## General Aptitude (GA)

Q. 1 - Q. 5 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | (i) <br> (ii) <br> (iii) |
| :--- | :--- |
|  | Arun and Aparna are here. <br> (iv) <br> Arun's families is here. <br> Which of the above sentences are grammatically CORRECT? |
| (A) | (i) and (ii) |
| (B) | (i) and (iv) |
| (C) | (ii) and (iv) |
| (D) | (iii) and (iv) |


| $0^{2}$ | PHYLAXIS |
| :---: | :---: |
| (4) | PH ${ }^{\text {PVXXI2 }}$ |
| (8) | bHイГVXIz |
| (c) | dH사 XXIz |
| (1) | bHATVXIS |


| Q.3 | Two identical cube shaped dice each with faces numbered $\mathbf{1}$ to $\mathbf{6}$ are rolled <br> simultaneously. The probability that an even number is rolled out on each <br> dice is: |
| :--- | :--- |
| (A) | $\frac{1}{36}$ |
| (B) | $\frac{1}{12}$ |
| (C) | $\frac{1}{8}$ |
| (D) | $\frac{1}{4}$ |


| Q.4 | $\oplus$ and $\odot$ are two operators on numbers $\boldsymbol{p}$ and $\boldsymbol{q}$ such that <br> $\boldsymbol{p} \odot \boldsymbol{q}=\boldsymbol{p}-\boldsymbol{q}$, and $p \oplus q=p \times q$ <br> Then, $(\mathbf{9} \odot(\mathbf{6} \oplus \mathbf{7})) \odot(\mathbf{7} \oplus(\mathbf{6} \odot \mathbf{5}))=$ <br> (A) |
| :--- | :--- |
| (B) | 40 |
| (C) | -26 |
| (D) | -33 |

GATE

## Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Civil Engineering (CE, Set-2)

| Q.5 | Four persons $P, Q, R$ and $S$ are to be seated in a row. $R$ should not be seated <br> at the second position from the left end of the row. The number of distinct <br> seating arrangements possible is: |
| :--- | :--- |
| (A) | 6 |
| (B) | 9 |
| (C) | 18 |
| (D) | 24 |

Civil Engineering (CE, Set-2)
Q. 6 - Q. 10 Multiple Choice Question (MCQ), carry TWO marks each (for each wrong answer: - 2/3).

| Q.6 | On a planar field, you travelled 3 units East from a point O. Next you <br> travelled 4 units South to arrive at point P. Then you travelled from P in the <br> North-East direction such that you arrive at a point that is 6 units East of <br> point O. Next, you travelled in the North-West direction, so that you arrive <br> at point Q that is 8 units North of point P. <br> The distance of point Q to point O, in the same units, should be -_ |
| :--- | :--- |
| (A) | 3 |
| (B) | 4 |
| (C) | 5 |
| (D) | 6 |


| Q.7 | The author said, "Musicians rehearse before their concerts. Actors rehearse <br> their roles before the opening of a new play. On the other hand, I find it <br> strange that many public speakers think they can just walk on to the stage <br> and start speaking. In my opinion, it is no less important for public speakers <br> to rehearse their talks." <br> Based on the above passage, which one of the following is TRUE? |
| :---: | :--- |
| (A) | The author is of the opinion that rehearsing is important for musicians, actors <br> and public speakers. |
| (B) | The author is of the opinion that rehearsing is less important for public speakers <br> than for musicians and actors. |
| (C) | The author is of the opinion that rehearsing is more important only for <br> musicians than public speakers. |
| (D) | The author is of the opinion that rehearsal is more important for actors than <br> musicians. |

GATE

## Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Civil Engineering (CE, Set-2)

| Q.8 | 1. Some football players play cricket. <br> 2. All cricket players play hockey. <br> Among the options given below, the statement that logically follows from <br> the two statements 1 and 2 above, is: |
| :--- | :--- |
| (A) | No football player plays hockey. |
| (B) | Some football players play hockey. |
| (C) | All football players play hockey. |
| (D) | All hockey players play football. |

