{\circ} + (8x+2)^{\circ} + (9x-3)^{\circ} + (5x+4)^{\circ} + (12x+6)^{\circ} = 360^{\circ}$   $50x = 360^{\circ} - 10^{\circ}$   $50x = 350^{\circ}$   $x = \frac{350}{50}$  x = 7  $\therefore \text{ Angles are } (6x-1)^{\circ} : (10x+2)^{\circ} : (8x+2)^{\circ} ; (9x-3)^{\circ} (5x+4)^{\circ} \text{ and } (12x+6)^{\circ}$   $i.e., (6x7-1)^{\circ} : (10x7+2)^{\circ} : (8x7+2)^{\circ} : (9x7-3)^{\circ} : (5x7+4)^{\circ} : (12x7+6)^{\circ})$ 

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41°; 72°; 58°; 60°; 39° and 90°
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# **Question 8.**

The interior angles of a pentagon are in the ratio 4:5:6:7:5. Find each angle of the pentagon.

# Solution:-



Let the interior angles of the pentagon be 4 x, 5 x, 6 x, 7 x, 5 x Their sum = 4 x+5 x+6 x+7 x+5 x=27 x Sum of interior angles of polygon =  $(n - 2) \times 180^{\circ} = (5 - 2) \times 180^{\circ} = 540^{\circ}$  27x = 540  $x = \frac{540}{27} = 20^{\circ}$   $\therefore$  Angles are  $4 \times 20^{\circ} = 80^{\circ}$   $5 \times 20^{\circ} = 100^{\circ}$   $6 \times 20^{\circ} = 120^{\circ}$   $7 \times 20^{\circ} = 140^{\circ}$  $5 \times 20^{\circ} = 100^{\circ}$ 

### **Question 9**

Two angles of a hexagon are 120° and 160°. If the remaining four angles are equal, find each equal angle.

### Solution:-

Two angles of a hexagon are 120°, 160°

Let remaining four angles be x, x, x and x.

Their sum =  $4 x + 280^{\circ}$ 

But sum of all the interior angles of a hexagon  $=(6-2) imes180^\circ=4 imes180^\circ=720^\circ$ 

∴ 4x+280°=720°

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\Rightarrow 4x=720°-280°=440° \Rightarrow x=110°
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∴Equal angles are 110° (each)

### **Question 10**

The figure, given below, shows a pentagon ABCDE with sides AB and ED parallel to each other, and <B : <C : <D:5:6:7.







(i) Using formula, find the sum of interior angles of the pentagon.

- (ii) Write the value of ∠A+∠E
- (iii) Find angles B, C and D .

# Solution:-

(i) Sum of interior angles of the pentagon  $= (5-2) \times 180^{\circ}$ =  $3 \times 180^{\circ} = 540^{\circ}$ (:: sumforapolygonofxsides =  $(x-2) \times 180^{\circ}$ 

(ii) Since AB || ED

∴∠A+∠E=180°

- (iii) Let  $\angle B=5 \times \angle C=6 \times \angle D=7x$
- ∴5x+6x+7x+180°=540°

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\angle A + \angle E = 180^{\circ} Proved in (ii)
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- 18x=540°-180°
- $\Rightarrow$  18x=360°  $\Rightarrow$  x=20°

 $\because \angle B = 5 \times 20^{\circ} = 100^{\circ}, \angle C = 6 \times 20 = 120^{\circ} \angle D = 7 \times 20 = 140^{\circ}$ 

# Question 11.

Two angles of a polygon are right angles and the remaining are 120° each. Find the number of sides in it.

# Solution:-

Let number of sides = n



Sum of interior angles  $=(n-2) imes180^\circ$ =180n-360°

Sum of 2 right angles  $= 2 imes 90\,^\circ$ 

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=180°
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∴ Sum of other angles =180n-360°-180°

=180 n-540

No. of vertices at which these angles are formed

=n-2

 $\therefore$  Each interior angle =  $\frac{180n-540}{n-2}$   $\therefore$   $\frac{180n-540}{n-2}=120^{\circ}$ 180 n-540=120 n-240 180 n-120 n=-240+540 60 n=300

n = 300/60

$$n = 5$$
  
Question 12.

