

## CAT 2020 Question Paper with Solution Slot 1 QA

1. If  $\log_4 5 = (\log_4 y)(\log_6 \sqrt{5})$ , then  $y$  equals \_\_\_\_.

**Answer:** 36

**Solution:**

$$\log_4 5 = (\log_4 y)(\log_6 \sqrt{5})$$

$$\Rightarrow \frac{\log 5}{\square\square\square 4} = \frac{\square\square\square \square}{\square\square\square 4} \times \frac{\square\square\square \left(5^{\frac{1}{2}}\right)}{\square\square\square 6}$$

$$\Rightarrow \frac{\log 5 \times \log 6}{\frac{1}{2} \log 5} = \log y$$

$$\Rightarrow 2 \log 6 = \log y$$

$$\Rightarrow \log 6^2 = \log y$$

$$\Rightarrow y = 36$$

###TOPIC###Quantitative Aptitude||Algebra||Logarithm###

2. An alloy is prepared by mixing three metals A, B, and C in the proportion 3:4:7 by volume. The weights of the same volume of the metals A, B, and C are in the ratio 5:2:6. In 130 kg of the alloy, the weight (in kg) of the metal C is \_\_\_\_\_.

- A. 96 kg
- B. 84 kg
- C. 70 kg
- D. 48 kg

**Answer:** B

**Solution:**

Ratio of volumes of A, B, C in the Alloy = 3:4:7

Ratio of weights of the same volumes or density of A, B, and C = 5:2:6

Ratio of weights of A, B, and C in the alloy =  $3 \times 5 : 4 \times 2 : 7 \times 6 = 15:8:42$

	Volume	Density	Weight
A	3	5	15
B	4	2	8
C	7	6	42
Overall	14	65/14	65

Total weight of alloy = 130 kg

$$\text{Weight of metal C} = \frac{42}{15+8+42} \times 130 = 84 \text{ kg}$$

###TOPIC###Quantitative Aptitude||Arithmetic||Ratio and Proportion###

3. Leaving home at the same time, Amal reaches his office at 10:15 a.m. if he travels at 8 km/h, and at 9:40 am if he travels at 15 km/h. Leaving home at 9:10 a.m., at what speed (in km/h) must he travel so as to reach office exactly at 10 a.m.?

A. 13

B. 14

C. 11

D. 12

**Answer:** D

**Solution:**

Let the distance between home and office be  $d$  km.

According to the question, we can write the following:

$$\frac{d}{8} - \frac{d}{15} = \frac{35}{60}$$

$$\Rightarrow \frac{7d}{120} = \frac{35}{60}$$

$$\Rightarrow d = 10 \text{ km}$$

Now he should reach the office in 50 min.

$$d = 10 \text{ km}$$

$$t = 50 \text{ min} = \frac{5}{6} \text{ h}$$

$$\text{Required speed} = \frac{10}{5/6} = 12 \text{ km/hr}$$

###TOPIC###Quantitative Aptitude||Arithmetic||Speed, Time and Distance###

4. Let A, B, and C be three positive integers such that the sum of A and the mean of B and C is 5. In addition, the sum of B and the mean of A and C is 7. Then, the sum of A and B is \_\_\_\_\_.

- A. 1.4
- B. 2.5
- C. 3.7
- D. 4.6

**Answer:** D

**Solution:**

The given equations are the following:

$$A + \frac{B+C}{2} = 5 \quad \Rightarrow 2A + B + C = 10 \quad \text{..... (1)}$$

$$B + \frac{A+C}{2} = 7 \quad \Rightarrow A + 2B + C = 14 \quad \text{..... (2)}$$

Subtracting equation (1) from equation (2), we get the following:

$$B - A = 4 \quad \text{.....(3)}$$

Putting  $A = 1$ , we will get  $B = 5$ ; this is the minimum value of B.

If  $A = C = 1$ , then, from (1), we will get  $B = 6 = \text{max value of B}$

But for  $A = 1$ , we were already getting  $B = 5$ .