Civil Engineering (CE, Set-2)

| Q. 9 |  |
| :--- | :--- |
| In the figure shown above, PQRS is a square. The shaded portion is formed |  |
| by the intersection of sectors of circles with radius equal to the side of the |  |
| square and centers at S and Q. |  |
| The probability that any point picked randomly within the square falls in the |  |
| shaded area is |  |


| Q.10 | In an equilateral triangle $P Q R$, side $P Q$ is divided into four equal parts, side <br> QR is divided into six equal parts and side PR is divided into eight equal parts. <br> The length of each subdivided part in cm is an integer. <br> The minimum area of the triangle $\mathbf{P Q R}$ possible, in $^{\mathbf{~ c m}}{ }^{\mathbf{2}}$, is |
| :---: | :--- |
| (A) | 18 |
| (B) | 24 |
| (C) | $48 \sqrt{3}$ |
| (D) | $144 \sqrt{3}$ |

## Civil Engineering (CE, Set-2)

Q. 1 - Q. 16 Multiple Choice Question (MCQ), carry ONE mark each (for each wrong answer: - 1/3).

| Q.1 | The value of $\lim _{x \rightarrow \infty} \frac{x \ln (x)}{1+x^{2}}$ is |
| :--- | :--- |
| (A) | 0 |
| (B) | 1.0 |
| (C) | 0.5 |
| (D) | $\infty$ |


| Q. 2 | The rank of the matrix $\left[\begin{array}{cccc}5 & 0 & -5 & 0 \\ 0 & 2 & 0 & 1 \\ -5 & 0 & 5 & 0 \\ 0 & 1 & 0 & 2\end{array}\right]$ is |
| :--- | :--- |
| (A) | 1 |
| (B) | 2 |
| (C) | 3 |
| (D) | 4 |


| Q.3 | The unit normal vector to the surface $X^{2}+Y^{2}+Z^{2}-48=0$ at the point $(\mathbf{4}, \mathbf{4}$, <br> 4) is |
| :--- | :--- |
| (A) | $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$ |$\quad$| (B) |
| :--- |
| (C) |
| $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{2}{\sqrt{2}}, \frac{2}{\sqrt{2}}$ |
| (D) |


| Q. 4 | If $\boldsymbol{A}$ is a square matrix then orthogonality property mandates |
| :---: | :--- |
| (A) | $A A^{\mathrm{T}}=I$ |
| (B) | $A A^{\mathrm{T}}=0$ |
| (C) | $A A^{\mathrm{T}}=A^{-1}$ |
| (D) | $A A^{\mathrm{T}}=A^{2}$ |


| Q.5 | In general, the CORRECT sequence of surveying operations is |
| :--- | :--- |
| $(A)$ | Field observations $\rightarrow$ Reconnaissance $\rightarrow$ Data analysis $\rightarrow$ Map making |
| $(B)$ | Data analysis $\rightarrow$ Reconnaissance $\rightarrow$ Field observations $\rightarrow$ Map making |
| $(C)$ | Reconnaissance $\rightarrow$ Field observations $\rightarrow$ Data analysis $\rightarrow$ Map making |
| $(D)$ | Reconnaissance $\rightarrow$ Data analysis $\rightarrow$ Field observations $\rightarrow$ Map making |


| Q.6 | Strain hardening of structural steel means |
| :---: | :--- |
| (A) | experiencing higher stress than yield stress with increased deformation |
| (B) | strengthening steel member externally for reducing strain experienced |
| (C) | strain occurring before plastic flow of steel material |
| (D) | decrease in the stress experienced with increasing strain |


| Q. 7 | A single story building model is shown in the figure. The rigid bar of mass ' $\boldsymbol{m}$ ' is supported by three massless elastic columns whose ends are fixed against rotation. For each of the columns, the applied lateral force $(\boldsymbol{P})$ and corresponding moment $(M)$ are also shown in the figure. The lateral deflection $(\delta)$ of the bar is given by $\delta=\frac{P L^{3}}{12 E I}$, where $L$ is the effective length of the column, $E$ is the Young's modulus of elasticity and $I$ is the area moment of inertia of the column cross-section with respect to its neutral axis. <br> For the lateral deflection profile of the columns as shown in the figure, the natural frequency of the system for horizontal oscillation is |
| :---: | :---: |
| (A) | $6 \sqrt{\frac{E I}{m L^{3}}} \mathrm{rad} / \mathrm{s}$ |
| (B) | $\frac{1}{L} \sqrt{\frac{2 E I}{m}} \mathrm{rad} / \mathrm{s}$ |
| (C) | $2 \sqrt{\frac{6 E I}{m L^{3}}} \mathrm{rad} / \mathrm{s}$ |
| (D) | $\frac{2}{L} \sqrt{\frac{E I}{m}} \mathrm{rad} / \mathrm{s}$ |