In a hexagon ABCDEF, side AB is parallel to side FE and  $\angle B: \angle C: \angle D: \angle E=6:4:2:3$ .find  $\angle B$  and  $\angle D$ .

# Solution:-



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Given: Hexagon ABCDEF in which AB II EF

and  $\angle B: \angle C: \angle D: \angle E=6:4:2:3$ 

To find :  $\angle B$  and  $\angle D$ 

Proof: No of sides n=6



 $m \therefore$  Sum of interior angles  $=(n-2) imes180^{\,\circ}=(6-2) imes180^{\,\circ}=720^{\,\circ}$ 

∴ABIEF (Given)

 $\therefore \mathbf{A} + \angle \mathbf{F} = 180^{\circ}$ But  $\angle A + \angle B + \angle C + \angle D + \angle E + \angle F = 720^{\circ}$ 

(proved)

 $\angle B + \angle C + \angle D + \angle E + \angle 180^{\circ} = 720^{\circ} \because \angle B + \angle C + \angle D + \angle E = 720^{\circ} - 180^{\circ} = 540^{\circ}$ Ratio =6:4:2:3

Sum of parts =6+4+2+3=15

 $\therefore \angle B = \frac{6}{15} \times 540 = 216^{\circ} \angle \mathbf{D} = \frac{2}{15} \times 540^{\circ} = 72^{\circ}$ Hence  $\angle B = 216^{\circ} : \angle D = 72^{\circ}$ 

### Question 13.

the angles of a hexagon are  $x+10^{\circ}, 2x+20^{\circ}, 2x-20^{\circ}, 3x-50^{\circ}, x+40^{\circ}$  and  $x+20^{\circ}$ . Find x.

### Solution:-

Angles of a hexagon are x+10°, 2x+20°,

2x-20°, 3x-50°, x+40° and x+20°

m : But sum of angles of a hexagon  $=(x-2) imes180^\circ=(6-2) imes180^\circ=4 imes180^\circ=720^\circ$ 

But sum=x+10+2x+20°+2x-20°+3x-50°+x+40+x+20

=10x+90-70=10x+20

∴10x+20=720°⇒10x=720-20=700

 $\Rightarrow x = \frac{700^{\circ}}{10} = 70^{\circ}$ ∴x=70°

#### **Question 14.**

In a pentagon, two angles are 40° and 60° and the rest are in the ratio 1:3:7. Find the biggest angle of the pentagon.

#### Solution:-



In a pentagon, two angles are 40° and 60° Sum of remaining 3 angles  $= 3 imes 180\degree$ 

=540°-40°-60°=540°-100°=440°

Ratio in these 3 angles =1:3:7

Sum of ratios =1+3+7=11

Biggest angle =  $rac{440 imes7}{11}=280\,^\circ$ 

# **Question 15**

# Fill in the blanks:

In case of regular polygon, with:

No. of sides	Each exterior angle	Each interior angle
(i)8		
(ii)12		
(iii)	72°	
(iv)	45°	
(v)		150°
(vi)		140°

# Solution:-

No. Of sides	Each exterior angle	Each interior angle
(i)8	45°	135°
(ii)12	30°	150°
(iii)5	72°	108°
(iv)8	45°	135°
(v)12	30°	150°
(vi)9	40°	140°



# **Explanation:**

(i) Each exterior angle  $= rac{360^\circ}{8} = 45^\circ$ Each interior angle=180°-45°-135° (ii) Each exterior angle  $=rac{360^\circ}{12}=30^\circ$ Each interior angle =180°-30°=150° (iii) Since each exterior =72°  $\therefore$  Number of sides  $= rac{360^{\circ}}{72^{\circ}} = 5$ Also interior angle =180°-72°=108° (iv) Since each exterior angle =45° : Number of sides =  $\frac{360^{\circ}}{45^{\circ}} = 8$ Interior angle =180°-45°=135° (v) Since interior angle =150° ∴ Exterior angle =180°-150°=30°  $\therefore$  Number of sides  $= rac{360^\circ}{30^\circ} = 12$ (vi) Since interior angle =140° ∴ Exterior angle =180°-140°=40°  $\therefore$  Number of sides  $=rac{360^\circ}{40^\circ}=9$ 