Hence,  $A = C = 1$  is not possible.

$$\Rightarrow 2A + B + C = 10$$

From this, by putting  $A = 1$  and  $B = 5$ , we get  $C = 3$

So, the only possible solution is  $A = 1$ ,  $B = 5$ , and  $C = 3$ .

$$\therefore A + B = 6$$

###TOPIC###Quantitative Aptitude||Arithmetic||Averages###

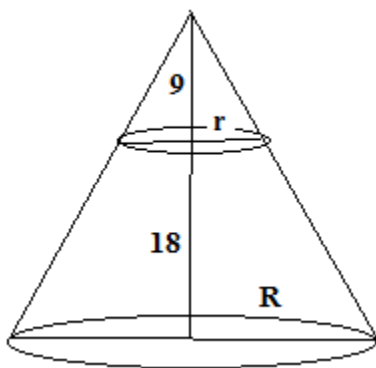


5. A solid right circular cone of height 27 cm is cut into two pieces parallel to its base at a height of 18 cm from the base. If the difference in volume of the two pieces is 225 cc, the volume, in cc, of the original cone is \_\_\_\_\_.

- A. 256
- B. 232
- C. 264
- D. 243

**Answer:** D

**Solution:**



Height of original cone = 27 cm

Height of smaller cone =  $27 - 18 = 9$  cm

Ratio of height of original cone and smaller cone =  $27:9 = 3:1$

Using the similarity of triangles, we get the following:

The ratio of the radius of original cone to that of the smaller cone is  $\frac{R}{r} = \frac{3}{1}$

Ratio of volumes =  $\left(\frac{3}{1}\right)^3 = \frac{27}{1} = 27:1$

Let the volume of the original cone be  $27k$ .

And the volume of the smaller cone =  $k$

Volume of frustum =  $(27 - 1)k = 26k$

Given,

$$26k - k = 225$$

$$25k = 225 = 9 \times 25$$

$$\Rightarrow k = 9$$

$$\therefore \text{Volume of original cone} = 27k = 27 \times 9 = 243 \text{ cc}$$

###TOPIC###Quantitative Aptitude||Mensuration||Mensuration###



6. Two persons are walking beside a railway track at respective speeds of 2 and 4 km per hour in the same direction. A train came from behind them and crossed them in 90 and 100 seconds, respectively. The time, in seconds, taken by the train to cross an electric post is nearest to \_\_\_\_.

A. 78

B. 82

C. 87

D. 75

**Answer:** B

**Solution:**

Let the length of the train be  $x$  metres and the speed of the train be  $s$  km/h.

As they are moving in the same direction, relative speed between the train and the first person =  $(s - 2)$  km/h

Similarly, relative speed between the train and the second person =  $(s - 4)$  km/h  
[because they are moving in the same direction]

Since the distance (length of train) is same in both the cases, we can write the following:

$$x_1 \times t_1 = x_2 \times t_2$$

$$\frac{s_1}{s_2} = \frac{t_2}{t_1}$$

Substituting these values, we get:

$$\Rightarrow \frac{s-2}{s-4} = \frac{100}{90}$$

$$\Rightarrow s = 22 \text{ km/hr}$$

Let the time taken by the train to cross an electric post be ' $t$ '.

We can write the following:

$$\Rightarrow \frac{s-2}{s} = \frac{t}{90}$$

$$\Rightarrow \frac{20}{22} = \frac{t}{90}$$



$\Rightarrow t \approx 82 \text{ sec}$

###TOPIC###Quantitative Aptitude||Arithmetic||Speed, Time and Distance###



7. A gentleman decided to treat a few children in the following manner. He gives half of his total stock of toffees and one extra to the first child, and then the half of the remaining stock along with one extra to the second and continues giving away in this fashion. His total stock exhausts after he takes care of 5 children. How many toffees were there in his stock initially?

**Answer:** 62

**Solution:**

We can solve this question by reverse calculations as stated in the table below:

After child number	Number of toffees
5	0
4	$2(0 + 1) = 2$
3	$2(2 + 1) = 6$
2	$2(6 + 1) = 14$
1	$2(14 + 1) = 30$
0	$2(30 + 1) = 62$

###TOPIC###Quantitative Aptitude||Number System||Properties of Numbers###

8. If  $a$ ,  $b$ , and  $c$  are positive integers such that  $ab = 432$ ,  $bc = 96$ , and  $c < 9$ , then the smallest possible value of  $a + b + c$  is \_\_\_\_\_.

