1. Rescue teams deployed ______disaster hit areas combat ______ a lot of difficulties to save the people.
   A. with, with  
   B. in, with  
   C. with, at  
   D. to, to  
   Ans. B

2. Select the most appropriate word that can replace the underlined word without changing the meaning of the sentence:
   Now-a-days, most children have a tendency to belittle the legitimate concerns of their parents.
   A. Disparate  
   B. Begrudge  
   C. Reduce  
   D. Applaud  
   Ans. A
   Sol. Belittle: Disparage

3. Select the word that fits the analogy:
   Partial : Impartial :: Popular : _______
   A. Dispopular  
   B. Impopular  
   C. Unpopular  
   D. Mispopular  
   Ans. C

4. After the inauguration of the new building, the Head of the Department (HoD) collated faculty preferences for office space. P wanted a room adjacent to the lab. Q wanted to be close to the lift. R wanted a view of the playground and S wanted a corner office.
   Assuming the everyone was satisfied, which among the following shows a possible allocation?
   A.  
   B.  
   C.  
   D.  
   Ans. C
   Sol. Option C is the only arrangement where all the conditions are successfully fulfilled.

5. If f(x) = x^2 for each x ∈ (−∞, ∞), then \( \frac{f(f(f(x)))}{f(x)} \) is equal to ______.
   A. (f(x))^4  
   B. (f(x))^2  
   C. (f(x))^3  
   D. f(x)  
   Ans. C
6. Nominal interest rate is defined as the amount paid by the borrower to the lender for using the borrowed amount for a specific period of time. Real interest rate calculated on the basis of actual value (inflation-adjusted), is approximately equal to the difference between nominal rate and expected rate of inflation in the economy.

Which of the following assertions is best supported by the above information?

A. Under low inflation, real interest rate is low and borrowers get benefited.
B. Under high inflation, real interest rate is low and lenders get benefited.
C. Under high inflation, real interest rate is low and borrowers get benefited.
D. Under low inflation, real interest rate is high and borrowers get benefited.

Ans. C

7. For the year 2019, which of the previous year’s calendar can be used?

A. 2013     B. 2014
C. 2012     D. 2011

Ans. A

Sol. A year has 365 days, except a leap year, which has 366 days.
365 days = 52 weeks + 1 day.
366 days = 52 weeks + 2 days.
So, for a normal year, the next year's calendar will shift by one day and for a leap year, the next year's calendar will shift by two days.
Assuming 2019 starts on a Sunday.
2018: Saturday
2017: Friday
2016: Wednesday (Since 2016 is a leap year)
2015: Tuesday
2014: Monday
2013: Sunday

8. The ratio of ‘the sum of the odd positive integers from 1 to 100’ to ‘the sum of the even positive integers from 150 to 200’ is ______.

A. 45 : 95     B. 1 : 2
C. 50 : 91     D. 1 : 1

Ans. C

Sol. Sum of the odd positive integers from 1 to 100
= 1 + 3 + 5 ...... + 99
No. of terms = 50,
First term = 1; Last term = 99
Therefore, Sum = 50×(1+99)/2 = 2500
Sum of the even positive integers from 150 to 200
= 150 + 152 + 154 + ......... + 198 + 200
No. of terms = 26
First term = 150; Last term = 200
Therefore, Sum = 26×(150+200)/2 = 4550
d ratio = 2500/4550 = 50/91

9. In a school of 1000 students, 300 students play chess and 600 students play football. If 50 students play both chess and football, the number of students who play neither is _____.

A. 150     B. 200
C. 100     D. 50

Ans. A

Sol. N(S) = 1000
N(C) = 300
N(F) = 600
N(C&F) = 50
N(S) = N(C) + N(F) - N(C&F) + N(none)
d N(none) = 150

10. The monthly distribution of 9 Watt LED bulbs sold by two firms X and Y from January to June 2018 is shown in the pie-chart and the corresponding table.
If the total number of LED bulbs sold by two firms during April-June 2018 is 50000, then the number of LED bulbs sold by the firm Y during April-June 2018 is ______.
Percentage of 9 Watt LED bulbs sold by the firms X and Y from January 2018 to June, 2018

<table>
<thead>
<tr>
<th>Month</th>
<th>Ratio of LED bulbs sold by two firms (X : Y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>January</td>
<td>7 : 8</td>
</tr>
<tr>
<td>February</td>
<td>2 : 3</td>
</tr>
<tr>
<td>March</td>
<td>2 : 1</td>
</tr>
<tr>
<td>April</td>
<td>3 : 2</td>
</tr>
<tr>
<td>May</td>
<td>1 : 4</td>
</tr>
<tr>
<td>June</td>
<td>9 : 11</td>
</tr>
</tbody>
</table>

A. 8750  
B. 8250  
C. 9750  
D. 11250

**Ans. C**
1. A triangular direct runoff hydrograph due to a storm has a time base of 90 hours. The peak flow of 60 m³/s occurs at 20 hours from the start of the storm. The area of catchment is 300 km². The rainfall excess of the storm (in cm), is
   A. 3.24  B. 6.48  C. 5.40  D. 2.00
   Ans. A
   Sol.

   \[
   \text{Area of DRH} = \text{Vol. of Rainfall Excess} = \frac{1}{2} \times 90 \times 60 \times 3600 = 300 \times 10^6 \times x \times 0.01
   \]
   \[
   x = 3.24 \text{ cm}
   \]

2. Soil deposit formed due to transportation by wind is termed as
   A. lacustrine deposit  B. aeolian deposit  C. estuarine deposit  D. alluvial deposit
   Ans. B

3. For an axle load of 15 tonne on a road, the Vehicle Damage Factor (round off to two decimal places), in terms of the standard axle load of 8 tonne, is ______.
   Ans. 12.36
   Sol. \[
   \text{VDF} = \left( \frac{\text{axle load}}{\text{standard load}} \right)^4 = \left( \frac{15}{8} \right)^4 = 12.36
   \]

4. The traffic starts discharging from an approach at an intersection with the signal turning green. The constant headway considered from the fourth or fifth headway position is referred to as
   A. Discharge headway  B. Saturation headway  C. Intersection headway  D. Effective headway
   Ans. B
   Sol. Saturation headway
   After initial some vehicle, Time headway remains constant.

