Page: 159



Exercise 9.2

1. In Fig. 9.15, ABCD is a parallelogram, AE \perp DC and CF \perp AD. If AB = 16 cm, AE = 8 cm and CF = 10 cm, find AD.

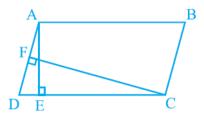


Fig. 9.15

Solution:

Given,

AB = CD = 16 cm (Opposite sides of a parallelogram)

CF = 10 cm and AE = 8 cm

Now.

Area of parallelogram = Base \times Altitude

 $= CD \times AE = AD \times CF$

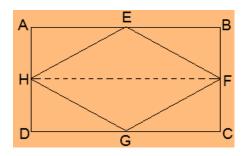
 $\Rightarrow 16 \times 8 = AD \times 10$

 \Rightarrow AD = 128/10 cm

 \Rightarrow AD = 12.8 cm

2. If E, F, G and H are respectively the mid-points of the sides of a parallelogram ABCD, show that ar (EFGH) = 1/2 ar(ABCD).

Solution:



Given,

E, F, G and H are the mid-points of the sides of a parallelogram ABCD respectively.

To Prove,

 $ar (EFGH) = \frac{1}{2} ar(ABCD)$

Construction,

H and F are joined.

Proof,

 $AD \parallel BC$ and AD = BC (Opposite sides of a parallelogram)

 $\Rightarrow \frac{1}{2} AD = \frac{1}{2} BC$

Also,

AH || BF and and DH || CF

 \Rightarrow AH = BF and DH = CF (H and F are mid points)

:, ABFH and HFCD are parallelograms.

Now,

NCERT Solution For Class 9 Maths Chapter 9- Areas Of Parallelograms And Triangles

We know that, \triangle EFH and parallelogram ABFH, both lie on the same FH the common base and in-between the same parallel lines AB and HF.

 \therefore area of EFH = $\frac{1}{2}$ area of ABFH --- (i)

And, area of GHF = $\frac{1}{2}$ area of HFCD --- (ii)

Adding (i) and (ii),

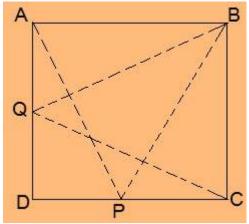
area of Δ EFH + area of Δ GHF = $\frac{1}{2}$ area of ABFH + $\frac{1}{2}$ area of HFCD

⇒ area of EFGH = area of ABFH

 \therefore ar (EFGH) = $\frac{1}{2}$ ar(ABCD)

3. P and Q are any two points lying on the sides DC and AD respectively of a parallelogram ABCD. Show that ar(APB) = ar(BQC).

Solution:



 \triangle APB and parallelogram ABCD lie on the same base AB and in-between same parallel AB and DC.

 $ar(\Delta APB) = \frac{1}{2} ar(parallelogram ABCD) --- (i)$ Similarly, $ar(\Delta BQC) = \frac{1}{2} ar(parallelogram ABCD) --- (ii)$ From (i) and (ii), we have

 $ar(\Delta APB) = ar(\Delta BQC)$

- 4. In Fig. 9.16, P is a point in the interior of a parallelogram ABCD. Show that
 - $ar(APB) + ar(PCD) = \frac{1}{2} ar(ABCD)$
 - (ii) ar(APD) + ar(PBC) = ar(APB) + ar(PCD)

[Hint: Through P, draw a line parallel to AB.]

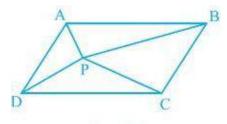
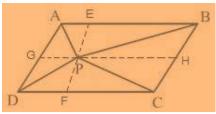


Fig. 9.16

Solution:



(i) A line GH is drawn parallel to AB passing through P.

In a parallelogram,

∴,

$$AD \parallel BC \Rightarrow AG \parallel BH --- (ii)$$

From equations (i) and (ii),

ABHG is a parallelogram.