A. 46

B. 59

C. 49

D. 56

**Answer: A**

**Solution:**

It is given that,

$$ab = 432, \quad bc = 96$$

Since  $a$ ,  $b$ ,  $c$  are positive integers and  $c < 9$ , we can get  $c$  as 8 or 6 or 4 or 3 or 2 or 1.

We can calculate the possible values of  $a$ ,  $b$ , and  $c$  as shown:

Case	A	B	C
1	4.5	96	1
2	9	48	2
3	13.5	32	3
4	18	24	4
5	27	16	6
6	36	12	8

Since all values should be integers, we can say that the cases 1 and 3 are to be ignored.

Hence,

Case	A	B	C	$a + b + c$
1	9	48	2	59
2	18	24	4	46
3	27	16	6	49
4	36	12	8	56

So, the minimum value of  $(a + b + c)$  is 46.

###TOPIC###Quantitative Aptitude||Number System||Properties of Numbers###



9. Among 100 students,  $x_1$  have birthdays in January,  $x_2$  have birthdays in February, and so on. If  $x_0 = \max(x_1, x_2, \dots, x_{12})$ , then the smallest possible value of  $x_0$  is \_\_\_\_.

- A. 10
- B. 9
- C. 12
- D. 8

**Answer:** B

**Solution:**

For the smallest possible value of  $x_0$ , all  $(x_1, x_2, x_3, \dots, x_{12})$  should be equal or closest to each other.

If we make all the values to be 8, we will have 4 left. Those 4 can be distributed 1 each.

So, the maximum value will be 9.

###TOPIC###Quantitative Aptitude||Number System||Properties of Numbers###



10. The mean of all 4-digit even natural numbers of the form 'aabb', where  $a > 0$ , is \_\_\_\_\_.

- A. 4466
- B. 4864
- C. 5050
- D. 5544

**Answer:** D

**Solution:**

The number 'aabb' means  $1000a + 100a + 10b + b = 11(100a + b)$ .

Now, a can be 1,2,3...9 and b can be 0, 2, 4, 6, 8.

So, we can form the following table :

The first row represents the values of 'b' and the first column represents the values of 'a'

	0	2	4	6	8	TOTAL
1	1100	1122	1144	1166	1188	5720
2	2200	2222	2244	2266	2288	11220
3	3300	3322	3344	3366	3388	16720
4	4400	4422	4444	4466	4488	22220
5	5500	5522	5544	5566	5588	27720
6	6600	6622	6644	6666	6688	33220
7	7700	7722	7744	7766	7788	38720
8	8800	8822	8844	8866	8888	44220
9	9900	9922	9944	9966	9988	49720
						249480

We can see that there are 5 values of 'b' and 9 values of 'a'.

Hence, there are 45 values in total.

So, average =  $\text{sum}/45 = 249480/45 = 5544$ .

Alternative solution by tabulating the values:

The numbers satisfying the given conditions are the following:

1100, 1122, 1144, 1166, 1188

2200, 2222, 2244, 2266, 2288

.....

.....

9900, 9922, 9944, 9966, 9988

We can notice that the numbers in each row are in AP.