GATE
2.21

## Graduate Aptitude Test in Engineering 2021

 Organising Institute - IIT BombayCivil Engineering (CE, Set-2)

| Q.8 | Seasoning of timber for use in construction is done essentially to |
| :---: | :--- |
| (A) | increase strength and durability |
| (B) | smoothen timber surfaces |
| (C) | remove knots from timber logs |
| (D) | cut timber in right season and geometry |


| Q.9 | In case of bids in Two-Envelop System, the correct option is |
| :---: | :--- |
| (A) | Technical bid is opened first |
| (B) | Financial bid is opened first |
| (C) | Both (Technical and Financial) bids are opened simultaneously |
| (D) | Either of the two (Technical and Financial) bids can be opened first |


| Q.10 | The most appropriate triaxial test to assess the long-term stability of an <br> excavated clay slope is |
| :--- | :--- |
| (A) | consolidated drained test |
| (B) | unconsolidated undrained test |
| (C) | consolidated undrained test |
| (D) | unconfined compression test |


| Q.11 | As per the Unified Soil Classification System (USCS), the type of soil <br> represented by 'MH' is |
| :--- | :--- |
| (A) | Inorganic silts of high plasticity with liquid limit more than $50 \%$ |
| (B) | Inorganic silts of low plasticity with liquid limit less than $50 \%$ |
| (C) | Inorganic clays of high plasticity with liquid limit less than $50 \%$ |
| (D) | Inorganic clays of low plasticity with liquid limit more than $50 \%$ |

GATE
$2 冈 21$

## Graduate Aptitude Test in Engineering 2021

 Organising Institute - IIT BombayCivil Engineering (CE, Set-2)

| Q. 12 | The ratio of the momentum correction factor to the energy correction factor for a laminar flow in a pipe is |
| :---: | :---: |
| (A) | $\frac{1}{2}$ |
| (B) | $\frac{2}{3}$ |
| (C) | 1 |
| (D) | $\frac{3}{2}$ |
| Q. 13 | Relationship between traffic speed and density is described using a negatively sloped straight line. If $\boldsymbol{v}_{f}$ is the free-flow speed then the speed at which the maximum flow occurs is |
| (A) | 0 |
| (B) | $\frac{v_{f}}{4}$ |
| (C) | $\frac{v_{f}}{2}$ |
| (D) | $v_{f}$ |

$\qquad$

| Q.14 | Determine the correctness or otherwise of the following Assertion [a] and the <br> Reason [r]. <br> Assertion [a]: One of the best ways to reduce the amount of solid wastes is to <br> reduce the consumption of raw materials. <br> Reason [r]: Solid wastes are seldom generated when raw materials are <br> converted to goods for consumption. |
| :--- | :--- |
| (A) | Both [a] and [r] are true and [r] is the correct reason for [a] |
| (B) | Both [a] and [r] are true but [r] is not the correct reason for [a] |
| (C) | Both [a] and [r] are false |
| (D) | [a] is true but [r] is false |


| Q.15 | The hardness of a water sample is measured directly by titration with <br> 0.01 M solution of ethylenediamine tetraacetic acid (EDTA) using <br> eriochrome black T (EBT) as an indicator. The EBT reacts and forms <br> complexes with divalent metallic cations present in the water. During <br> titration, the EDTA replaces the EBT in the complex. When the replacement <br> of EBT is complete at the end point of the titration, the colour of the solution <br> changes from |
| :--- | :--- |
| (A) | blue-green to reddish brown |
| (B) | blue to colourless |
| (C) | reddish brown to pinkish yellow |
| (D) | wine red to blue |


| Q.16 | The softening point of bitumen has the same unit as that of |
| :---: | :--- |
| (A) | distance |
| (B) | temperature |
| (C) | time |
| (D) | viscosity |

