

BYJU'S Study Planner for Board Term I (CBSE Grade 12)

Date: 09/11/2021

Subject: Mathematics

Topic : Relations and Functions

Class: Standard XII

1. Let A be a non-empty set such that $A \times A$ has 9 elements and $(-1, 0), (0, 1)$ are elements of $A \times A$, then $A =$
 - A. $\{-1, 0, 2\}$
 - B. $\{-1, 0, 1\}$
 - C. $\{-2, 0, 1\}$
 - D. Cannot be determined

2. Let \mathbb{N} denote the set of all natural numbers. Define two binary relations on \mathbb{N} as
$$R_1 = \{(x, y) \in \mathbb{N} \times \mathbb{N} : 2x + y = 10\}$$
 and
$$R_2 = \{(x, y) \in \mathbb{N} \times \mathbb{N} : x + 2y = 10\}.$$
 Then
 - A. Both R_1 and R_2 are transitive relations.
 - B. Range of R_2 is $\{1, 2, 3, 4\}$.
 - C. Range of R_1 is $\{2, 4, 8\}$.
 - D. Both R_1 and R_2 are symmetric relations.

3. If the function $f : B \rightarrow [-5, \infty)$ defined by $f(x) = x^2 - 4x + 5$ is one-one function, then B is
 - A. $[2, \infty)$
 - B. $[0, \infty)$
 - C. $[-5, \infty)$
 - D. $[-1, \infty)$

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4. Consider the set $A = \{1, 2, 3\}$ and the relation on A as $R = \{(1, 2), (1, 3)\}$, then R is
- A. a reflexive relation
 - B. a symmetric relation
 - C. a transitive relation
 - D. None of the above
5. The number of solution(s) of the equation $|x - 3| = x^3$ is
- A. 1
 - B. 0
 - C. 2
 - D. 3
6. Let $f(x) = \frac{x^2 - 1}{x}$, $g(x) = \frac{x + 2}{x - 3}$ then domain of $\frac{f(x)}{g(x)}$ is
- A. $\mathbb{R} - \{0, -2\}$
 - B. $\mathbb{R} - \{-2, 0, 3\}$
 - C. \mathbb{R}
 - D. $\mathbb{R} - \{0, -3\}$
7. The function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = |(x - 1)(x - 2)|$ is
- A. One-one function
 - B. Many-one function
 - C. Constant function
 - D. None of these

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8. Let $A = \{1, 2, 3\}$ and R, S be two relations on A given by
 $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 1)\}$, $S = \{(1, 1), (2, 2), (3, 3), (2, 3), (3, 2)\}$
 then $R \cup S$ is
- A. Reflexive, symmetric and transitive relation
 - B. reflexive and transitive relation only
 - C. not a transitive relation
 - D. Reflexive relation but not Symmetric relation
9. Let $f(x) = (1 + b^2)x^2 + 2bx + 1$ and let $m(b)$ be the minimum value of $f(x)$.
 As b varies, the range of $m(b)$ is
- A. $[0, 1]$
 - B. $\left[0, \frac{1}{2}\right]$
 - C. $\left[\frac{1}{2}, 1\right]$
 - D. $(0, 1]$
10. The domain of $f(x) = \sqrt{\frac{4 - x^2}{[x] + 2}}$ is
 (where $[.]$ represents the greatest integer function)
- A. $(-\infty, 1)$
 - B. $(-\infty, -2) \cup [-1, 2]$
 - C. $(-\infty, -1) \cup [2, \infty)$
 - D. $(-\infty, 1) \cup [2, \infty)$

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11. Let the function $f : \mathbb{R} - \{-b\} \rightarrow \mathbb{R} - \{1\}$ be defined by $f(x) = \frac{x+a}{x+b}, a \neq b$, then
- f is one-one but not onto function
 - f is onto but not one-one function
 - f is bijective function
 - f is neither one-one nor onto function
12. If relation R is defined as aRb if " a is the father of b ". Then R is
- reflexive
 - symmetric
 - transitive
 - none of these
13. Let \mathbb{N} denote the set of natural numbers and R be a relation on $\mathbb{N} \times \mathbb{N}$ defined by $(a, b)R(c, d) \iff ad(b+c) = bc(a+d)$. Then on $\mathbb{N} \times \mathbb{N}$, R is
- An equivalence relation
 - Reflexive and symmetric relation only
 - Transitive relation only
 - Symmetric and transitive relation only

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14. Let a relation f defined on $(0, \infty)$ as $f(x) = \left|1 - \frac{1}{x}\right|$. Then which among the following is true

- A. $f(-1) = 2$
- B. f is many-one function
- C. f is one-one function
- D. Relation f is not a function

15. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = \frac{(e^x - e^{-x})}{2}$.

The inverse of the given function is:

- A. $f^{-1}(x) = \log_e(x + \sqrt{x^2 + 1})$
- B. $f^{-1}(x) = \log_e(x - \sqrt{x^2 + 1})$
- C. $f^{-1}(x) = \log_e(x + \sqrt{x^2 - 1})$
- D. $f^{-1}(x) = \log_e(x - \sqrt{x^2 - 1})$

16. Which among the following relations on \mathbb{Z} is an equivalence relation

- A. $xRy \Leftrightarrow |x| = |y|$
- B. $xRy \Leftrightarrow x \geq y$
- C. $xRy \Leftrightarrow x > y$
- D. $xRy \Leftrightarrow x < y$

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17. Let S be the set of all triangles and R^+ be the set of all positive real numbers. If the relation f defined from S to R^+ such that $f(\triangle) = \text{area of triangle}$, $\triangle \in S$, then which of the following is true about relation f
- f is not a function
 - relation f is a many-one function
 - If $\triangle_1 \cong \triangle_2$, then $f(\triangle_1) \neq f(\triangle_2)$
 - None of the above
18. If a relation R is defined on set of real numbers as $xRy \iff x - y + \sqrt{2}$ is an irrational number, then the relation R is
- a reflexive relation
 - a symmetric relation
 - a transitive relation
 - both reflexive and transitive relation
19. Consider the functions $f(x) = \begin{cases} x + 1, & x \leq 1 \\ 2x + 1, & 1 < x \leq 2 \end{cases}$
- $$g(x) = \begin{cases} x^2, & -1 \leq x < 2 \\ x + 2, & 2 \leq x \leq 3 \end{cases}$$
- Domain of $f(g(x))$ is
- $[0, \sqrt{2}]$
 - $[-1, 2]$
 - $[-1, \sqrt{2}]$
 - $[\sqrt{2}, \sqrt{2}]$

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20. Consider the functions $f(x) = \begin{cases} x+1, & x \leq 1 \\ 2x+1, & 1 < x \leq 2 \end{cases}$

$$g(x) = \begin{cases} x^2, & -1 \leq x < 2 \\ x+2, & 2 \leq x \leq 3 \end{cases}$$

Range of the function $f(g(x))$ is

- A.** $[1, 5]$
- B.** $[2, 3]$
- C.** $[1, 2] \cup (3, 5]$
- D.** $[1, 5] - \{3\}$