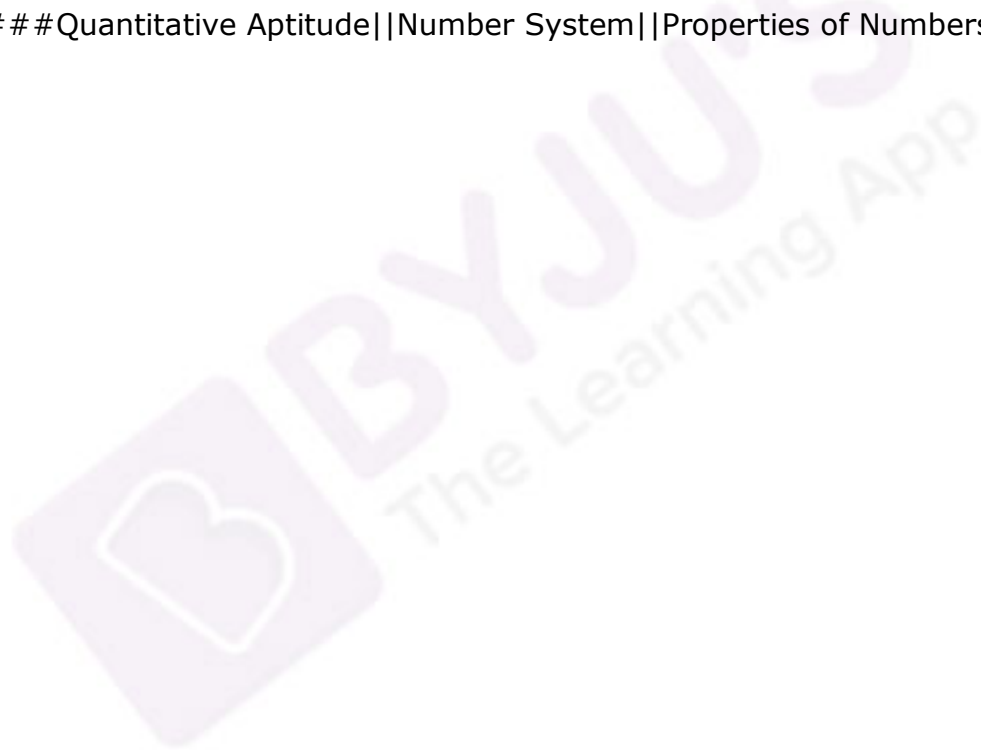
So, the middle number of each row will be the mean of that row.

So, the mean of the rows are 1144, 2244, 3344, 4444, 5544, 6644, 7744, 8844, and 9944.

Now the mean of these numbers is 5544.

Hence, the mean of all 4-digit even natural numbers of the form 'aabb' is 5544.

###TOPIC###Quantitative Aptitude||Number System||Properties of Numbers###





11. The number of real valued solutions of the equation  $2^x + 2^{-x} = 2 - (x - 2)^2$  is \_\_\_\_.

- A. 1
- B. 0
- C. Infinite
- D. 2

**Answer:** B

**Solution:**

Given,

$$2^x + 2^{-x} = 2 - (x - 2)^2$$

$2^x > 0$  for all real values of  $x$ .

We know that, for all positive values 'P',  $\square + \frac{1}{\square} \geq 2$  and the equality occurs at  $P = 1$ .

$$\therefore 2^x + 2^{-x} \geq 2 \dots\dots\dots(1)$$

Now, since the square of any real quantity can be at least zero, we can write the following:

$$(\square - 2)^2 \geq 0$$

$$\Rightarrow 2 - (x - 2)^2 \leq 2$$

Now, the only possible solution is when both the LHS and RHS are equal to 2 simultaneously.

$$2^x + 2^{-x} = 2 \text{ or } x = 0$$

$$\text{And } 2 - (x - 2)^2 = 2 \text{ or } x = 2$$

So, there is no common value of  $x$  for which  $\text{LHS} = \text{RHS}$ .

Hence, the given equation does not have a solution.

###TOPIC###Quantitative Aptitude||Algebra||Quadratic Equations###

12. How many distinct positive integer valued solutions exist to the equation

$$(x^2 - 7x + 11)^{(x^2 - 13x + 42)} = 1?$$

A. 8

B. 2

C. 4

D. 6

**Answer:** D

**Solution:**

$(x^2 - 7x + 11)^{(x^2 - 13x + 42)} = 1$  in the following cases:

Case	$x^2 - 7x + 11$	$x^2 - 13x + 42$	Value/s of x
1	1	Immaterial	5 or 2
2	Non zero	0	6 or 7
3	(-1)	Even	3 or 4

So, there are SIX possible values of x.

###TOPIC###Quantitative Aptitude||Algebra||Quadratic Equations###

13. In a group of people, 28% of the members are young, while the rest are old. If 65% of the members are literates, and 25% of the literates are young, then the percentage of old people among the illiterates is nearest to \_\_\_\_.

- A. 66
- B. 59
- C. 62
- D. 55

**Answer:** A

**Solution:**

From the given data:

	Young	Old	Total
Literates	16.25	48.75	65
Illiterates	11.75	23.25	35
Total	28	72	100

We have filled in the values from the given data.