5. A weightless cantilever beam of span L is loaded as shown in the figure. For the entire span of the beam, the material properties are identical and the cross section is rectangular with constant width.

   From the flexure-critical perspective, the most economical longitudinal profile of the beam to carry the given loads amongst the options given below, is
   A.  
   B. 

6. As per IS 456:2000, the pH value of water for concrete mix shall NOT be less than
   A. 6.0      B. 4.5
   C. 5.0      D. 5.5
   Ans. A
   Sol. As per IS: 456-2000, Page no-14, clause 5.4.2, the pH value of water \( \not< 6 \) of the water used in construction should not be acidic in nature. If water used in construction is acidic, durability problem of concrete occurs.

7. The ordinary differential equation
   \[
   \frac{d^2u}{dx^2} - 2x^2u + \sin x = 0
   \]
   is
   A. linear and homogeneous
   B. linear and nonhomogeneous
   C. nonlinear and homogeneous
   D. nonlinear and nonhomogeneous
   Ans. B
   Sol. \[
   \frac{d^2x}{dx^2} - 2x^2u + \sin x = 0
   \]
   The degree of all terms is different; hence it is non-homogeneous equation. The given ordinary differential equation is linear because the coefficient of \( y \) and \( y' \), \( y'' \) is the function of \( x \).

8. A one-dimensional consolidation test is carried out on a standard 19 mm thick clay sample. The oedometer's deflection gauge indicates a reading of 2.1 mm, just before removal of the load, without allowing any swelling. The void ratio is 0.62 at this stage. The initial void ratio (round off to two decimal places) of the standard specimen is _____.
   Ans. 0.8213
   Sol. \[
   \frac{\Delta e}{1+e_f} = \frac{\Delta H}{H_f}
   \]
   \[
   \frac{e_i - .62}{1+.62} = \frac{2.1}{16.9}
   \]
   \[
   e_i = .8213
   \]
9. The relationship between oxygen consumption and equivalent biodegradable organic removal (i.e., BOD) in a closed container with respect to time is shown in the figure.

Assume that the rate of oxygen consumption is directly proportional to the amount of degradable organic matter and is expressed as \( \frac{dL_t}{dt} = -kL_t \), where, \( L_t \) (in mg/litre) is the oxygen equivalent of the organics remaining at time \( t \) and \( k \) (in d\(^{-1}\)) is the degradation rate constant. \( L_0 \) is the oxygen equivalent of organic matter at time, \( t = 0 \).

In the above context, the correct expression is

A. \( BOD_t = L_0 - L_t \)
B. \( BOD_t = L_5 \)
C. \( L_t = L_0 (1 - e^{-kt}) \)
D. \( L_0 = L_t e^{-kt} \)

Ans. A

Sol. Here, \( L_0 \) = total oxygen equivalent of the organics at time, \( t = 0 \)
\( L_t \) = total oxygen equivalent at \( t = t \)

Given, \( \frac{dL_t}{dt} = -kL_t \)

\[ \Rightarrow \int_{L_t}^{L_0} \frac{dt}{L_t} = -k \int_0^t dt \]

\[ \Rightarrow \ln \left( \frac{L_t}{L_0} \right) = -kt \]

\[ \Rightarrow L_t = L_0 e^{-kt} \]

:. BOD exerted = \( BOD_t = (L_0 - L_t) = L_0 - L_0 e^{-kt} = L_0 (1 - e^{-kt}) \)

10. The velocity components in the x and y directions for an incompressible flow are given as \( u = (-5 + 6x) \) and \( v = -(9 + 6y) \), respectively. The equation of the streamline is

A. \( \frac{-5 + 6x}{9 + 6y} = \text{constant} \)
B. \( (-5 + 6x)(9 + 6y) = \text{constant} \)
C. \( (-5 + 6x) - (9 + 6y) = \text{constant} \)
D. \( \frac{9 + 6y}{-5 + 6x} = \text{constant} \)

Ans. B

Sol. Equation of streamline can be given as

\[ \frac{dx}{u} = \frac{dy}{v} \]

Given: \( u = (-5 + 6x) \)
\( V = -(9 + 6y) \)

\[ \therefore \frac{dx}{(-5 + 6x)} = -\frac{dy}{(9 + 6y)} \]

\[ \Rightarrow \ln((-5 + 6x)) + \ln(9 + 6y) = \text{constant} \]

\[ \Rightarrow (-5 + 6x)(9 + 6y) = \text{constant} \]

11. Velocity distribution in a boundary layer is given by

\[ \frac{u}{U_\infty} = \sin \left( \frac{\pi y}{2\delta} \right) \]

where \( u \) is the velocity at vertical coordinate \( y \), \( U_\infty \) is the free stream velocity and \( \delta \) is the boundary layer thickness. The values of \( U_\infty \) and \( \delta \) are 0.3 m/s and 1.0 m, respectively. The velocity gradient \( \frac{dU}{dy} \) (in s\(^{-1}\), round off to two decimal places) at \( y = 0 \), is ______.

