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### 1. Evaluate:

- (i)  $\sin 18^{\circ}/\cos 72^{\circ}$
- (ii)  $\tan 26^{\circ}/\cot 64^{\circ}$
- (iii)  $\cos 48^{\circ} \sin 42^{\circ}$
- (iv)  $\csc 31^{\circ} \sec 59^{\circ}$

### Solution:

(i) sin 18°/cos 72°

To simplify this, convert the sin function into cos function

We know that,  $18^{\circ}$  is written as  $90^{\circ}$  -  $18^{\circ}$ , which is equal to the cos  $72^{\circ}$ .

 $= \sin (90^{\circ} - 18^{\circ}) / \cos 72^{\circ}$ 

Substitute the value, to simplify this equation

- $= \cos 72^{\circ} / \cos 72^{\circ} = 1$
- (ii)  $\tan 26^{\circ}/\cot 64^{\circ}$

To simplify this, convert the tan function into cot function

We know that,  $26^{\circ}$  is written as  $90^{\circ}$  -  $26^{\circ}$ , which is equal to the cot  $64^{\circ}$ .

 $= \tan (90^{\circ} - 26^{\circ})/\cot 64^{\circ}$ 

Substitute the value, to simplify this equation

- $= \cot 64^{\circ}/\cot 64^{\circ} = 1$
- (iii)  $\cos 48^{\circ} \sin 42^{\circ}$

To simplify this, convert the cos function into sin function

We know that,  $48^{\circ}$  is written as  $90^{\circ}$  -  $42^{\circ}$ , which is equal to the  $\sin 42^{\circ}$ .

 $= \cos (90^{\circ} - 42^{\circ}) - \sin 42^{\circ}$ 

Substitute the value, to simplify this equation

- $= \sin 42^{\circ} \sin 42^{\circ} = 0$
- (iv)  $\csc 31^{\circ} \sec 59^{\circ}$

To simplify this, convert the cosec function into sec function

We know that,  $31^{\circ}$  is written as  $90^{\circ}$  -  $59^{\circ}$ , which is equal to the sec  $59^{\circ}$ =

 $\csc (90^{\circ} - 59^{\circ}) - \sec 59^{\circ}$ 

Substitute the value, to simplify this equation

 $= \sec 59^{\circ} - \sec 59^{\circ} = 0$ 

## 2. Show that:

- (i)  $\tan 48^{\circ} \tan 23^{\circ} \tan 42^{\circ} \tan 67^{\circ} = 1$
- (ii)  $\cos 38^{\circ} \cos 52^{\circ} \sin 38^{\circ} \sin 52^{\circ} = 0$

Solution:

(i)  $\tan 48^{\circ} \tan 23^{\circ} \tan 42^{\circ} \tan 67^{\circ}$ 

Simplify the given problem by converting some of the tan functions to the cot functions

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We know that,  $\tan 48^\circ = \tan (90^\circ - 42^\circ) = \cot 42^\circ$ 

 $\tan 23^{\circ} = \tan (90^{\circ} - 67^{\circ}) = \cot 67^{\circ}$ 

 $= \tan (90^{\circ} - 42^{\circ}) \tan (90^{\circ} - 67^{\circ}) \tan 42^{\circ} \tan 67^{\circ}$ 

Substitute the values

 $= \cot 42^{\circ} \cot 67^{\circ} \tan 42^{\circ} \tan 67^{\circ}$ 

 $= (\cot 42^{\circ} \tan 42^{\circ}) (\cot 67^{\circ} \tan 67^{\circ}) = 1 \times 1 = 1$ 

(ii)  $\cos 38^{\circ} \cos 52^{\circ} - \sin 38^{\circ} \sin 52^{\circ}$ 

Simplify the given problem by converting some of the cos functions to the sin functions

We know that,

 $\cos 38^{\circ} = \cos (90^{\circ} - 52^{\circ}) = \sin 52^{\circ}$ 

 $\cos 52^{\circ} = \cos (90^{\circ} - 38^{\circ}) = \sin 38^{\circ}$ 

 $= \cos (90^{\circ} - 52^{\circ}) \cos (90^{\circ} - 38^{\circ}) - \sin 38^{\circ} \sin 52^{\circ}$ 