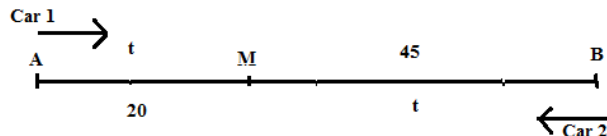
So, the required percentage =  $23.25/35 \times 100\% = 66\%$  ( approx.)

14. A straight road connects points A and B. Car 1 travels from A to B and Car 2 travels from B to A, both leaving at the same time. After meeting each other, they take 45 minutes and 20 minutes, respectively, to complete their journey. If Car 1 travels at the speed of 60 km/h, then the speed of Car 2, in km/hr, is \_\_\_\_.

- A. 100
- B. 80
- C. 90
- D. 70

**Answer:** C

**Solution:**



Let the two cars meet at point M and the time they take to meet is 't' min.

Also, assume the speed of Car 1 to be  $S_1$  and that of Car 2 to be  $S_2$ . [in suitable units]

Time taken by Car 1 to travel from A to M = t min

Time taken by Car 2 to travel from M to A = 20 min

Since distance is same in both cases, we can write the following:

$$\frac{S_1}{S_2} = \frac{20}{t} \dots\dots\dots(1)$$

Similarly, we can write the following:

Time taken by Car 1 to travel from M to B = 45 min

Time taken by Car 2 to travel from B to M = t min

Since distance is same in both the cases, we can write the following:

$$\frac{S_1}{S_2} = \frac{t}{45} \dots\dots\dots(2)$$

From (1) and (2), we get the following:

$$\frac{20}{t} = \frac{t}{45} \quad \Rightarrow t = 30 \text{ min}$$

Putting  $t = 30$  and  $S_1 = 60$  in the first equation, we get the following:

$$\frac{60}{S_2} = \frac{20}{30} \quad \Rightarrow S_2 = 90 \text{ km / hr}$$

###TOPIC###Quantitative Aptitude||Arithmetic||Speed, Time and Distance###

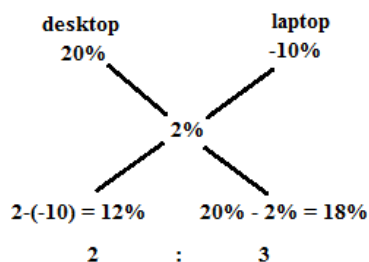


15. A person spent Rs. 50000 to purchase a desktop computer and a laptop computer. He sold the desktop at 20% profit and the laptop at 10% loss. If he made a 2% profit overall, then the purchase price, in rupees, of the desktop is \_\_\_\_\_.

**Answer:** 20000

**Solution:**

Using allegations, we can find the ratio of the cost prices of the two articles.



Desktop:Laptop = 2:3

Cost price of desktop =  $\frac{2}{2+3} \times 50000 = \text{Rs. } 20000$

###TOPIC###Quantitative Aptitude||Arithmetic||Profit, Loss and Discount###

16. If  $f(5 + x) = f(5 - x)$  for every real  $x$ , and  $f(x) = 0$  has four distinct real roots, then the sum of these roots is \_\_\_\_\_.

- A. 20
- B. 0
- C. 40
- D. 10

**Answer:** A

**Solution:**

Given,

$$f(5 + x) = f(5 - x)$$

$$\text{Let } x = 5 - y$$

Putting this value, we get the following:

$$f(10 - y) = f(y) \dots\dots\dots(1)$$

Now let  $a$  and  $b$  be two of the four roots of  $f(X) = 0$ .

$$\Rightarrow f(a) = f(b) = 0$$

Substituting  $y = a$  in equation (1), we get the following:

$$f(10 - a) = f(a) = 0$$

This means  $10 - a$  is the root of the given equation.

Similarly, if  $b$  is a root, then  $(10 - b)$  is also a root of the given equation.

Hence, the four roots of the given equation are  $a, b, 10 - a$ , and  $10 - b$ .

$$\text{Sum of roots} = a + b + 10 - a + 10 - b = 20.$$

###TOPIC###Quantitative Aptitude||Functions and Graphs||Functions and Graphs###

17. Veeru invested Rs. 10000 at 5% simple annual interest, and exactly after two years, Joy invested Rs. 8000 at 10% simple annual interest. How many years after Veeru's investment will their balances, i.e., principal plus accumulated interest, be equal?