Ans. 0.4712

Sol. \[ \frac{U}{U_\infty} = \sin \left( \frac{\pi y}{2\delta} \right) \]

Velocity gradient \( \frac{dU}{dy} \)\( y = 0 \)

\[ U = U_\infty \sin \left( \frac{\pi y}{2\delta} \right) \]

\[ \frac{dU}{dy} = \frac{\pi U_\infty}{2\delta} \cos \left( \frac{\pi y}{2\delta} \right) \]
\[
\frac{\partial \gamma}{\partial y}_{y=0} = \frac{\pi U_0}{2} \cos \left( \frac{\pi x}{2} \right)
\]

\[
= \frac{\pi U_0}{2} \cos 0 \quad \because \cos 0 = 1
\]

\[
= \frac{\pi U_0}{2} \frac{0.3}{1} = 0.3 \times \frac{\pi}{2}
\]

\[
= 0.4712
\]

12. The maximum applied load on a cylindrical concrete specimen of diameter 150 mm and length 300 mm tested as per the split tensile strength test guidelines of IS 5816:1999 is 157 kN. The split tensile strength (in MPa, round off to one decimal place) of the specimen is

Ans. 2.22 N/mm²

Sol. Split tensile strength

\[
\sigma = \frac{2P}{\pi LD} = \frac{\left( 2 \times 157 \times 10^3 \right)}{\left( \pi \times 300 \times 150 \right)} = 2.22 \text{ N/mm}^2
\]

13. The ratio of the plastic moment capacity of a beam section to its yield moment capacity is termed as

A. load factor
B. shape factor
C. slenderness ratio
D. aspect ratio

Ans. B

Sol. Shape factor is defined as the ratio of plastic moment of resistance of the section to yield moment of resistance of section.

14. A gas contains two types of suspended particles having average sizes of 2 μm and 50 μm. Amongst the options given below, the most suitable pollution control strategy for removal of these particles is

A. Electrostatic precipitator followed by venturi scrubber
B. Electrostatic precipitator followed by cyclonic separator
C. Settling chamber followed by bag filter
D. Bag filter followed by electrostatic precipitator

Ans. C

15. Two identically sized primary settling tanks receive water for Type-I settling (discrete particles in dilute suspension) under laminar flow conditions. The Surface Overflow Rate (SOR) maintained in the two tanks are 30 m³/m².d and 15 m³/m².d. The lowest diameters of the particles, which shall be settled out completely under SORs of 30 m³/m².d and 15 m³/m²/d are designated as \( d_{30} \) and \( d_{15} \), respectively. The ratio, \( \frac{d_{30}}{d_{15}} \) (round off to two decimal places), is ______.

Ans. 1.414

Sol. According to stokes law

\[
V_s = \frac{(G-1)gd^2}{18u}
\]

Where, \( V_s \) = settling velocity
\( G \) = specific gravity \( y \) the particle
\( d \) = diameter of particle
\( v \) = kinematic viscosity

\[
\therefore \text{By above expression we can imply } V_s \propto d^2
\]

\[
\Rightarrow \frac{V_{30}}{V_{15}} = \left( \frac{d_{30}}{d_{15}} \right)^2
\]

\[
\Rightarrow \frac{d_{30}}{d_{15}} = \sqrt{\frac{30}{15}} \quad \therefore V_{30} = 30 \text{ m/d} \quad V_{15} = 15 \text{ m/d}
\]

\[
\Rightarrow \frac{d_{30}}{d_{15}} = 1.414
\]

16. Super passage is a canal cross-drainage structure in which

A. Natural stream water flows under pressure below a canal
B. Canal water flows under pressure below a natural stream
C. Natural stream water flows with free surface below a canal
D. Canal water flows with free surface below a natural stream

Ans. D
17. A soil has dry unit weight of 15.5 kN/m³, specific gravity of 2.65 and degree of saturation of 72%. Considering the unit weight of water as 10 kN/m³, the water content of the soil (in %, round off to two decimal places) is _______.

**Ans.** 19.27%

**Sol.**
\[
\gamma_d = 15.5 \text{ kN/m}^3 \\
G = 2.65 \\
S = .72 \\
\gamma_w = 10 \text{ kN/m}^3 \\
w = ? \\
\gamma_d = \frac{G \gamma_w}{1 + e} \\
15.5 = \frac{2.65 \times 10}{1 + e} \\
e = .7096 \\
S_e = wG \\
0.72 \times 0.7096 = w \times 2.65 \\
w = 0.1927 = 19.27\%
\]

18. The following partial differential equation is defined for \( u: u(x, y) \)
\[
\frac{\partial u}{\partial y} = \frac{\partial^2 u}{\partial x^2}; \quad y \geq 0; \quad x_1 \leq x \leq x_2 
\]

The set of auxiliary conditions necessary to solve the equation uniquely, is
A. Two initial conditions and one boundary condition
B. Three boundary conditions
C. One initial condition and two boundary conditions
D. Three initial conditions

**Ans.** A

**Sol.** Let \( u = xy \)
\[
\frac{\partial u}{\partial y} = xy' \\
\frac{\partial^2 u}{\partial x^2} = yx'' \\
\text{Given} \quad \frac{\partial u}{\partial y} = \frac{\partial^2 u}{\partial x^2} \\
x'y' = yx'' \\
\Rightarrow \quad \frac{y'}{x} = \frac{x'}{y} = k
\]

19. Muskingum method is used in
A. Hydrologic channel routing
B. Hydrologic reservoir routing
C. Hydraulic channel routing
D. Hydraulic reservoir routing

**Ans.** A

20. The integral
\[
\int_0^1 (5x^3 + 4x^2 + 3x + 2)dx
\]

is estimated numerically using three alternative methods namely the rectangular, trapezoidal and Simpson's rules with a common step size. In this context, which one of the following statements is TRUE?
A. Simpson's rule as well as rectangular rule of estimation will give NON-zero error.
B. Simpson’s rule, rectangular rule as well as trapezoidal rule of estimation will give NON-zero error.
C. Only Simpson’s rule of estimation will give zero error.
D. Only the rectangular rule of estimation will give zero error.

Ans. C

Sol. Simpson uses a cubic function for interpolation and it does not give an error for a cubic functions.