Substitute the values

 $= \sin 52^{\circ} \sin 38^{\circ} - \sin 38^{\circ} \sin 52^{\circ} = 0$ 

## 3. If $\tan 2A = \cot (A - 18^{\circ})$ , where 2A is an acute angle, find the value of A.

#### Solution:

 $\tan 2A = \cot (A-18^{\circ})$ 

We know that  $\tan 2A = \cot (90^{\circ} - 2A)$ 

Substitute the above equation in the given problem

$$\Rightarrow$$
 cot (90° - 2A) = cot (A -18°)

Now, equate the angles,

$$\Rightarrow 90^{\circ} - 2A = A - 18^{\circ} \Rightarrow 108^{\circ} = 3A$$

 $A = 108^{\circ} / 3$ 

Therefore, the value of  $A = 36^{\circ}$ 

## 4. If $\tan A = \cot B$ , prove that $A + B = 90^{\circ}$ .

#### Solution:

 $\tan A = \cot B$ 

We know that  $\cot B = \tan (90^{\circ} - B)$ 

To prove  $A + B = 90^{\circ}$ , substitute the above equation in the given problem

 $\tan A = \tan (90^{\circ} - B)$ 

 $A = 90^{\circ} - B$ 

 $A + B = 90^{\circ}$ 

Hence Proved.

# 5. If sec $4A = cosec (A - 20^{\circ})$ , where 4A is an acute angle, find the value of A.

Solution:

 $sec 4A = cosec (A - 20^{\circ})$ 

We know that  $\sec 4A = \csc (90^{\circ} - 4A)$ 

To find the value of A, substitute the above equation in the given problem (A - 200)

 $\csc (90^{\circ} - 4A) = \csc (A - 20^{\circ})$ 

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Now, equate the angles  $90^{\circ}$  - 4A= A-  $20^{\circ}$   $110^{\circ}$  = 5A

 $A = 110^{\circ}/5 = 22^{\circ}$ 

Therefore, the value of  $A = 22^{\circ}$ 

# 6. If A, B and C are interior angles of a triangle ABC, then show that

 $\sin (B+C/2) = \cos A/2$ 

Solution:

We know that, for a given triangle, sum of all the interior angles of a triangle is equal to 180°

$$A + B + C = 180^{\circ} \dots (1)$$

To find the value of (B+C)/2, simplify the equation (1)

 $\Rightarrow$  B + C = 180° - A

 $\Rightarrow$  (B+C)/2 = (180°-A)/2

 $\Rightarrow$  (B+C)/2 = (90°-A/2)

Now, multiply both sides by sin functions, we get

 $\Rightarrow$  sin (B+C)/2 = sin (90°-A/2)

Since  $\sin (90^{\circ}-A/2) = \cos A/2$ , the above equation is equal to

 $\sin (B+C)/2 = \cos A/2$ 

Hence proved.

# 7. Express $\sin 67^{\circ} + \cos 75^{\circ}$ in terms of trigonometric ratios of angles between $0^{\circ}$ and $45^{\circ}$ .

Solution:

Given:

 $\sin 67^{\circ} + \cos 75^{\circ}$ 

In term of sin as cos function and cos as sin function, it can be written as follows

 $\sin 67^{\circ} = \sin (90^{\circ} - 23^{\circ})$ 

 $\cos 75^{\circ} = \cos (90^{\circ} - 15^{\circ})$ 

So,  $\sin 67^{\circ} + \cos 75^{\circ} = \sin (90^{\circ} - 23^{\circ}) + \cos (90^{\circ} - 15^{\circ})$ 

Now, simplify the above equation

 $= \cos 23^{\circ} + \sin 15^{\circ}$ 

Therefore,  $\sin 67^{\circ} + \cos 75^{\circ}$  is also expressed as  $\cos 23^{\circ} + \sin 15^{\circ}$