**Answer:** 12

**Solution:**

We can draw the following table:

Name	Principal	Rate	Year	Interest	Amount
Veeru	10000	5	T	500T	10000 + 500T
Joy	8000	10	T-2	800(T - 2)	8000 + 800(T - 2)

So,  $10000 + 500T = 8000 + 800(T - 2)$

$2000 + 500T = 800T - 1600$

$\Rightarrow 3600 = 300T$

$\Rightarrow T = 12$

###TOPIC###Quantitative Aptitude||Arithmetic||Interest (Simple and Compound)###



18. On a rectangular metal sheet of area 135 sq in, a circle is painted such that the circle touches two possible sides. If the area of the sheet left unpainted is two-thirds of the painted area, then the perimeter of the rectangle, in inches, is

A.  $5\sqrt{\pi}\left(3 + \frac{9}{\pi}\right)$

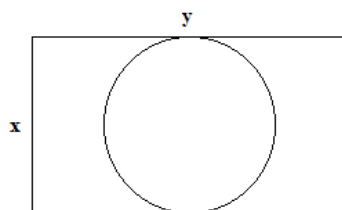
B.  $3\sqrt{\pi}\left(\frac{5}{2} + \frac{6}{\pi}\right)$

C.  $4\sqrt{\pi}\left(3 + \frac{9}{\pi}\right)$

D.  $3\sqrt{\pi}\left(5 + \frac{12}{\pi}\right)$

**Answer: D**

**Solution:**



Let the dimensions of the rectangle be  $x$  and  $y$ , where  $x < y$ .

Then,  $xy = 135$  .....(1)

Diameter of the circle =  $x$

$\Rightarrow$  Radius of circle =  $x/2$

Painted area of sheet =  $\pi\left(\frac{x}{2}\right)^2$

Unpainted area of sheet =  $135 - \pi\left(\frac{x}{2}\right)^2$

According to the question, we can write the following:

$$135 - \pi\left(\frac{x}{2}\right)^2 = \frac{2}{3} \times \pi\left(\frac{x}{2}\right)^2$$

$$\Rightarrow 135 = \frac{5}{3} \times \pi \left( \frac{x}{2} \right)^2$$

$$\Rightarrow \frac{81}{\pi} = \left( \frac{x}{2} \right)^2 \quad \Rightarrow x = \frac{18}{\sqrt{\pi}} \text{ inches}$$

Putting this in (1), we get the following:

$$y = \frac{135\sqrt{\pi}}{18} = \frac{15\sqrt{\pi}}{2} \text{ inches}$$

$$\text{Perimeter of rectangle} = 2x + 2y = \frac{36}{\sqrt{\pi}} + 15\sqrt{\pi} = 3\sqrt{\pi} \left( 5 + \frac{12}{\pi} \right)$$

###TOPIC###Quantitative Aptitude||Mensuration||Mensuration###



19. How many 3-digit numbers are there, for which the product of their digits is more than 2 but less than 7?

**Answer:** 21

**Solution:**

Let us assume the three digit number is abc.

Since  $2 < a \times b \times c < 7$ , the product of the digits can be 3, 4, 5, or 6.

Case	Product	A	B	C	No. of numbers
1	3	1	1	3	$3!/2! = 3$
2	4	1	1	4	3
3	4	1	2	2	3
4	5	1	1	5	3
5	6	1	2	3	$3! = 6$
6	6	1	1	6	3
Total					21

###TOPIC###Quantitative Aptitude||Algebra||Permutation and Combination###

20. The number of distinct real roots of the equation  $\left(x + \frac{1}{x}\right)^2 - 3\left(x + \frac{1}{x}\right) + 2 = 0$  equals \_\_\_\_.

**Answer:** 1

**Solution:**

Substituting  $x + \frac{1}{x} = y$  in the given equation, we get the following:

$$y^2 - 3y + 2 = 0$$

$$\Rightarrow (y - 1)(y - 2) = 0$$

$$\Rightarrow y = 1 \text{ or } 2$$

Case 1: If  $y = 1$

$$x + \frac{1}{x} = 1$$

$$x^2 - x + 1 = 0$$

$$D = (-1)^2 - 4 \times 1 \times 1 = -3 < 0$$

There is no real root in this case.