21. The value of \( \lim_{x \to \infty} \frac{\sqrt{9x^2 + 2020}}{x + 7} \) is

A. 3
B. indeterminable
C. \( \frac{7}{9} \)
D. 1

Ans. A

Sol. \( \lim_{x \to \infty} \frac{\sqrt{9x^2 + 2020}}{x + 7} \)

Dividing numerator and denominator by ‘x’

\( \lim_{x \to \infty} \frac{\sqrt{\frac{9x^2 + 2020}{x^2}}}{\frac{x + 7}{x}} \)

\( \lim_{x \to \infty} \frac{\sqrt{\frac{9 + \frac{2020}{x^2}}{1 + \frac{7}{x}}}}{1 + \frac{7}{x}} \)

Putting \( x \to \infty \) \( \Rightarrow \frac{1}{x^2} \to 0, \frac{1}{x} \to 0 \)

\( = \frac{\sqrt{9 + 0}}{1 + 0} = \frac{\sqrt{9}}{1} = 3 \)

22. A sample of 500 g dry sand, when poured into a 2-litre capacity cylinder which is partially filled with water, displaces 188 cm\(^3\) of water. The density of water is 1 g/cm\(^3\). The specific gravity of the sand is

A. 2.72
B. 2.66
C. 2.52
D. 2.55

Ans. B

Sol. Mass = 500 gm

Volume displaced = 188 cm\(^3\)

\( G = \frac{\rho_{solid}}{\rho_{water}} \)

\( G = \frac{500gm / 188cc}{1gm / cc} \)

\( G = 2.659 \)

23. A fair (unbiased) coin is tossed 15 times. The probability of getting exactly 8 Heads (round off to three decimal places), is ______.

Ans. 0.196

Sol. \( x = 15 \)

\( P(r = 8) = \binom{n}{r} p^r q^{n-r} \)

\( = 15C_8 p^8 q^{15-8} \)

\( P = (\text{probability of success in toss}) = \frac{1}{2} \)

\( q = (\text{probability of failure during toss}) = \frac{1}{2} \)

\( P(r = 8) = 15C_8 \left( \frac{1}{2} \right)^8 \left( \frac{1}{2} \right)^7 \)

\( = 15C_8 \left( \frac{1}{2} \right)^{15} = 0.196 \)

24. The state of stress represented by Mohr’s circle shown in the figure is

[Diagram of Mohr’s circle showing Shear stress and Normal stress with point (0, 0)]

https://byjus.com/gate/
A. pure shear  
B. biaxial tension of equal magnitude  
C. hydrostatic stress  
D. uniaxial tension  

**Ans. A**

**Sol.**  
\[ \therefore \sigma_1 = -\sigma_2 \]  
\[ \therefore A \]

25. 24-h traffic count at a road section was observed to be 1000 vehicles on a Tuesday in the month of July. If daily adjustment factor for Tuesday is 1.121 and monthly adjustment factor for July is 0.913, the Annual Average Daily Traffic (in veh/day, round off to the nearest integer) is _______.

**Ans. 1023**

**Sol.**  
24 hr daily volume of Tuesday = 1000 vch  
Daily adjustment factor = 1.121  
Monthly adjustment factor = 0.913  
Vol. d week = 1000 × 1.21 = 1121  
AADT = Monthly Adjustment factor × ADT = 0.913 × 1121  
= 1023.473 veh.per day  
= 1023 veh.per day

26. For the hottest month of the year at the proposed airport site, the monthly mean of the average daily temperature is 39°C. The monthly mean of the maximum daily temperature is 48°C for the same month of the year. From the given information, the calculated Airport Reference Temperature (in °C), is  
A. 42  
B. 48  
C. 39  
D. 36  

**Ans. A**

**Sol.**  
Airport reference temperature is given by following expression.  
\[ ART = \left[ T_a + \frac{T_m + T_a}{3} \right] \]  
where, \( T_a \) = average daily temperature  
\( T_m \) = maximum daily temperature  
\[ \therefore ART = \left[ 39 + \frac{48 - 39}{3} \right] \]  
\[ \therefore ART = 42°C \]

27. The flow-density relationship of traffic on a highway is shown in the figure.  

The correct representation of speed-density relationship of the traffic on this highway is  

**Ans. A**
28. Permeability tests were carried out on the samples collected from two different layers as shown in the figure (not drawn to the scale). The relevant horizontal \((k_h)\) and vertical \((k_v)\) coefficients of permeability are indicated for each layer.

\[
\begin{align*}
&k_{h1} = 4.4 \times 10^{-3} \text{ m/s} \\
&k_{v1} = 4 \times 10^{-3} \text{ m/s} \\
&k_{h2} = 6 \times 10^{-1} \text{ m/s} \\
&k_{v2} = 5.5 \times 10^{-1} \text{ m/s}
\end{align*}
\]

Ground level

\[
\begin{align*}
&3 \text{ m} \\
&4 \text{ m}
\end{align*}
\]

Layer 1

Layer 2

The ratio of the equivalent horizontal to vertical coefficients of permeability, is

A. 37.29  
B. 68.25  
C. 80.20  
D. 0.03

Ans. A

Sol. \[
\begin{align*}
keq_h &= \frac{4.4 \times 10^{-3} \times 3 + 6 \times 10^{-1} \times 4}{7} \\
keq_v &= \frac{3}{4 \times 10^{-3} + \frac{4}{5.5 \times 10^{-1}}}
\end{align*}
\]

\[
\begin{align*}
&= 37.29
\end{align*}
\]

29. A 4\times 4\) matrix \([P]\) is given below

\[
[P] = \begin{bmatrix}
0 & 1 & 3 & 0 \\
-2 & 3 & 0 & 4 \\
0 & 0 & 6 & 1 \\
0 & 0 & 1 & 6
\end{bmatrix}
\]

The eigenvalues of \([P]\) are

A. 1, 2, 3, 4  
B. 1, 2, 5, 7  
C. 3, 4, 5, 7  
D. 0, 3, 6, 6

Ans. B

Sol.

\[
[P] = (-2) \begin{bmatrix}
1 & 3 & 0 \\
0 & 6 & 1 \\
0 & 1 & 6
\end{bmatrix}
\]

\[
\begin{align*}
&= \begin{bmatrix}
1 & 3 & 0 \\
0 & 6 & 1 \\
0 & 1 & 6
\end{bmatrix}
\end{align*}
\]

\[
|P| = 2 \{1(36 - 1) - 3 (0 - 0) - 0(0 - 0)\}
\]

\[
|P| = 70
\]

As, the determinant of the given matrix is non-zero

Hence, the matrix is singular.