## Q. 17 Multiple Select Question (MSQ), carry ONE mark (no negative marks).

| Q.17 | Which of the following statement(s) is/are correct? |
| :---: | :--- |
| (A) | Increased levels of carbon monoxide in the indoor environment result in the <br> formation of carboxyhemoglobin and the long term exposure becomes a cause of <br> cardiovascular diseases. |
| (B) | Volatile organic compounds act as one of the precursors to the formation of <br> photochemical smog in the presence of sunlight. |
| (C) | Long term exposure to the increased level of photochemical smog becomes a <br> cause of chest constriction and irritation of the mucous membrane. |
| (D) | Increased levels of volatile organic compounds in the indoor environment will <br> result in the formation of photochemical smog which is a cause of cardiovascular <br> diseases. |

## Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Civil Engineering (CE, Set-2)
Q. 18 - Q. 25 Numerical Answer Type (NAT), carry ONE mark each (no negative marks).
Q. 18 The value (round off to one decimal place) of $\int_{-1}^{1} x e^{|x|} d x$ is $\qquad$
Q. 19 A solid circular torsional member OPQ is subjected to torsional moments as shown in the figure (not to scale). The yield shear strength of the constituent material is $\mathbf{1 6 0} \mathrm{MPa}$.


The absolute maximum shear stress in the member (in MPa, round off to one decimal place) is $\qquad$
Q. 20 A propped cantilever beam $X Y$, with an internal hinge at the middle, is carrying a uniformly distributed load of $10 \mathrm{kN} / \mathrm{m}$, as shown in the figure.


The vertical reaction at support X (in kN , in integer) is $\qquad$
Q. 21 The internal $\left(d_{i}\right)$ and external ( $d_{o}$ ) diameters of a Shelby sampler are 48 mm and 52 mm , respectively. The area ratio $\left(A_{r}\right)$ of the sampler (in \%, round off to two decimal places) is $\qquad$

```
Q.22 A 12-hour unit hydrograph (of 1 cm excess rainfall) of a catchment is of a
triangular shape with a base width of }\mathbf{144}\mathrm{ hour and a peak discharge of 23
m}\mp@subsup{}{}{3}/\textrm{s}\mathrm{ . The area of the catchment (in km}\mp@subsup{}{}{2}\mathrm{ , round off to the nearest integer)
is
```

$\qquad$
Q. 23 A lake has a maximum depth of $\mathbf{6 0} \mathbf{m}$. If the mean atmospheric pressure in the lake region is 91 kPa and the unit weight of the lake water is $9790 \mathrm{~N} / \mathrm{m}^{3}$, the absolute pressure (in kPa , round off to two decimal places) at the maximum depth of the lake is $\qquad$
Q. 24 In a three-phase signal system design for a four-leg intersection, the critical flow ratios for each phase are $\mathbf{0 . 1 8 , 0 . 3 2}$, and 0.22 . The total loss time in each of the phases is $\mathbf{2} \mathbf{s}$. As per Webster's formula, the optimal cycle length (in s , round off to the nearest integer) is $\qquad$
Q. 25 A horizontal angle $\theta$ is measured by four different surveyors multiple times and the values reported are given below.

| Surveyor | Angle $\theta$ | Number of <br> observations |
| :---: | :---: | :---: |
| 1 | ${36^{\circ} 30^{\prime}}^{4}$ |  |
| 2 | $36^{\circ} 00^{\prime}$ | 3 |
| 3 | ${35^{\circ}}^{\circ} 30^{\prime}$ | 8 |
| 4 | $36^{\circ} 30^{\prime}$ | 4 |

The most probable value of the angle $\theta$ (in degree, round off to two decimal places) is $\qquad$

## Graduate Aptitude Test in Engineering 2021

 Organising Institute - IIT BombayCivil Engineering (CE, Set-2)
Q. 26 - Q. 35 Multiple Choice Question (MCQ), carry TWO mark each (for each wrong answer: - 2/3).

| Q.26 | If $\boldsymbol{k}$ is a constant, the general solution of $\frac{d y}{d x}-\frac{y}{x}=1$ will be in the form of |
| :--- | :--- |
| (A) | $y=x \ln (k x)$ |
| (B) | $y=k \ln (k x)$ |
| (C) | $y=x \ln (x)$ |
| (D) | $y=x k \ln (k)$ |


| Q. 27 | The smallest eigenvalue and the corresponding eigenvector of the matrix <br> $\left[\begin{array}{cc}2 & -2 \\ -1 & 6\end{array}\right]$, respectively, are |
| :--- | :--- |
| (A) | 1.55 and $\left\{\begin{array}{l}2.00 \\ 0.45\end{array}\right\}$ |$|$| (B) | 2.00 and $\left\{\begin{array}{c}1.00 \\ 1.00\end{array}\right\}$ |
| :--- | :--- |
| (C) | 1.55 and $\left\{\begin{array}{c}-2.55 \\ -0.45\end{array}\right\}$ |
| (D) | 1.55 and $\left\{\begin{array}{c}2.00 \\ -0.45\end{array}\right\}$ |

