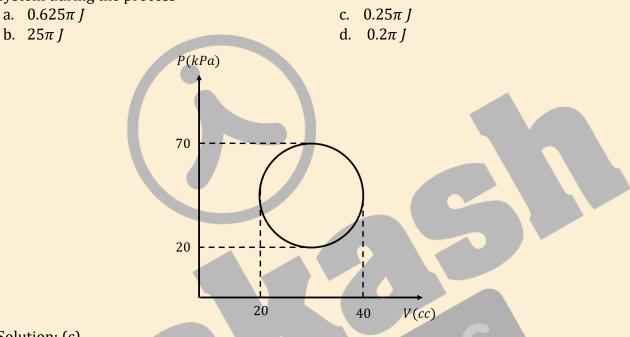
B

(Memory Based)

Date of Exam: 20th July 2021 Time: 9:00 a.m.-12 a.m. Subject: Physics

1. Consider the P-V diagram given below for a cyclic process. Find the net heat supplied to the system during the process



Solution: (c)

It is a cyclic process so the net change in internal energy of the system will zero. i.e.,

From first law of thermodynamics,

 $\Delta Q = \Delta U + \Delta W$

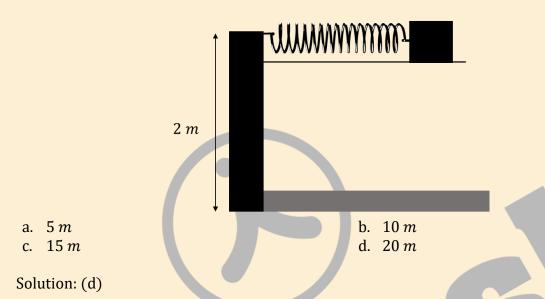
 $\Delta U = 0$

 $\Delta Q = 0 + \Delta W$ $\therefore \Delta Q = \Delta W$ Where, $\Delta W = \text{Area of the shaded portion,}$

$$=\pi \left[\frac{70-20}{2}\right] \times 10^{3} \times \left[\frac{40-20}{2}\right] \times 10^{-6}$$
$$=\pi [25] \times 10^{-3} \times 10$$
$$=0.25\pi J$$



2. A spring of force constant k = 100 N/m is compressed to x = 0.5 m by a block of mass 100 g and released. Find the distance d where it falls



Here, we can find the horizontal velocity v with which the block will leave the surface. So, using principle of conservation of energy we have,

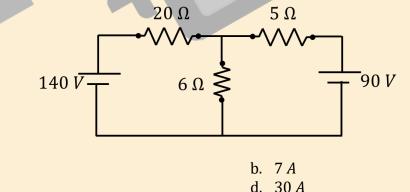
$$\frac{1}{2}kx^2 = \frac{1}{2}mv^2$$

 $\Rightarrow \frac{1}{2} \times 100 \times (5 \times 10^{-1})^2 = \frac{1}{2} \times 0.1 \times v^2$

$$\Rightarrow v = 5\sqrt{10} m/s$$

Now, the horizontal distance moved by the block is given by d = vt, where *t* is the time taken by the block to fall the distance 2 *m* Therefore, $d = 5\sqrt{10} \times \sqrt{(2h)/g}$ $\Rightarrow d = 5\sqrt{10} \times \sqrt{4/10} = 10 m$

3. In the given circuit, find the current through 6 Ω resistor



Solution: (a) Equivalent EMF of battery $EMF_{eq} = \frac{\frac{140}{20} + \frac{90}{5}}{\frac{1}{20} + \frac{1}{5}} = (7 + 18)4 = 100 V$ Internal Equivalent resistant of battery $\frac{1}{r_{eq}} = \frac{1}{20} + \frac{1}{5} = \frac{1}{4} \Rightarrow r_{eq} = 4 \Omega$ Equivalent resistance of the circuit $R_{eq} = 6 + 4 = 10 \Omega$ $\therefore i = \frac{100}{10} = 10 A$

- 4. Four moles of a diatomic gas is heated from 0°C to 50°C. Find the heat supplied to the gas if work done by it is zero.
 - a. 700 R
 - c. 500 R

Solution: (c)

