









Formula Sheet

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QUADRATIC EQUATIONS

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CP - 01

QUADRATIC EQUATIONS

Quadratic Equation

- 1. Standard Form of Quadratic Equations
- 2. Zeros, Roots and Solutions
- 3. Methods to Solve
- 4. Nature of Roots





Important Terms

Degree

a, b, and c are real numbers and a ≠ 0

Zeroz.

Zeros of

quadratic

polynomial

P(x)

P(x) = (x-2)(x-2)

x=2&2

Rooty

Roots of quadratic equation

$$(x-2)(x-2)=0$$

 $x=2 \& 2$

Solution

The values of the unknown variable x, which satisfy the equation..

(x-2)(x-2)=0

x = 2

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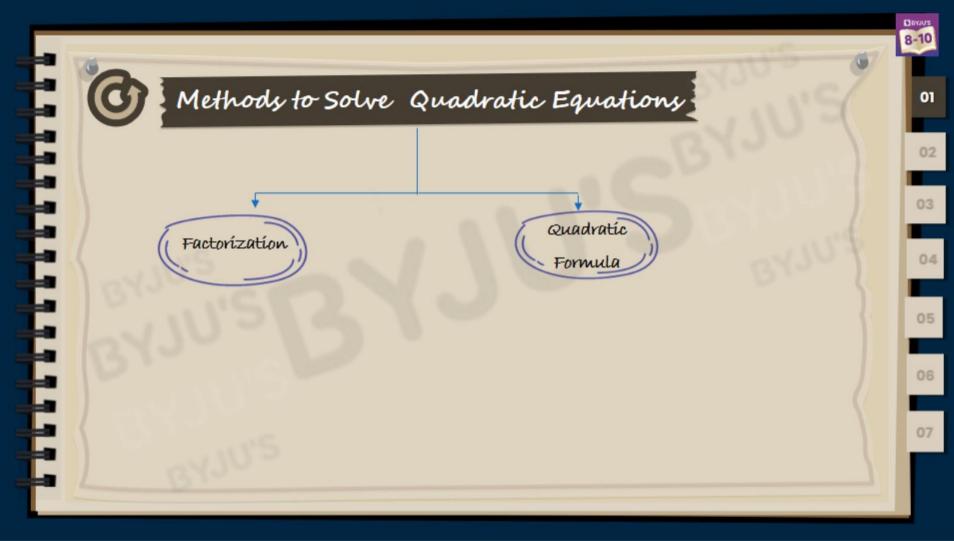
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Factorization

1. Split the middle term.

Product of split terms ; = (a x c)

General form. $ax^2 + bx + c = 0.$

Eg:
$$9x^2 - 3x - 2 = 0$$
.
 $9x^2 - 6x + 3x - 2 = 0$.

2. Factorize the equation 3x(3x-2)+1(3x-2)=0.

$$3x(3x-2)+1(3x-2)=0.$$

$$\forall$$

13. Equate each factor to
$$0$$
; $(3x-2)(3x+1)=0$

$$(3x-2)(3x+1)=0$$

$$x = \frac{2}{3} \text{ or } x = -\frac{1}{3}.$$

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Quadratic Formula

$$ax^2 + bx + c = 0$$

Root
$$x = \frac{\left(-b \pm \sqrt{b^2 - 4ac}\right)}{2a}$$

$$x = \frac{\left(-b + \sqrt{b^2 - 4ac}\right)}{2a} \qquad x = \frac{\left(-b - \sqrt{b^2 - 4ac}\right)}{2a}$$

where,
$$b^2 - 4ac \ge 0$$



The quadratic formula is used where the factorization method is difficult to apply.