The product of eigen values = \(|A|\)

\[
\lambda_1, \lambda_2, \lambda_3, \lambda_4 = 70
\]

sum of eigen values = trace of matrix \(P\)

trace of matrix \(P = 0 + 3 + 6 + 6 \)

\[
= 15
\]

\[
\lambda_1 + \lambda_2 + \lambda_3 + \lambda_4 = 50
\]

Checking the above options, only (B) option is correct.

\[
\lambda_1, \lambda_2, \lambda_3, \lambda_4, = 1, 2, 5, 7
\]

30. The diameter and height of a right circular cylinder are 3 cm and 4 cm, respectively. The absolute error in each of these two measurements is 0.2 cm. The absolute error in the computed volume (in cm\(^3\), round off to three decimal places), is _____.

Ans. 5.18 cm\(^3\)

Sol.

\[
\text{diameter} = d = 3 \text{ cm} \\
\text{height} = h = 4 \text{ cm} \\
\text{e}_d = \text{e}_h = \pm 0.2 \text{ cm} \\
\text{v} = f(d, h) \\
\text{v} = \frac{\pi d^2 h}{4} \\
\text{dv} = \left(\frac{\partial v}{\partial d}\right) \text{dd} + \left(\frac{\partial v}{\partial h}\right) \text{dh} \\
\text{dv} = \frac{\pi dh}{2} \times e_d + \frac{\pi d^2}{4} \times e_h \\
\therefore \text{Absolute error} = 5.18 \text{ cm}^3
\]
31. Two steel plates are lap jointed in a workshop using 6 mm thick fillet weld as shown in the figure (not drawn to the scale). The ultimate strength of the weld is 410 MPa.

As per Limit State Design of IS 800:2007, the design capacity (in kN, round off to three decimal places) of the welded connection, is _______.

Ans. 413.586 kN

Sol. \[
\left(\frac{t_{uw}}{\sqrt{3} \times 1.25}\right) \times r \times (t_1) = \left(\frac{410}{\sqrt{3} \times 1.25}\right) \times 520 \times (0.7 \times 6) = 413.586 \text{ kN}.
\]

32. The ion product of water ($pK_w$) is 14. If a rain water sample has a pH of 5.6, the concentration of OH$^-$ in the sample (in $10^{-9}$ mol/litre, round off to one decimal place), is _______.

Ans. 3.981

Sol. pH + POH = 14

$\Rightarrow 5.6 + \text{POH} = 14$

$\Rightarrow \text{POH} = 14 - 5.6 = 8.4$

Also, POH = $-\log [\text{OH}^-]$

$\Rightarrow 8.4 = -\log [\text{OH}^-]$

$\Rightarrow 10^{-8.4} = [\text{OH}^-]$

$\Rightarrow [\text{OH}^-] = 3.981 \times 10^{-9} \text{ M}$

33. A sample of water contains an organic compound CaH$_{16}$O$_8$ at a concentration of $10^{-3}$ mol/litre. Given that the atomic weight of C = 12 g/mol, H = 1 g/mol, and O = 16 g/mol, the theoretical oxygen demand of water (in g of O$_2$ per litre, round off to two decimal places), is _______.

Ans. 0.256 g/l

34. A waste to energy plant burns dry solid waste of composition: Carbon = 35%, Oxygen = 26%, Hydrogen = 10%, Sulphur = 6%, Nitrogen = 3% and Inerts = 20%. Burning rate is 1000 tonnes/d. Oxygen in air by weight is 23%. Assume complete conversion of Carbon to CO$_2$, Hydrogen to H$_2$O, Sulphur to SO$_2$ and Nitrogen to NO$_2$.

Given Atomic weights: H = 1, C = 12, N = 14, O = 16, S = 32

The stoichiometric (theoretical) amount of air (in tones/d, round off to the nearest integer) required for complete burning of this waste, is _______.

Ans. 6965.2

Sol. Carbon to CO$_2$:

$$\text{C} + \text{O}_2 \rightarrow \text{CO}_2$$

1 mole of C$_8$H$_{16}$O$_8$ require 8 mole of O$_2$

$\therefore 10^{-3} \text{ mole/l require} = 8 \times 10^{-3} \text{ mole/l}$

$8 \times 10^{-3} = \frac{x}{32} \Rightarrow x = 0.256 \text{ g/l}$

35. A constant-head permeability test was conducted on a soil specimen under a hydraulic gradient of 2.5. The soil specimen has specific gravity of 2.65 and

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saturated water content of 20%. If the coefficient of permeability of the soil is 0.1 cm/s, the seepage velocity (in cm/s, round off to two decimal places) through the soil specimen is ______.