GATE

## Graduate Aptitude Test in Engineering 2021

 Organising Institute - IIT BombayCivil Engineering (CE, Set-2)

| Q.28 | A prismatic steel beam is shown in the figure. |
| :--- | :--- |
| (A) | $M_{\mathrm{p}, \mathrm{static}}>\frac{2 P L}{9}=M_{\mathrm{p}, \mathrm{kinematic}}$ |
| The plastic moment, $M_{\mathrm{p}}$ calculated for the collapse mechanism using static |  |
| (B) | $M_{\mathrm{p}, \mathrm{static}}=\frac{2 P L}{9} \neq M_{\mathrm{p}, \mathrm{kinematic}}$ |
| (C) | $M_{\mathrm{p}, \mathrm{static}}=\frac{2 P L}{9}=M_{\mathrm{p}, \mathrm{kinematic}}$ |
| (D) | $M_{\mathrm{p}, \mathrm{static}}<\frac{2 P L}{9}=M_{\mathrm{p}, \mathrm{kinematic}}$ |


| Q.29 | A frame EFG is shown in the figure. All members are prismatic and have <br> equal flexural rigidity. The member FG carries a uniformly distributed load <br> w per unit length. Axial deformation of any member is neglected. |
| :--- | :--- |
| (A) | $0.375 w L$ |
| (B) | $0.453 w L$ |
| (C) | $0.482 w L$ |
| (D) | $0.500 w L$ |


| Q. 30 | A clay layer of thickness $\boldsymbol{H}$ has a preconsolidation pressure $\boldsymbol{p}_{\boldsymbol{c}}$ and an initial <br> void ratio $\boldsymbol{e}_{0}$. The initial effective overburden stress at the mid-height of the <br> layer is $p_{0}$. At the same location, the increment in effective stress due to <br> applied external load is $\Delta \boldsymbol{p}$. The compression and swelling indices of the clay <br> are $\boldsymbol{C}_{\boldsymbol{c}}$ and $\boldsymbol{C}_{s}$, respectively. If $p_{0}<p_{c}<\left(p_{0}+\Delta p\right)$, then the correct <br> expression to estimate the consolidation settlement $\left(s_{c}\right)$ of the clay layer is |
| :--- | :--- |
| (A) | $s_{c}=\frac{H}{1+e_{0}}\left[C_{c} \log \frac{p_{c}}{p_{0}}+C_{s} \log \frac{p_{0}+\Delta p}{p_{c}}\right]$ |
| (B) | $s_{c}=\frac{H}{1+e_{0}}\left[C_{s} \log \frac{p_{c}}{p_{0}}+C_{c} \log \frac{p_{0}+\Delta p}{p_{c}}\right]$ |
| (C) | $s_{c}=\frac{H}{1+e_{0}}\left[C_{c} \log \frac{p_{0}}{p_{c}}+C_{s} \log \frac{p_{0}+\Delta p}{p_{c}}\right]$ |
| (D) | $s_{c}=\frac{H}{1+e_{0}}\left[C_{s} \log \frac{p_{0}}{p_{c}}+C_{c} \log \frac{p_{0}+\Delta p}{p_{c}}\right]$ |


| Q.31 | A rectangular open channel of 6 m width is carrying a discharge of $20 \mathrm{~m} \mathrm{~m}^{3} / \mathrm{s}$. <br> Consider the acceleration due to gravity as $9.81 \mathrm{~m} / \mathbf{s}^{2}$ and assume water as <br> incompressible and inviscid. The depth of flow in the channel at which the <br> specific energy of the flowing water is minimum for the given discharge will <br> then be |
| :--- | :--- |
| (A) | 0.82 m |
| (B) | 1.04 m |
| (C) | 2.56 m |
| (D) | 3.18 m |

Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Civil Engineering (CE, Set-2)

| Q. 32 | Read the statements given below. <br> (i) Value of the wind profile exponent for the 'very unstable' atmosphere <br> is smaller than the wind profile exponent for the 'neutral' atmosphere. <br> (ii) Downwind concentration of air pollutants due to an elevated point <br> source will be inversely proportional to the wind speed. <br> (iii)Value of the wind profile exponent for the 'neutral' atmosphere is <br> smaller than the wind profile exponent for the 'very unstable' <br> atmosphere. <br> (iv) Downwind concentration of air pollutants due to an elevated point <br> source will be directly proportional to the wind speed. |
| :--- | :--- |
| Select the correct option. |  |


| Q.33 | A water filtration unit is made of uniform-size sand particles of 0.4 mm <br> diameter with a shape factor of 0.84 and specific gravity of 2.55 . The depth <br> of the filter bed is 0.70 m and the porosity is 0.35 . The filter bed is to be <br> expanded to a porosity of 0.65 by hydraulic backwash. If the terminal <br> settling velocity of sand particles during backwash is $4.5 \mathrm{~cm} / \mathrm{s}$, the required <br> backwash velocity is |
| :--- | :--- |
| (A) | $5.79 \times 10^{-3} \mathrm{~m} / \mathrm{s}$ |
| (B) | $6.35 \times 10^{-3} \mathrm{~m} / \mathrm{s}$ |
| (C) | $0.69 \mathrm{~cm} / \mathrm{s}$ |
| (D) | $0.75 \mathrm{~cm} / \mathrm{s}$ |


| Q.34 | For a given traverse, latitudes and departures are calculated and it is found <br> that sum of latitudes is equal to $\mathbf{+ 2 . 1} \mathbf{~ m}$ and the sum of departures is equal to <br> $-\mathbf{2 . 8} \mathbf{~}$. The length and bearing of the closing error, respectively, are |
| :---: | :--- |
| (A) | 3.50 m and $53^{\circ} 7^{\prime} 48{ }^{\prime \prime} \mathrm{NW}$ |
| (B) | 2.45 m and $53^{\circ} 7^{\prime} 48 \mathrm{NW}$ |
| (C) | 0.35 m and $53.13^{\circ} \mathrm{SE}$ |
| (D) | 3.50 m and $53.13^{\circ} \mathrm{SE}$ |


| Q.35 | From laboratory investigations, the liquid limit, plastic limit, natural <br> moisture content and flow index of a soil specimen are obtained as $\mathbf{6 0 \%}$, <br> $\mathbf{2 7 \%}, \mathbf{3 2 \%}$ and 27, respectively. The corresponding toughness index and <br> liquidity index of the soil specimen, respectively, are |
| :---: | :--- |
| (A) | 0.15 and 1.22 |
| (B) | 0.19 and 6.60 |
| (C) | 1.22 and 0.15 |
| (D) | 6.60 and 0.19 |

$\qquad$
Q. 36 - Q. 55 Numerical Answer Type (NAT), carry TWO mark each (no negative marks).
Q. 36 A function is defined in Cartesian coordinate system as $f(x, y)=x e^{y}$. The value of the directional derivative of the function (in integer) at the point ( $\mathbf{2}$, 0 ) along the direction of the straight line segment from point $(2,0)$ to point $\left(\frac{1}{2}, 2\right)$ is $\qquad$
Q. 37 An elevated cylindrical water storage tank is shown in the figure. The tank has inner diameter of 1.5 m . It is supported on a solid steel circular column of diameter 75 mm and total height $(L)$ of 4 m . Take, water density $=$ $1000 \mathrm{~kg} / \mathrm{m}^{3}$ and acceleration due to gravity $=10 \mathrm{~m} / \mathrm{s}^{2}$.


If elastic modulus $(E)$ of steel is 200 GPa , ignoring self-weight of the tank, for the supporting steel column to remain unbuckled, the maximum depth ( $h$ ) of the water permissible (in m , round off to one decimal place) is $\qquad$

Civil Engineering (CE, Set-2)
Q. 38 A prismatic fixed-fixed beam, modelled with a total lumped-mass of 10 kg as a single degree of freedom (SDOF) system is shown in the figure.


If the flexural stiffness of the beam is $4 \pi^{2} \mathrm{kN} / \mathrm{m}$, its natural frequency of vibration (in Hz , in integer) in the flexural mode will be $\qquad$
Q. 39 A perfectly flexible and inextensible cable is shown in the figure (not to scale). The external loads at $F$ and $G$ are acting vertically.