Given number of moles of gas, n = 4Increase in temperature, $\Delta T = 50 K$

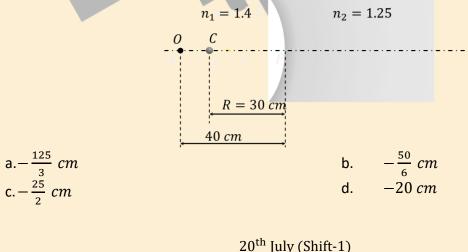
For the diatomic gas,

 $C_V = \frac{5R}{2}$

The work done by gas is zero that means the given thermodynamic process is an isochoric process.

$$Q = W + \Delta U$$
$$Q = \Delta U$$
$$Q = nC_V \Delta T = 4 \times \frac{5R}{2} \times 50 = 500R$$

5. For the spherical interface shown in the figure, the two different media with refractive indices $n_1 = 1.4$ and $n_2 = 1.25$ are present as shown. The image will be formed at





b. 600 Rd. 100 R

Solution:(a)

Given:

 $\Rightarrow \frac{1.25}{v} =$

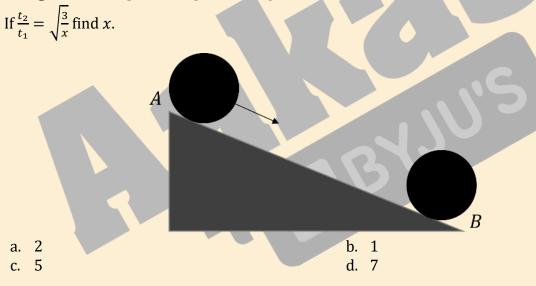
Position of the object (u) = -40 cm Refractive index of medium $1(n_1) = 1.4$ Refractive index of medium 2 $(n_2) = 1.25$ Radius of the interface (R) = -30 cm We know that for the spherical interface,

$$\frac{n_2}{v} - \frac{n_1}{u} = \frac{n_2 - n_1}{R}$$

$$\frac{1.25}{v} - \frac{1.4}{-40} = \frac{1.25 - 1.4}{(-30)}$$

$$\Rightarrow \frac{1.25}{v} = -\frac{1.25}{0.03} cm$$
Or, $v = -\frac{125}{3} cm$

6. When a disc slides on smooth inclined surface from rest, the time taken to move from A to B is t_1 . When disc performs pure rolling from rest then time taken to move from A to B is t_2 .



Solution:(a)

When disc slides $a_1 = g \sin \theta$ So, $S = ut_1 + \frac{1}{2}a_1t_1^2 = \frac{1}{2}g\sin\theta t_1^2$(1) When disc do pure rolling $a_2 = \frac{g \sin \theta}{1 + k^2/R^2} = \frac{g \sin \theta}{1 + 1/2} = \frac{2}{3}g \sin \theta$

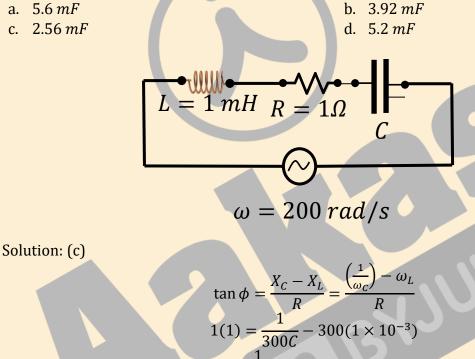


So, $S = ut_2 + \frac{1}{2}a_2t_2^2 = \frac{1}{2}x_3^2g\sin\theta t_2^2$ (2) From (1) & (2)

$$\frac{t_2}{t_1} = \sqrt{\frac{3}{2}}$$

So, *x* = 2

7. An AC circuit consists of a series combination of an inductance L 1 mH, a resistance R = 111 and a capacitance C. It is observed that the current leads the voltage by 45°. Find the value of capacitance 'C' if angular frequency of applied AC is 300 rad/s.



$$1(1) = \frac{1}{300C} - 300(1 \times 10^{-3})$$
$$\frac{1}{300C} = 1 + 0.3 = 1.3$$
$$= \frac{1}{300 \times 1.3} = 0.00256 F = 2.56 mF$$

8. An electron is projected into a magnetic field of $B = 5 \times 10^{-3}$ T and rotates in a circle of radius of R = 3 mm. Find the work done by the force due to magnetic field.

| a. | 0 J | b. | 15 mJ |
|----|-------|----|-------|
| c. | 14 mJ | d. | 20 mJ |

С

Solution: (a)

The work done by the force due to magnetic field is 0.