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Nature Of Roots

$$ax^2 + bx + c = 0$$

Discriminant (D) =
$$b^2 - 4ac$$

Nature of Roots

$$b^2 - 4ac > 0$$
 $b^2 - 4ac = 0$ $b^2 - 4ac < 0$

Type of Roots

Value of

Roots

Real & Distinct Roots

 $=\frac{-b\pm\sqrt{D}}{2a}$

Real & Equal Roots

 $=\frac{-b}{2a},\frac{-b}{2a}$

No Real Roots

Not Valid 01

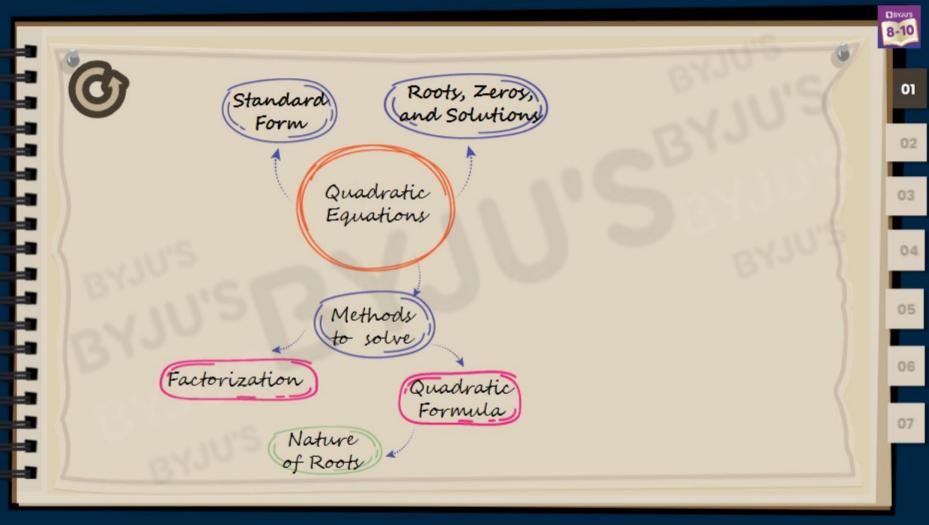
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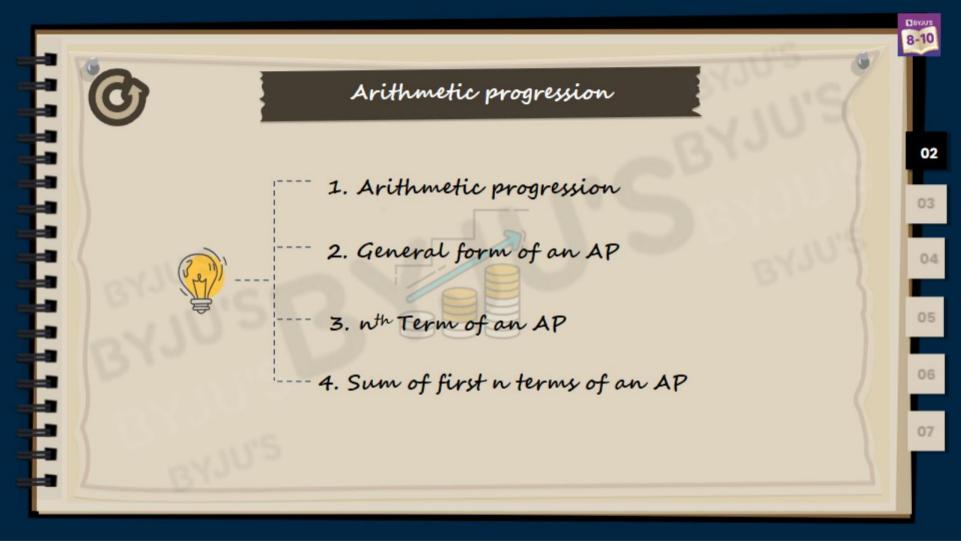


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QUADRATIC EQUATIONS

CP - 02

ARITHMETIC PROGRESSIONS





Arithmetic progression

An arithmetic progression is a sequence of numbers in which each term is obtained by adding a fixed number to the preceding term, except the first term.

Common consecutive terms in an AP is a fixed number, d)



General Form of an AP

A sequence of the form

a, a+d, a+2d, a+3d, a+4d and so on,

Where a is the first term and d is a common difference.

nth Term of an AP

$$a_n = \{a + (n-1)d\}$$

where a_n is the nth term,

- a is the first term,
- d is the common difference and
- n is the number of terms in the sequence.

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Sum of First n Terms in an AP