**Ans.** 0.7217

**Sol.**

\[ V_{\text{discharge}} = K_i \]

\[ = 0.1 \times 2.5 \]

\[ = 0.25 \text{ cm/sec} \]

\[ V_{\text{seepage}} = \frac{V_{\text{discharge}}}{n} \]

\[ n = \frac{e}{1+e} = \frac{0.53}{1+0.53} = 0.3464 \]

\[ S_e = W_G \]

\[ 1-e = 0.2 \times 2.65 \]

\[ e = 0.53 \]

\[ V_{\text{seepage}} = \frac{0.25}{0.3464} \]

\[ V_{\text{seepage}} = 0.7217 \]

36. Crops are grown in a field having soil, which has field capacity of 30% and permanent wilting point of 13%. The effective depth of root zone is 80 cm. Irrigation water is supplied when the average soil moisture drops to 20%. Consider density of the soil as 1500 kg/m³ and density of water as 1000 kg/m³. If the daily consumptive use of water for the crops is 2 mm, the frequency of irrigating the crops (in days), is

A. 13  
B. 10  
C. 11  
D. 7

**Ans.** A

**Sol.** Given: Final capacity = 30%

Permanent wilting point = 13%

Depth of root zone = 80 cm

Density of soil = 1500 kg/m³

Density of water = 1000 kg/m³

Consumptive use = Cu = 2 mm

\[ d = \frac{\delta \times d_x \times (FC - PWP) \times D}{\delta_w} \]

\[ d = \frac{1500 \times 0.8 \times (0.3 - 0.13) \times 0.8}{1000} = 163.2 \text{ mm} \]

\[ F_{01} = \frac{d}{Cu} = \frac{164}{2} = 82 \text{ days} \]

(No option matching)

37. The Fourier series to represent \( x - x^2 \) for \( -\pi \leq x \leq \pi \) is given by

\[ x - x^2 = a_0 + \sum_{n=1}^{\infty} a_n \cos nx + \sum_{n=1}^{\infty} b_n \sin nx \]

The value of \( a_0 \) (round off to two decimal places), is ______.

**Ans.** -6.58

**Sol.** Comparing the above equation with standard trigonometric farriers series representation,

\[ f(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} a_n \cos nx + \sum_{n=1}^{\infty} b_n \sin nx \]

\[ a_0 = \frac{1}{2\pi} \int_{-\pi}^{\pi} f(x) dx \]

\[ a_0 = \frac{1}{2\pi} \int_{-\pi}^{\pi} (x - x^2) dx \]

\[ a_0 = \frac{1}{2\pi} \left[ \int_{-\pi}^{\pi} x dx - \int_{-\pi}^{\pi} x^2 dx \right] \]

\[ a_0 = \frac{1}{2\pi} \left[ \left. \frac{x^2}{2} \right|_{-\pi}^{\pi} - \left. \frac{x^3}{3} \right|_{-\pi}^{\pi} \right] \]

\[ a_0 = \frac{1}{2\pi} \left[ \left. \frac{\pi^2}{2} - \frac{\pi^2}{2} \right] - \left. \frac{\pi^3}{3} - \frac{\pi^3}{3} \right] \]

\[ a_0 = \frac{1}{2\pi} \left[ -2\pi^3 \right] \]

\[ a_0 = -\frac{1}{2\pi} \times 2\pi^3 \]

\[ a_0 = -\frac{\pi^2}{3} \]

\[ a_0 = -\frac{\pi^2}{3} \]

\[ a_0 = -\frac{2\pi^3}{3} \]

38. A prismatic linearly elastic bar of length \( L \), cross-sectional area \( A \), and made up of a material with Young’s modulus \( E \), is subjected to axial tensile force as shown in the figures. When the bar is subjected
to axial tensile forces $P_1$ and $P_2$, the strain energies stored in the bar are $U_1$ and $U_2$, respectively.

If $U$ is the strain energy stored in the same bar when subjected to an axial tensile force $(P_1 + P_2)$, the correct relationship is

A. $U > U_1 + U_2$
B. $U = U_1 - U_2$
C. $U < U_1 + U_2$
D. $U = U_1 + U_2$

Ans. A

Sol.

$U_1 = \frac{P_1^2 \ell}{2AE}$

$U_2 = \frac{P_2^2 \ell}{2AE}$

$U = \frac{(P_1 + P_2)^2 \ell}{2AE}$

$U = \frac{P_1^2 \ell}{2AE} + \frac{P_2^2 \ell}{2AE} + \frac{P_1 P_2 \ell}{AE}$

$\therefore U > U_1 + U_2$

39. Group-I gives a list of test methods for evaluating properties of aggregates. Group-II gives the list of properties to be evaluated.

<table>
<thead>
<tr>
<th>Group-I: Test methods</th>
<th>Group-II: Properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>P. Soundness test</td>
<td>1. Strength</td>
</tr>
<tr>
<td>Q. Crushing test</td>
<td>2. Resistance to weathering</td>
</tr>
<tr>
<td>R. Los Angeles abrasion test</td>
<td>3. Adhesion</td>
</tr>
<tr>
<td>S. Stripping value test</td>
<td>4. Hardness</td>
</tr>
</tbody>
</table>

The correct match of test methods under Group-I to properties under Group-II, is

A. P-2; Q-1; R-4; S-3
B. P-2; Q-4; R-3; S-1
C. P-4; Q-1; R-2; S-3
D. P-3; Q-4; R-1; S-2

Sol. A

40. The plane truss has hinge supports at P and W and is subjected to the horizontal forces as shown in the figure (not drawn to the scale)
Representing the tensile force with ‘+’ sign and the compressive force with ‘–’ sign, the force in member XW (in kN, round off to the nearest integer), is _______.

Ans. –30 kN

Sol. First find support reaction

Chose the section as shown above and take the FBD of structure above the section X-X

For the above FBD apply \( \Sigma M_Q = 0 \)
\( (10 \times 4) + (10 \times 8) + F_{xw}[4] = 0 \)
\( F_{xw} = -30 \text{ kN} \) (Compression force)

Sign convention while writing equilibrium equation.

41. Joints I, J, K, L, Q and M of the frame shown in the figure (not drawn to the scale) are pins. Continuous members IQ and LJ are connected through a pin at N. Continuous members JM and KQ are connected through a pin at P. The frame has hinge supports at joints R and S. The loads acting at joints I, J and K are along the negative Y direction and the loads acting at joints L and M are along the positive X direction.