9. A charge *Q* is divided into *q* and (Q - q). If $\frac{Q}{q} = x$, such that the repulsion between them is maximum, find *x*.

| a. 1 | b. 2 |
|------|------|
| c. 3 | d. 4 |

Solution: (b)

As we know, $F = \frac{k(Q-q)q}{d^2}$ For F to be maximum,

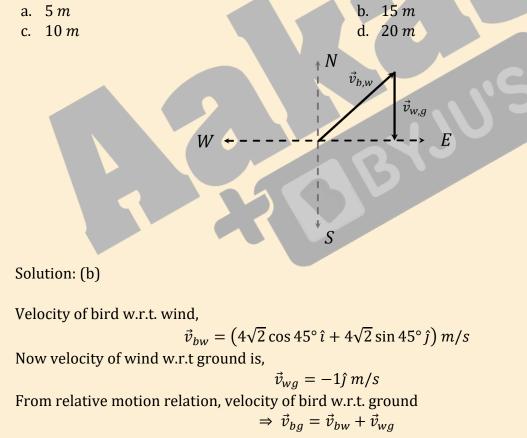
$$\frac{dF}{dq} = 0$$

$$\Rightarrow Q - 2q = 0$$

$$\Rightarrow \frac{Q}{q} = 2$$

$$\Rightarrow x = 2$$

10. Bird is flying in north-east direction with or $v = 4\sqrt{2} m/s$ with respect to the wind and the wind blowing from north to south with speed 1 m/s. Find the magnitude of the displacement of bird in 3 sec.





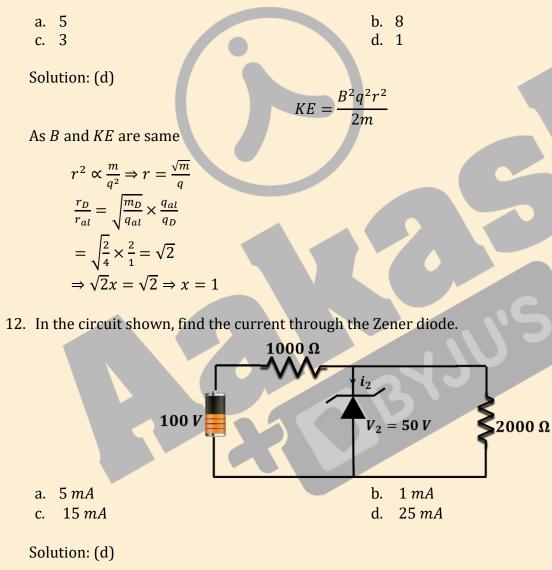
$$\vec{v}_{bg} = 4\hat{\imath} + 4\hat{\jmath} - 1\hat{\jmath} = 4\hat{\imath} + 3\hat{\jmath}$$
$$\left|\vec{v}_{bg}\right| = \sqrt{(3)^2 + (4)^2} = 5 \ m/s$$

Then displacement of bird in 3 sec,

$$\Rightarrow d = \left| \vec{v}_{bg} \right| \times t$$

or, $d = 5 \times 3 = 15 \text{ m/s}$

11. Deuteron and alpha particle having same *K*. *E*. in magnetic field. If the ratio of radius of Deuteron and alpha particle is $x\sqrt{2}$. Then x = ?



Since 2000 Ω is parallel to Zener diode So, the current passing through it as shown in the circuit,

$$i_3 = \frac{50}{2000} = 25 \ mA$$

20th July (Shift-1)

b. $\sqrt{A^2 + B^2 - \sqrt{2AB}}$ d. $\sqrt{A^2 + B^2 - \sqrt{2}AB}$



Potential difference across 1000 Ω, $V_1 = 100 - 50 = 50 V$ So, the electric current passing through it, $i_1 = \frac{50}{1000} = 50 mA$ So, current through Zener diode, $i_2 = 50 - 25 = 25 mA$ If $\vec{A} \cdot \vec{B} = \vec{A} \times \vec{B}$, find $|\vec{A} - \vec{B}|$