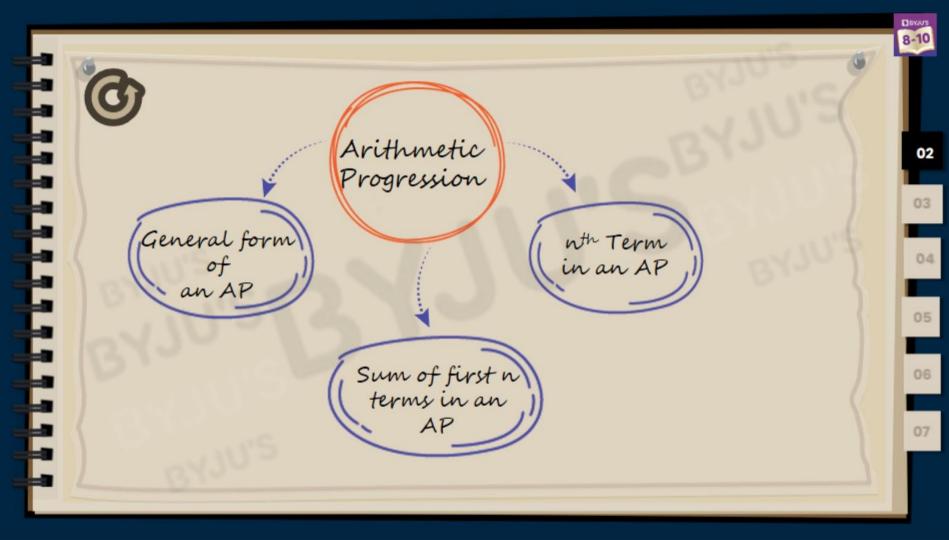
$$S_n = \frac{n}{2} \{ 2a + (n-1)d \}$$

When first term (a) and common difference (d) are known

$$S_n = \frac{n}{2}(a+l)$$

When first term (a) and last term (1) are known

where n is the number of terms in the sequence and S_n is the sum of first n terms



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Sector

The region between an arc and the two radii



Segment

The region between a chord and the arc



Major segment

Minor segment

Tangent

Line touching the circle at only one point



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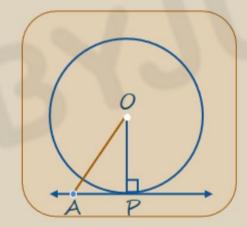
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Theorem 1

The tangent at any point of a circle is perpendicular to the radius through the point of contact.



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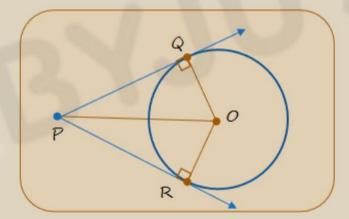
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Theorem 2

The lengths of tangents drawn from an external point to a circle are equal.



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Construction

1. Division of a line segment in a given ratio



2. Construction of pair of tangents

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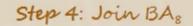
Division of a line segment in the given ratio

Step 1: Draw AB = 16 cm

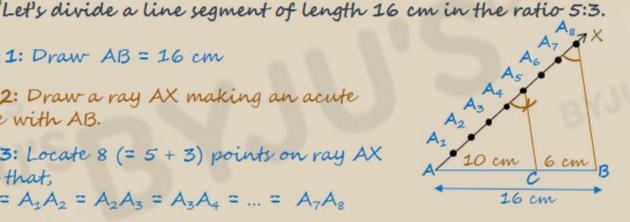
Step 2: Draw a ray AX making an acute angle with AB.

Step 3: Locate 8 (= 5 + 3) points on ray AX such that,

 $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = ... = A_7A_8$



Step 5: Draw a line parallel to BA, from point A5 (by making an angle equal to LAA, B) intersecting AB at point C.





Construction of Pair of Tangents

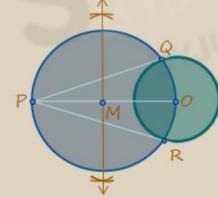
Example

To construct the tangents to a circle from a point P outside it.

Step 1: Join PO and draw a perpendicular bisector of PO to locate its midpoint: Let's say M is the midpoint of PO.

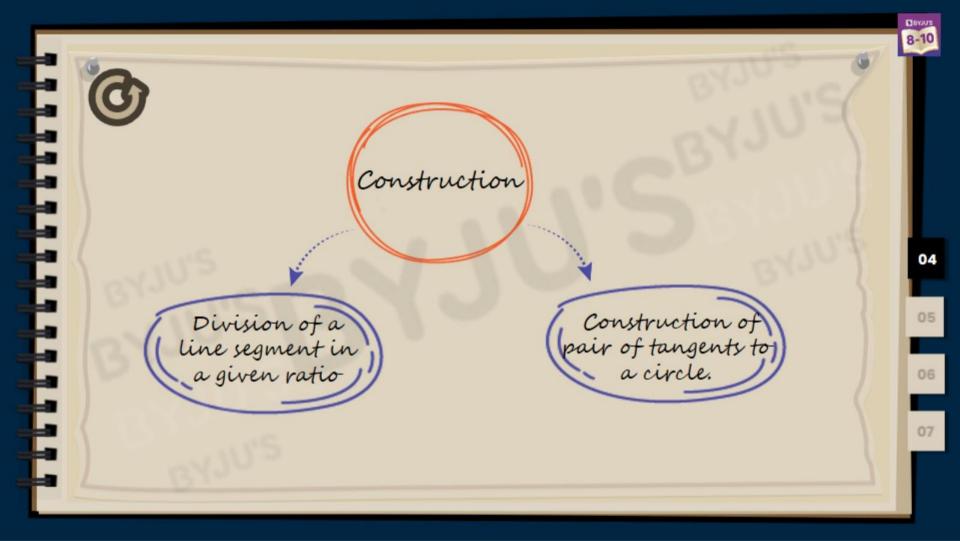
Step 2: Taking M as a centre and MO (or MP) as radius, draw a circle. Let it intersect the given circle at the points Q and R.