Case 1: If  $y = 2$

$$x + \frac{1}{x} = 2$$

$$x^2 - 2x + 1 = 0$$

$$D = (-2)^2 - 4 \times 1 \times 1 = 0$$

There is exactly one distinct real root in this case.

Hence, the given equation has only 1 distinct real root.

###TOPIC###Quantitative Aptitude||Algebra||Quadratic Equations###

21. A solution of volume 40 litres has dye and water in the proportion 2:3. Water is added to the solution to change this proportion to 2:5. If one-fourths of this diluted solution is taken out, how many litres of dye must be added to the remaining solution to bring the proportion back to 2:3?

**Answer:** 8

**Solution:**

For the initial solution,

Total volume = 40 litres

Volume of dye =  $\frac{2}{5}$  of 40 = 16 litres

Volume of water =  $\frac{3}{5}$  of 40 = 24 litres

Now we add water to change the proportion to 2:5.

So, the volume of dye will not change.

Volume of dye in the new solution = 16 litres

Since water:dye = 5:2

⇒ Volume of water in new solution =  $\frac{5}{2}$  of 16 = 40 litres

Total volume of new solution = 56 litres

Now  $\frac{1}{4}$ <sup>th</sup> of the solution is removed.

So,  $\frac{3}{4}$ <sup>th</sup> of the solution remains.

Total volume left =  $\frac{3}{4}$  of 56 = 42 litres

Volume of dye left =  $\frac{3}{4}$  of 16 = 12 litres

Volume of water left =  $\frac{3}{4}$  of 40 = 30 litres

Volume of dye =  $\frac{2}{3}$  of 30 = 20 litres

Volume of dye added = 20 - 12 = 8 litres

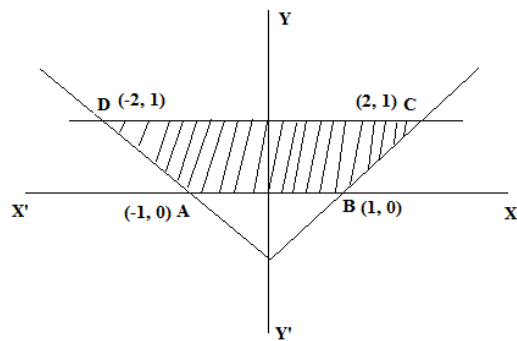
###TOPIC###Quantitative Aptitude||Arithmetic||Mixtures and Alligations###

22. The area of the region satisfying the inequalities  $|x| - y \leq 1$ ,  $y \geq 0$  and  $y \leq 1$  is

**Answer:** 3

**Solution:**

We can draw the following graph by using the given inequalities.



The required region is the area of the trapezium ABCD shown in the graph.

$AB = 2$  units

$CD = 4$  units

$h = 1$  unit

Area of a trapezium is  $\frac{1}{2} \times \text{height} \times \text{sum of the parallel sides}$

$$\text{Area} = \frac{1}{2} \times (2 + 4) \times 1 = 3 \text{ sq. unit}$$

###TOPIC###Quantitative Aptitude||Algebra||Inequalities###

23. A circle is inscribed in a rhombus with diagonals 12 cm and 16 cm. The ratio of the area of the circle to the area of the rhombus is \_\_\_\_\_.

A.  $6\pi/25$

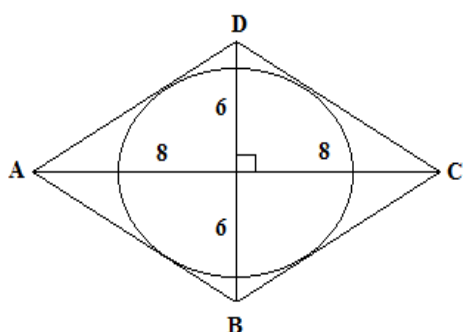
B.  $2\pi/15$

C.  $3\pi/25$

D.  $5\pi/18$

**Answer: A**

**Solution:**



We know that diagonals of the rhombus bisect each other at  $90^\circ$ .