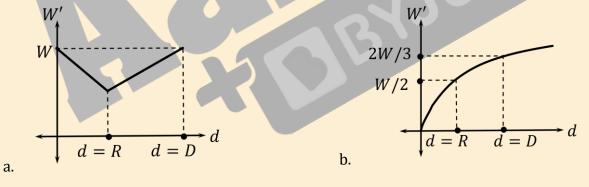
- 13. If $\vec{A} \cdot \vec{B} = \vec{A} \times \vec{B}$, find $|\vec{A} \vec{B}|$ a. A - B
 - c. A + B

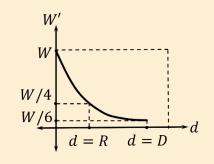
Solution: (d)

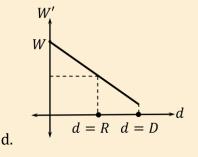
Since, $\vec{A} \cdot \vec{B} = \vec{A} \times \vec{B}$ $\Rightarrow |\vec{A}||\vec{B}| \cos\theta = |\vec{A}||\vec{B}| \sin\theta \Rightarrow$ Angle between the vectors, $\theta = 45^{\circ}$ Hence,

$$\left|\vec{A} - \vec{B}\right| = \sqrt{A^2 + B^2 - 2AB\cos\theta} = \sqrt{A^2 + B^2 - \sqrt{2}AB}$$

14. An object moves from earth's surface to the surface of the moon. The acceleration due to gravity on the earth's surface is $10 m/s^2$. Considering the acceleration due to gravity on the moon to be 1/6th times of that of earth. If *R* be the earth's radius and its weight be *W* and the distance between the earth and the moon is *D*. The correct variation of the weight *W*' versus distance *d* for a body when it moves from the earth to the moon is







C.

Solution: (c)

At the earth's surface the weight of body is, W = mgAt the moon the distance of body from the earth's is d = DAt moon's surface the value of acceleration due to gravity is $g' = \frac{g}{6}$

 $\Rightarrow W' = \frac{W}{6}$

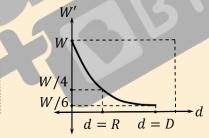
From the relation of acceleration due to gravity at height *d* above earth's surface,

$$g' = \frac{gR^2}{(R+d)^2} \dots (i)$$

For $d = 0$, $\Rightarrow g' = g$ or $W' = W$
At $d = R$,
 $\Rightarrow g' = \frac{gR^2}{4R^2} = \frac{g}{4}$
Or, $W' = \frac{mg}{4} = \frac{W}{4}$
At distance $d = D$, when the body reaches surface of moon
 $W' = \frac{mg}{6} = \frac{W}{6}$
Since Eq.(i) suggests that variation of g with distance(d) is non-linear, hence the graph of

W' vs d will be non-linear as well. Also $d \uparrow$, W' \downarrow

Thus the correct variation is represented by following graph



15. For an element decaying through simultaneous reaction, the half-life for respective decaying path is 1400 *s* and 700 *s*. Find the time taken when the number of atoms become $N_0/3$ in the element sample. (N_0 is initial number of atoms in sample)

a.
$$\frac{1400}{5} \ln 3$$

b. $\frac{1400}{3} \ln 3$
c. $\frac{1400}{3} \ln 2$
b. $\frac{1400}{3} \ln 3$
d. $\frac{700}{3} \ln 2$

20th July (Shift-1)



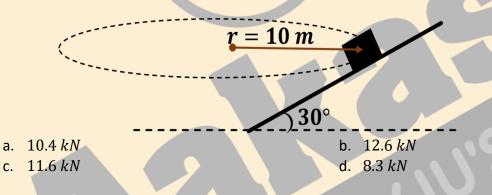
Solution: (b)

$$N = N_o e^{-\frac{t}{\tau}}$$
$$\frac{N_o}{3} = N_o e^{-\frac{t}{\tau}}$$

Taking natural log on both sides,

$$\ln\left(\frac{1}{3}\right) = \left(-\frac{t}{\tau}\right)\ln e$$
$$-\ln 3 = \left(-\frac{t}{\frac{1400}{3}}\right) \times 1$$
$$\therefore t = \frac{1400}{3}\ln 3$$

16. Consider a body of 800 kg moving with a maximum speed v on a road banked at $\theta = 30^{\circ}$, given $cos30^{\circ} = 0.87$. Find the normal reaction on the body. Coefficient of friction $\mu_s = 0.2$. [Take radius, r = 10 m]



Solution: (a)