Step 3: Join PQ and PR.



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Some Applications of Trigonometry

1. Basic Terminologies

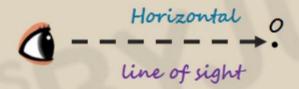


2. Assumptions made while solving

3. Trigonometric Ratios of Some Common Angles



If the object to be viewed is straight ahead, then the line of sight is the same as the horizontal level.



Line of Sight

The line drawn from the eyes of an observer to a point on the object viewed.

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On Line of Sight

Horizontal

Angle of Elevation (θ)

Angle of Elevation

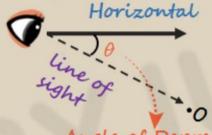
The angle formed by the line of sight with the horizontal when the point being viewed is above the horizontal level.

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Look Below



Angle of Depression (θ)

Angle of Depression

The angle formed by the line of sight with the horizontal when the point being viewed is below the horizontal level.

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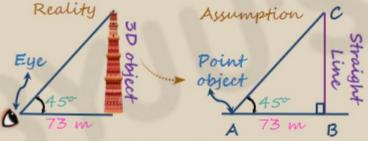
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Assumptions made while solving

Examp

The angle of elevation of the top of the Qutub Minar, 73 m away from its base is 45°.



Steps to Draw the figure:

- 1, Represent the 3D object by a vertical line.
- 2. Represent the observer as a point object.
- 3. Label the angle, height and distance

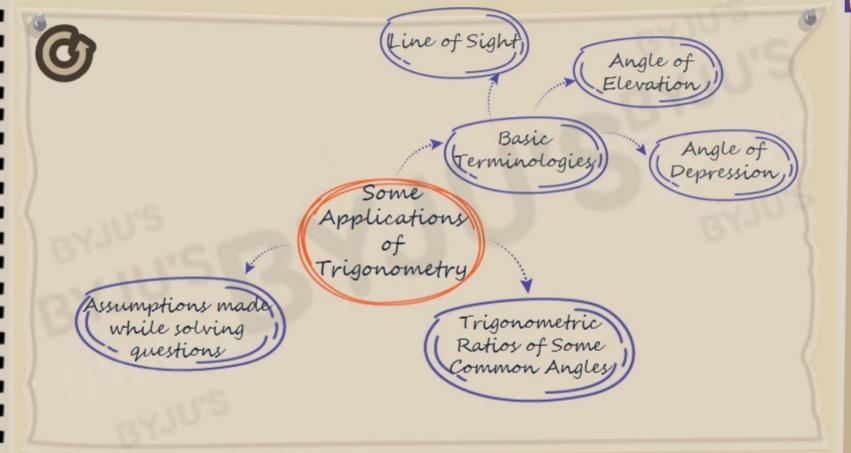
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Trigonometric Ratios of Some Common Angles

		~		Angle θ	——	
		0°	30°	45°	60°	90°
Ratio	sIn θ	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
	cos θ	1	$\frac{2}{\sqrt{3}}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
	tan θ	0	<u>1</u> √3	1	√3	Not defined
	cosec θ	Not defined	2	√2	$\frac{2}{\sqrt{3}}$	1
	sec θ	1	$\frac{2}{\sqrt{3}}$	√2	2	Not defined
	cot θ	Not defined	√3	1	$\frac{1}{\sqrt{3}}$	0



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AND VOLUMES

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Surface Areas and Volumes

- 1. Formulae of Solids
- 2. Combination of Solids



- 3. Surface Area of Combined Solids
- 4. Volume of Combined Solids
- 5. Conversion of Solids



Formulae of Solids

Cube

4a2

: Lateral surface area

: Total surface area

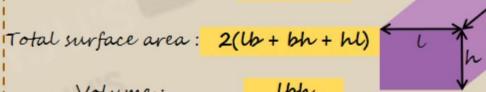
: Volume

Cuboid

Lateral surface area: 2h(l+b)

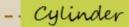
Volume:

Uph





Formulae of Solids



 $2\pi rh$: Curved surface area

 $2\pi rh + 2\pi r^2$: Total surface area

πr2h : Volume

Sphere

Curved surface area:

 $4\pi r^2$

Volume:

 $\frac{4}{3}\pi r^3$





Formulae of Solids

Curved surface area:

 $2\pi r^2$

Total surface area:

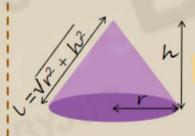
 $3\pi r^2$

Hemisphere

Volume:

2 πr3

Cone



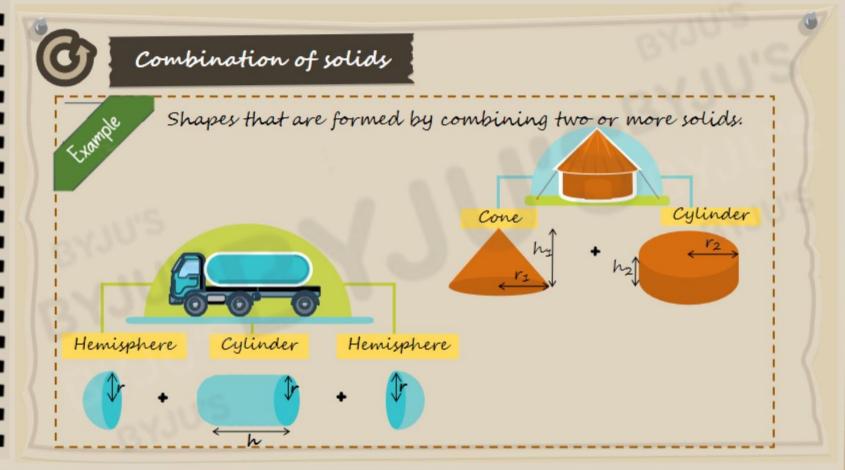
: Curved surface area

 $\pi rl + \pi r^2$: Total surface area

 $\frac{1}{3}\pi r^2 h$

: Volume







Conversion of solids

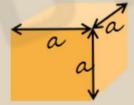
When a solid is reshaped, its volume remains the same.













Sum of volumes of = smaller spheres

Volume of the larger = Volume of sphere

the cube

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STATISTICS



Statistics

1. Mean of Grouped Data



2. Median of Grouped Data

3. Mode of Grouped Data



Mean of Grouped Data

Mean is a measure of central tendency which gives the average of data.

Direct Method

$$\bar{x} = \frac{\sum f_i x_i}{\sum f_i}$$

Class mark $(x_i) = \frac{Upper + Lower Class Limit}{2}$

Mean

Assumed Mean Method

An arbitrary mean 'a' is chosen which is called 'assumed mean', somewhere in the middle of all the values of x.

$$\bar{x} = a + \frac{\sum f_i d_i}{\sum f_i}$$
 Where $d_i = (x_i - a)$



Median of Grouped Data

The median of a set of data is the middlemost number or center value in the set.

Median =
$$l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$$

l = Lower limit of median class

n = Number of observations

f = Frequency of median class

cf = Cumulative frequency of preceding class

h = Class size



Mode of Grouped Data

The mode is the value that is repeatedly occurring in a given set.

Mode=
$$l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right) \times h$$

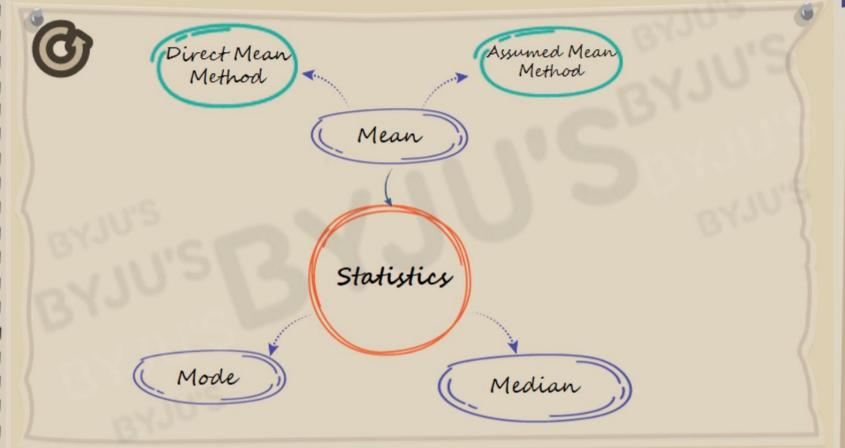
l = lower class limit of the modal class

h = class interval size

 f_1 = frequency of the modal class

fo = frequency of the preceding class

 f_2 = frequency of the succeeding class





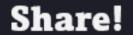














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