Therefore, using Pythagoras' theorem, we can write the following:

$$\text{Side of rhombus} = \sqrt{\left(\frac{12}{2}\right)^2 + \left(\frac{16}{2}\right)^2} = 10 \text{ cm}$$

$$\text{Area of rhombus} = \frac{1}{2} \times 12 \times 16 = 96 \text{ cm}^2$$

Also, area of rhombus =  $s \times r$ , where 's' is the semi-perimeter and 'r' is the radius of the incircle.

$$96 = 20 \times r$$

$$r = 24/5 \text{ cm}$$

$$\frac{\text{Area of circle}}{\text{Area of rhombus}} = \frac{\pi \left(\frac{24}{5}\right)^2}{96} = \frac{6\pi}{25}$$

###TOPIC###Quantitative Aptitude||Geometry||Plane Geometry###

24. If y is a negative number such that  $2^{y^2 \log_3 5} = 5^{\log_2 3}$ , then y equals \_\_\_\_\_.

A.  $-\log_2(1/5)$

B.  $\log_2(1/3)$

C.  $\log_2(1/5)$

D.  $-\log_2(1/3)$

**Answer: B**

**Solution:**

$$2^{y^2(\log_3 5)} = 5^{\log_2 3}$$

Taking log both sides, we get the following:

$$\log 2^{y^2(\log_3 5)} = \log 5^{\log_2 3}$$

$$\Rightarrow y^2(\log_3 5) \times \log 2 = \log_2 3 \times \log 5$$

$$\Rightarrow y^2 \times \frac{\log 5}{\log 3} \times \log 2 = \frac{\log 3}{\log 2} \times \log 5$$

Cancelling log 5 from both sides, we get the following:

$$\Rightarrow y^2 = (\log_2 3)^2$$

$$\Rightarrow y = \pm \log_2 3$$

Since it is given that 'y' is negative, we can write the following:

$$\Rightarrow y = -\log_2 3 = -1/\log_2 3$$

Hence, option (B) is the correct answer.

###TOPIC###Quantitative Aptitude||Algebra||Logarithm###

25. A train travelled at one-thirds of its usual speed, and hence reached the destination 30 minutes after the scheduled time. On its return journey, the train initially travelled at its usual speed for 5 minutes but then stopped for 4 minutes for an emergency. The percentage by which the train must now increase its usual speed so as to reach the destination at the scheduled time, is nearest to \_\_\_\_.

A. 67



B. 61

C. 50

D. 58

**Answer:** A

**Solution:**

Let the scheduled time be  $T$ .

If the speed is  $1/3$  of the usual speed, then the time should be 3 times the initial time taken.

So, new time =  $3T$

$$3T - T = 30$$

$$\Rightarrow T = 15 \text{ min}$$

On the return journey, the train travelled at its usual speed for 5 min.

So, the remaining distance should be covered in 10 min at the usual speed.

Since 4 min are wasted, the distance should be covered in 6 min.

The remaining time is  $6/10 = 3/5$  of the usual time.

So, the speed should be  $5/3 = 166.67\%$  of the usual speed.

So, the speed should increase by 67% approx.

###TOPIC###Quantitative Aptitude||Arithmetic||Speed, Time and Distance###

26. If  $x = (4096)^{7+4\sqrt{3}}$ , then which of the following equals 64?

A.  $\frac{x^7}{x^{2\sqrt{3}}}$

B.  $\frac{x^7}{x^{4\sqrt{3}}}$

C.  $\frac{x^{\frac{7}{2}}}{x^{2\sqrt{3}}}$

D.  $\frac{x^{\frac{7}{2}}}{x^{\frac{4}{\sqrt{3}}}}$

**Answer: C**

**Solution:**

$$x = (4096)^{7+4\sqrt{3}}$$

Taking both sides power, we get the following:

$$\Rightarrow x^{7-4\sqrt{3}} = (4096)^{(7+4\sqrt{3})(7-4\sqrt{3})}$$

Simplifying this, we can write the following:

$$\Rightarrow x^{7-4\sqrt{3}} = (64^2)^1$$

$$\Rightarrow 64 = (x^{7-4\sqrt{3}})^{\frac{1}{2}}$$

$$\Rightarrow 64 = x^{\frac{7}{2}-2\sqrt{3}}$$

$$\Rightarrow 64 = \frac{x^{\frac{7}{2}}}{x^{2\sqrt{3}}}$$

Hence, option (C) is the correct answer.

###TOPIC###Quantitative Aptitude||Algebra||Higher Degree Equations###