Since the circular motion is such that $v = v_{max}$ the tendency of body is to move up the inclined plane

$$[f_s]_{max} = \mu_s N = 0.2 N$$

Resolving along X and Y axis, we have $N \cos 30^\circ = mg + [f_s]_{max} \sin 30^\circ$

$$\Rightarrow N[0.87] = 8000 + 0.2N \left[\frac{1}{2}\right]$$
$$N[0.87 - 0.1] = 8000$$
$$N = \frac{8000}{0.77} \approx 10,400 \text{ newton}$$



17. A spring with natural length l_0 has a tension T_1 when its length is l_1 and the tension is T_2 when its length is l_2 . The natural length of spring will be: b. $\frac{T_2 l_1 - T_1 l_2}{T_2 - T_1}$ d. $\frac{T_2 l_1 - T_1 l_2}{T_2 + T_1}$

a.
$$\frac{T_1 l_2 - T_2 l_1}{l_1 - l_2}$$

C.
$$\frac{T_1 - T_2}{T_1 - T_2}$$

Solution: (b)

-mmmmm--mmmmmm- $T_1 l_1$

all and a second second

Let the natural length be L₀

Using hook's law , $Y = \frac{TL}{AdL}$, where dL = L - L₀

Case 1 : when tension is T_1 length of wire = L_1

$$L_1 - L_0 = \frac{T_1 L_0}{4V} \dots (1)$$

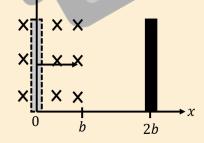
Case 2: Tension is T_2 and length of wire = L_2

L₂ - l₀ =
$$\frac{T_2}{4} \frac{l_0}{V}$$
.....(2)

Dividing both equations :

$$L_o = \frac{l_1 T_2 - l_2 T_1}{T_2 - T_1}$$

18. A conducting rod of length *l* is moving perpendicular to magnetic field. The rod moves from 0 to 2b while field exists only from 0 to b. Find the graph for emf and power dissipated w.r.t x.





Solution:

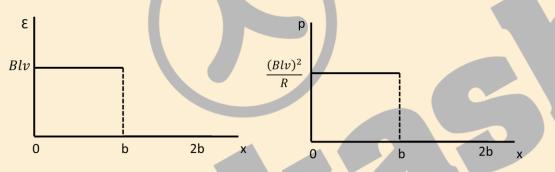
From the given figure it is clear that field exist from 0 to b only, therefore, the given conductor will experience field only from 0 to b. Here the given conductor is moving in a uniform magnetic field as long as field exist a constant $emf(\mathcal{E})$ will be induced in the conductor.

Induced emf in the conductor (\mathcal{E}) = Blv

due to this emf current developed in the conductor as, $i = \frac{e.m.f}{R} = \frac{Blv}{R}$

Power dissipation exists as long as emf exists in the conductor, $p = i^2 R = \frac{(Blv)^2}{R}$

Hence, the graph of E vs x and p vs x as follows,



19. A travelling wave is found to have the displacement by $y = \frac{1}{1+x^2}$ at t = 0, after 3 *sec* the wave pulse is represented by equation $y = \frac{1}{1+(1+x)^2}$. The velocity of wave is:

b. $\frac{1}{3} m/s$ d. $\frac{1}{4} m/s$

- a. 1*m/s*
- c. $\frac{2}{3} m/s$

Solution: (b)

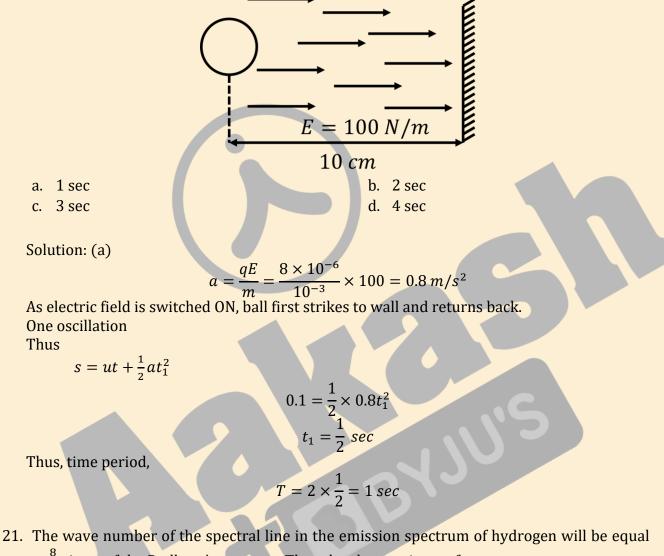
Displacement of wave, $\Delta x = 1 m$

$$\Rightarrow v \times t = 1$$
$$t = \frac{1}{v}$$
$$3 = \frac{1}{v}$$
$$v = \frac{1}{3} m/s$$