Now,

 Δ APB and parallelogram ABHG are lying on the same base AB and in-between the same parallel lines AB and GH.

$$\therefore ar(\Delta APB) = \frac{1}{2} ar(ABHG) --- (iii)$$

also,

 Δ PCD and parallelogram CDGH are lying on the same base CD and in-between the same parallel lines CD and GH.

$$\therefore$$
 ar(\triangle PCD) = $\frac{1}{2}$ ar(CDGH) --- (iv)

Adding equations (iii) and (iv),

$$ar(\Delta APB) + ar(\Delta PCD) = \frac{1}{2} [ar(ABHG) + ar(CDGH)]$$

$$\Rightarrow$$
 ar(APB)+ ar(PCD) = $\frac{1}{2}$ ar(ABCD)

(ii) A line EF is drawn parallel to AD passing through P.

In the parallelogram,

∴,

$$AB \parallel CD \Rightarrow AE \parallel DF --- (ii)$$

From equations (i) and (ii),

AEDF is a parallelogram.

Now,

 Δ APD and parallelogram AEFD are lying on the same base AD and in-between the same parallel lines AD and EF.

$$\therefore$$
ar(\triangle APD) = $\frac{1}{2}$ ar(AEFD) --- (iii)

also,

 ΔPBC and parallelogram BCFE are lying on the same base BC and in-between the same parallel lines BC and EF.

$$\therefore$$
ar(\triangle PBC) = $\frac{1}{2}$ ar(BCFE) --- (iv)

Adding equations (iii) and (iv),

$$ar(\Delta APD) + ar(\Delta PBC) = \frac{1}{2} \{ar(AEFD) + ar(BCFE)\}$$

$$\Rightarrow$$
ar(APD)+ar(PBC) = ar(APB)+ar(PCD)

5. In Fig. 9.17, PQRS and ABRS are parallelograms and X is any point on side BR. Show that ar (PQRS) = ar (ABRS)

$$ar(AXS) = \frac{1}{2}ar(PQRS)$$

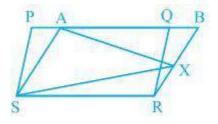


Fig. 9.17

Solution:

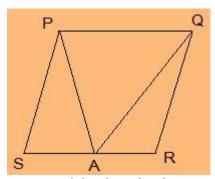
- (i) Parallelogram PQRS and ABRS lie on the same base SR and in-between the same parallel lines SR and PB.
 - \therefore ar(PQRS) = ar(ABRS) --- (i)
- (ii) ΔAXS and parallelogram ABRS are lying on the same base AS and in-between the same parallel lines AS and BR.
 - $\therefore ar(\Delta AXS) = \frac{1}{2} ar(ABRS) --- (ii)$

From (i) and (ii), we find that,

 $ar(\Delta AXS) = \frac{1}{2} ar(PQRS)$

6. A farmer was having a field in the form of a parallelogram PQRS. She took any point A on RS and joined it to points P and Q. In how many parts the fields is divided? What are the shapes of these parts? The farmer wants to sow wheat and pulses in equal portions of the field separately. How should she do it?

Solution:



The field is divided into three parts each in triangular shape.

Let, Δ PSA, Δ PAQ and Δ QAR be the triangles.

Area of
$$\triangle PSA + \triangle PAQ + \triangle QAR = Area of PQRS --- (i)$$

Area of $\triangle PAQ = \frac{1}{2}$ area of PQRS --- (ii)

Here, the triangle and parallelogram are on the same base and in-between the same parallel lines. From (i) and (ii),

Area of $\triangle PSA + Area$ of $\triangle QAR = \frac{1}{2}$ area of PQRS --- (iii)

From (ii) and (iii), we can conclude that,

The farmer must sow wheat or pulses in ΔPAQ or either in both ΔPSA and ΔQAR .