The magnitude of the horizontal component of reaction (in kN) at S, is

A. 5  
B. 10  
C. 20  
D. 15

Ans. B

42. A 5 m high vertical wall has a saturated clay backfill. The saturated unit weight and cohesion of clay are 18 kN/m\(^3\) and 20 kPa, respectively. The angle of internal friction of clay is zero. In order to prevent development of tension zone, the height of the wall is required to be increased. Dry sand is used as backfill above the clay for the increased portion of the wall. The unit weight and angle of internal friction of sand are 16 kN/m\(^3\) and 30\(^\circ\), respectively. Assume that the back of the wall is smooth and top of the backfill is horizontal. To prevent the development of tension zone, the minimum height (in m, round off to one decimal place) by which the wall has to be raised, is

Ans. 2.5
43. A footing of size 2 m × 2 m transferring a pressure of 200 kN/m², is placed at a depth of 1.5 m below the ground as shown in the figure (not drawn to the scale). The clay stratum is normally consolidated. The clay has specific gravity of 2.65 and compression index of 0.3.

Considering 2:1 (vertical to horizontal) method of load distribution and $\gamma_w = 10$ kN/m³, the primary consolidation settlement (in mm, round off to two decimal places) of the clay stratum is ______.

**Ans.** 74.27

**Sol.**

For CLAY

\[
\gamma_{SAT} = \left( \frac{G + e}{1 + e} \right) \gamma_w = \left( \frac{2.65 + e}{1 + e} \right) \times 10
\]

= 17 kN/m²

\(e_0 = 1.357\)

\(H_0 = 1.5\) m

\(\sigma_0 AT x x = 24d + 0.54\) sant + 0.754 SAT – 1.25 \(\gamma_w\)

\(= 39.25\) kN/m²

\[\Delta \sigma = \frac{qB^2}{(B + 2n)^2} = \frac{\text{force}}{\text{Area}} = \frac{200 \times 2 \times 2}{\left(2 + \frac{1}{2} \times 1.75\right)^2} \Delta \sigma = 56.88\] kN/m²

\[\Delta H = \frac{C_H b}{1 + e_0} \log \left( \frac{\sigma_0 + \Delta \sigma}{\sigma_0} \right)
\]

\[= \frac{1.5 \times 0.3}{1 + 1.357} \log \left( \frac{39.25 + 56.88}{39.25} \right)\]

\(\Delta H = 74.27\) mm

44. A hydraulic jump occurs in a triangular (V-shaped) channel with side slopes 1:1 (vertical to horizontal). The sequent depths are 0.5 m and 1.5 m. The flow rate (in m³/s, round off to two decimal places) in the channel is _______.

**Ans.** 1.728 m³/sec

**Sol.** In case of V shaped channel, flow rate can be given as
Flow rate \( Q = y_1 y_2 \sqrt{\frac{g}{3} \left( \frac{y_3^2 - y_1^2}{y_2^2 - y_1^2} \right)} \)

\[ Q = 0.5 \times 1.5 \sqrt{9.81 \left( \frac{1.5^3 - 0.5^3}{1.5^2 - 0.5^2} \right)} \]

\[ Q = 1.728 \text{ m}^3/\text{sec} \]

45. The planar structure RST shown in the figure is roller-supported at S and pin-supported at R. Members RS and ST have uniform flexural rigidity (EI) and S is a rigid joint. Consider only bending deformation and neglect effects of self-weight and axial stiffening.

\[ \int M_x \cdot m_x \cdot dx \quad \text{Take “R” as the origin} \]

\( M_x \to \text{B.M due to applied loads/moments in the idealised structure} \)

\( m_x \to \text{B.M in the given structure due to unit load alone} \)

\[ \theta_R = \frac{P}{L} \left( \frac{dx}{EI} \right) \]

When the structure is subjected to a concentrated horizontal load \( P \) at the end \( T \), the magnitude of rotation at the support \( R \), is

A. \( \frac{PL^2}{12EI} \)

B. \( \frac{PL}{6EI} \)

C. \( PL^2 \)

D. \( \frac{PL^3}{12EI} \)

Ans. A

Sol.

(Finding support reactions at “R” & “S”) Using unit load method

46. A concrete beam of span 15 m, 150 mm wide and 350 mm deep is prestressed with a parabolic cable as shown in the figure (not drawn to the scale). Coefficient of friction for the cable is 0.35, and coefficient of wave effect is 0.0015 per meter.

If the cable is tensioned from one end only, the percentage loss (round off to one decimal place) in the cable force due to friction, is _______.

Ans. 4.49

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The general solution of the above equation (with constants $C_1$ and $C_2$), is

A. $y(x) = C_1e^{\frac{x}{3}} + C_2e^{\frac{x}{2}}$

B. $y(x) = C_1e^{\frac{x}{3}} + C_2xe^{\frac{x}{2}}$

C. $y(x) = C_1e^{\frac{x}{3}} + C_2e^{\frac{x}{2}}$

D. $y(x) = C_1e^{\frac{x}{3}} + C_2e^{\frac{x}{2}}$

Ans. D

Sol. 

$$6\frac{d^2y}{dx^2} + \frac{dy}{dx} - y = 0$$

$$(6m^2 + m - 1) y = 0$$

$$m = \frac{d}{dx}$$

Auxiliary equation is

$$6m^2 + m - 1 = 0$$

$$6m^2 + 3m - 2m - 1 = 0$$

$$3m (2m + 1) - 1 (2m + 1) = 0$$

$$3m + 1 = 0$$

$$m = \frac{1}{2}, \frac{1}{3}$$

$$C.F. = C_1e^{\frac{1}{2}x} + C_2e^{\frac{1}{3}x}$$

$$P.I. = 0 \text{ as } f(x) = 0$$

General solution

$$y = C_1e^{\frac{1}{2}x} + C_2e^{\frac{1}{3}x}$$
Sol.

\[ \frac{PQ}{400} = \tan 7^\circ \]
\[ PQ = 49.113 \]
RL of B = 212.250 + 49.113 – 4
= 257.363 m

50. A 10 m high slope of dry clay soil (unit weight = 20 kN/m³), with a slope angle of 45° and the circular slip surface, is shown in the figure (not drawn to the scale). The weight of the slip wedge is denoted by W. The undrained unit cohesion (c_u) is 60 kPa.