20th July (Shift-1)



20. A ball of charge to mass ratio $8 \mu C/g$ is placed at a distance of 10 cm from the ball. An electric field 100 N/m is switched on in the direction of wall. Find the time period of its oscillations. Assume all collisions elastic.



to $\frac{8}{9}$ times of the Rydberg's constant. Then the electron jumps from

a. $5 \rightarrow 2$ b. $5 \rightarrow 3$ c. $3 \rightarrow 1$ d. $4 \rightarrow 2$

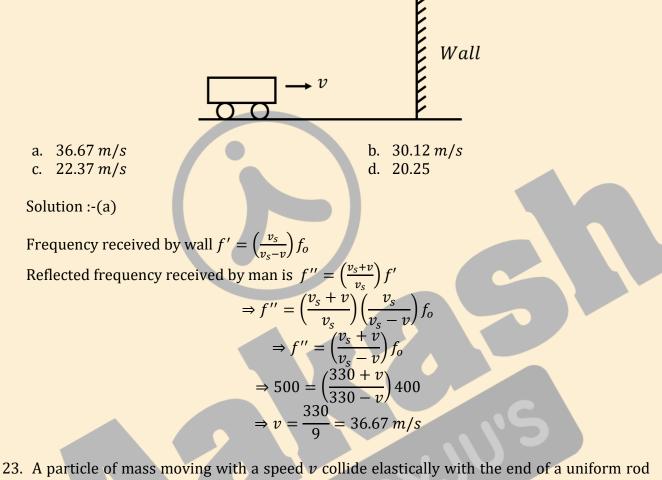
Solution: (c)

$$\bar{\nu} = Rz^2 \left(\frac{1}{n_L^2} - \frac{1}{n_H^2}\right)$$
$$\bar{\nu} = R.\,1^2 \left(\frac{1}{1^2} - \frac{1}{3^2}\right) = \frac{8}{9}R$$

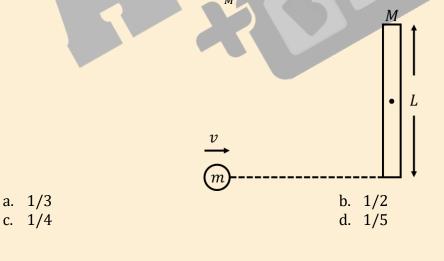
If $n_L = 1$, $n_H = 3$



22. A vehicle moving with velocity v and releasing sound of frequency 400 *Hz*. Listening the reflected sound from a wall of frequency 500 *Hz*. Find the velocity of vehicle v.

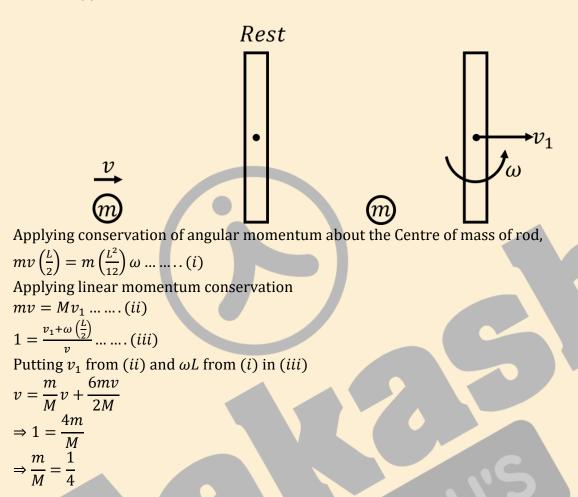


23. A particle of mass moving with a speed v collide elastically with the end of a uniform rod of mass M and length L perpendicularly as shown in the figure. If the particle comes to rest after collision, find the value of $\frac{m}{M}$.





Solution: (c)



24. Four planks are arranged in a lift going upwards with an acceleration of $0.2 m/s^2$ as shown in figure. Find the normal reaction applied by the lift on 10 kg block: $(g = 9.8 m/s^2)$