The magnitude of tension in the cable segment FG (in kN , round off to two decimal places) is $\qquad$

Civil Engineering (CE, Set-2)
Q. 40 A fire hose nozzle directs a steady stream of water of velocity $50 \mathrm{~m} / \mathrm{s}$ at an angle of $45^{\circ}$ above the horizontal. The stream rises initially but then eventually falls to the ground. Assume water as incompressible and inviscid. Consider the density of air and the air friction as negligible, and assume the acceleration due to gravity as $9.81 \mathrm{~m} / \mathrm{s}^{2}$. The maximum height (in m , round off to two decimal places) reached by the stream above the hose nozzle will then be $\qquad$
Q. 41 A rectangular cross-section of a reinforced concrete beam is shown in the figure. The diameter of each reinforcing bar is 16 mm . The values of modulus of elasticity of concrete and steel are $2.0 \times 10^{4} \mathrm{MPa}$ and $2.1 \times 10^{5} \mathrm{MPa}$, respectively.


The distance of the centroidal axis from the centerline of the reinforcement $(x)$ for the uncracked section (in mm , round off to one decimal place) is $\qquad$
Q. 42 The activity details for a small project are given in the Table.

| Activity | Duration (days) | Depends on |
| :--- | :--- | :--- |
| A | 6 | - |
| B | 10 | A |
| C | 14 | A |
| D | 8 | B |
| E | 12 | C |
| F | 8 | C |
| G | 16 | D, E |
| H | 8 | F, G |
| K | 2 | B |
| L | 5 | G, K |

The total time (in days, in integer) for project completion is $\qquad$
Q. 43

An equipment has been purchased at an initial cost of ₹ 160000 and has an estimated salvage value of ₹ 10000 . The equipment has an estimated life of 5 years. The difference between the book values (in ₹, in integer) obtained at the end of $4^{\text {th }}$ year using straight line method and sum of years digit method of depreciation is $\qquad$ -

Civil Engineering (CE, Set-2)
Q. 44

A rectangular footing of size $2.8 \mathrm{~m} \times 3.5 \mathrm{~m}$ is embedded in a clay layer and a vertical load is placed with an eccentricity of 0.8 m as shown in the figure (not to scale). Take Bearing capacity factors: $N_{c}=5.14, N_{q}=1.0$, and $N_{\gamma}=$ 0.0; Shape factors: $s_{c}=1.16, s_{q}=1.0$ and $s_{\gamma}=1.0$; Depth factors: $d_{c}=1.1, d_{q}=$ 1.0 and $d_{\gamma}=1.0$; and Inclination factors: $i_{c}=1.0$ and $i_{q}=1.0$ and $i_{\gamma}=1.0$.


Using Meyerhoff's method, the load (in kN , round off to two decimal places) that can be applied on the footing with a factor of safety of 2.5 is

Graduate Aptitude Test in Engineering 2021 Organising Institute - IIT Bombay

Civil Engineering (CE, Set-2)

| Q. 45 | The soil profile at a road construction site is as shown in figure (not to scale). A large embankment is to be constructed at the site. The ground water table (GWT) is located at the surface of the clay layer, and the capillary rise in the sandy soil is negligible. The effective stress at the middle of the clay layer after the application of the embankment loading is $180 \mathrm{kN} / \mathrm{m}^{2}$. Take unit weight of water, $\gamma_{w}=9.81 \mathrm{kN} / \mathrm{m}^{3}$. <br> The primary consolidation settlement (in m , round off to two decimal places) of the clay layer resulting from this loading will be $\qquad$ |
| :---: | :---: |

Q. 46 Numerically integrate, $f(x)=10 x-20 x^{2}$ from lower limit $a=0$ to upper limit $b=0.5$. Use Trapezoidal rule with five equal subdivisions. The value (in units, round off to two decimal places) obtained is $\qquad$
Q. 47 The void ratio of a clay soil sample $M$ decreased from 0.575 to 0.510 when the applied pressure is increased from 120 kPa to 180 kPa . For the same increment in pressure, the void ratio of another clay soil sample $\mathbf{N}$ decreases from 0.600 to 0.550 . If the ratio of hydraulic conductivity of sample $M$ to sample $N$ is 0.125 , then the ratio of coefficient of consolidation of sample $M$ to sample $\mathbf{N}$ (round off to three decimal places) is $\qquad$

## Q. 48

The hyetograph in the figure corresponds to a rainfall event of $\mathbf{3} \mathbf{~ c m}$.