The factor of safety of the slope against slip failure, is
A. 1.57  
B. 1.84  
C. 1.67  
D. 0.58
Ans. B

Sol. Area of circular Arc soil
\[ = \frac{Q}{360} \times \pi \times (10^2 - \frac{1}{2} \times 10 \times 10) \]
\[ = 28.59 \text{ m}^2 \]
Weight of wedge = volume \times y = Area \times 1 \times y = 28.54 \times 1 \times 20 = 570.8 \text{ kN}
FOS =
\[ \frac{\text{Restoring Moment}}{\text{Overturning Moment}} = \frac{60 \times 10 \times \pi / 4 \times 10}{570.8 \times 4.48} \]

51. A concrete dam holds 10 m of static water as shown in the figure (not drawn to the scale). The uplift is assumed to vary linearly from full hydrostatic head at the heel, to zero at the toe of dam. The coefficient of friction between the dam and foundation soil is 0.45. Specific weights of concrete and water are 24 kN/m³ and 9.81 kN/m³, respectively.

For NO sliding condition, the required minimum base width B (in m, round off to two decimal places) is __________.

Ans. 15.873

Sol. For no sliding, minimum width of dam
\[ B_{min} = \frac{H}{\mu(G - 1)} \]
Here H = 10 m
\[ \mu = 0.45 \]
G = 2.4
\[ \therefore B_{min} = \frac{10}{0.45(2.4 - 1)} = 15.873 \text{ m} \]

52. The design speed of a two-lane two-way road is 60 km/h and the longitudinal coefficient of friction is 0.36. The reaction time of a driver is 2.5 seconds. Consider acceleration due to gravity as 9.8 m/s². The intermediate sight distance (in m, round off to the nearest integer) required for the road is ________.

Ans. 162 m

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Sol. Given: \( V = 60 \text{ kmph} = 16.67 \text{ m/sec} \)
\( f = 0.36 \)
\( t = 2.5 \text{ sec} \)
\( g = 9.8 \text{ m/s}^2 \)
As we know, \( 1\text{SD} = 2\text{SSD} \) (stopping sight distance)
\[ \Rightarrow \text{SSD} = \frac{vt + \frac{v^2}{2gf}}{2} \]
\[ = 16.67 \times 2.5 + \frac{16.67^2}{2 \times 9.81 \times 0.36} \]
\[ = 41.675 + 39.34 = 81.01 \text{ m} \]
\( \therefore 1\text{SD} = 2 \times 81.01 = 162 \text{ m} \).

53. Alkalinity of water, in equivalent/litre (eq/litre), is given by
\[ \{\text{HCO}_3^-\} + 2\{\text{CO}_3^{2-}\} + \{\text{OH}^-\} - \{\text{H}^+\} \]
Where, \( \{ \} \) represents concentration in mol/litre. For a water sample, the concentrations of \( \text{HCO}_3^- = 2 \times 10^{-3} \text{ mol/litre}, \text{CO}_3^{2-} = 3.04 \times 10^{-4} \text{ mol/litre} \) and the pH of water = 9.0. The atomic weights are: Ca = 40; C = 12; and O = 16. If the concentration of \( \text{OH}^- \) and \( \text{H}^+ \) are NEGLECTED, the alkalinity of the water sample (in mg/litre as \( \text{CaCO}_3 \)), is
A. 50.0         B. 130.4
C. 100.0        D. 65.2

Ans. B

Sol. We know
\[ \text{HCO}_3^- = 2 \times 10^{-3} \text{ mol/litre} \]
\[ \text{CO}_3^{2-} = 3.04 \times 10^{-4} \text{ mol/litre} \]
According to question neglecting \( \text{OH}^- \) and \( \text{H}^+ \),
Alkalinity of water = \( (2 \times 10^{-3} + 2 \times 3.04 \times 10^{-4}) \times 130.4 = 2.608 \times 10^{-3} \text{ eq/litre} \)
In terms of \( \text{ca}_3\),
Alkalinity of water = \( 2.608 \times 10^{-3} \times 50 \text{ gm/litre} \)
\( \therefore \text{Alkalinity} = 130.4 \text{ mg/litre as } \text{CaCO}_3 \).

54. The cross-section of the reinforced concrete beam having an effective depth of 500 mm is shown in the figure (not drawn to the scale). The grades of concrete and steel used are M35 and Fe550, respectively. The area of tension reinforcement is 400 mm². It is given that corresponding to 0.2% proof stress, the material safety factor is 1.15 and the yield strain of Fe550 steel is 0.0044.

As per IS 456:2000, the limiting depth (in mm, round off to the nearest integer) of the neutral axis measured from the extreme compression fiber, is ______.

Ans. 221.52 mm

Sol. We know
\[ \text{D} = 500 \text{ mm} = \text{Effective depth} \]
Strain block@ Balanced failure
\[ 0.0044 = \left[ 0.002 + \frac{0.87f}{E_s} \right] \]
From similar triangles properties
\[ 0.0035 = \frac{0.0044}{(x_u)\lim} \]
\( (x_u)\lim = \frac{d - (x_u)\lim}{d} \times d = 500 \text{ mm} \)
\( x_u \lim = 221.52 \text{ mm} \)

55. A theodolite was set up at a station P. The angle of depression to a vane 2 m above the foot of a staff held at another station Q was 45°. The horizontal distance between stations P and Q is 20 m. The staff reading at a benchmark S of RL 433.050 m is 2.905 m. Neglecting the errors due to curvature and refraction, the RL of the station Q (in m), is
A. 413.955  
B. 413.050  
C. 431.050  
D. 435.955

**Ans.** A

**Sol.**

\[
\frac{x}{20} = \tan 45
\]

\[x = 20
\]

\[RL \ d \ Q = 433.05 + 2.905 - x - 2
\]

\[= 413.955 \ m
\]
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