If the rainfall event has produced a direct runoff of 1.6 cm , the $\phi$-index of the event (in mm/hour, round off to one decimal place) would be

Civil Engineering (CE, Set-2)

| Q.49 | A venturimeter as shown in the figure (not to scale) is connected to measure <br> the flow of water in a vertical pipe of 20 cm diameter. |
| :--- | :--- |
| Assume $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$. When the deflection in the mercury manometer is 15 <br> cm, the flow rate (in lps, round off to two decimal places) considering no loss <br> in the venturimeter is |  |

Q. 50 A reservoir with a live storage of $\mathbf{3 0 0}$ million cubic metre irrigates $\mathbf{4 0 0 0 0}$ hectares ( 1 hectare $=10^{4} \mathrm{~m}^{2}$ ) of a crop with two fillings of the reservoir. If the base period of the crop is $\mathbf{1 2 0}$ days, the duty for this crop (in hectares per cumec, round off to integer) will then be $\qquad$

Civil Engineering (CE, Set-2)

| Q. 51 | An activated sludge process (ASP) is designed for secondary treatment of $7500 \mathrm{~m}^{3} /$ day of municipal wastewater. After primary clarifier, the ultimate BOD of the influent, which enters into ASP reactor is $200 \mathrm{mg} / \mathrm{L}$. Treated effluent after secondary clarifier is required to have an ultimate BOD of 20 $\mathrm{mg} / \mathrm{L}$. Mix liquor volatile suspended solids (MLVSS) concentration in the reactor and the underflow is maintained as $3000 \mathrm{mg} / \mathrm{L}$ and $12000 \mathrm{mg} / \mathrm{L}$, respectively. The hydraulic retention time and mean cell residence time are 0.2 day and 10 days, respectively. A representative flow diagram of the ASP is shown below. |
| :---: | :---: |
|  |  |
|  | The underflow volume (in $\mathrm{m}^{3} / \mathrm{day}$, round off to one decimal place) of sludge wastage is $\qquad$ |

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| Q.52 | A grit chamber of rectangular cross-section is to be designed to remove <br> particles with diameter of 0.25 mm and specific gravity of 2.70 . The terminal <br> settling velocity of the particles is estimated as $2.5 \mathrm{~cm} / \mathrm{s}$. The chamber is <br> having a width of 0.50 m and has to carry a peak wastewater flow of 9720 <br> m $3 / \mathrm{d}$ giving the depth of flow as 0.75 m. If a flow-through velocity of $0.3 \mathrm{~m} / \mathrm{s}$ <br> has to be maintained using a proportional weir at the outlet end of the <br> chamber, the minimum length of the chamber (in m, in integer) to remove <br> 0.25 mm particles completely is |
| :--- | :--- |

Q. 53 In an aggregate mix, the proportions of coarse aggregate, fine aggregate and mineral filler are $55 \%, 40 \%$ and $5 \%$, respectively. The values of bulk specific gravity of the coarse aggregate, fine aggregate and mineral filler are $\mathbf{2 . 5 5}, 2.65$ and 2.70 , respectively. The bulk specific gravity of the aggregate mix (round off to two decimal places) is $\qquad$
Q. 54 The stopping sight distance (SSD) for a level highway is 140 m for the design speed of $90 \mathrm{~km} / \mathrm{h}$. The acceleration due to gravity and deceleration rate are $9.81 \mathrm{~m} / \mathrm{s}^{2}$ and $3.5 \mathrm{~m} / \mathrm{s}^{2}$, respectively. The perception/reaction time (in s , round off to two decimal places) used in the SSD calculation is $\qquad$
Q. 55 For a $2{ }^{\circ}$ curve on a high speed Broad Gauge (BG) rail section, the maximum sanctioned speed is $100 \mathrm{~km} / \mathrm{h}$ and the equilibrium speed is $80 \mathrm{~km} / \mathrm{h}$. Consider dynamic gauge of BG rail as 1750 mm . The degree of curve is defined as the angle subtended at its center by a 30.5 m arc. The cant deficiency for the curve (in mm , round off to integer) is $\qquad$

## END OF THE QUESTION PAPER

