



POST CLASS NOTES

Constructions



Topics



1. Division of a line segment in the given ratio
2. Construction of similar triangles
3. Construction of pair of tangents



1. Division of a Line Segment in the Given Ratio

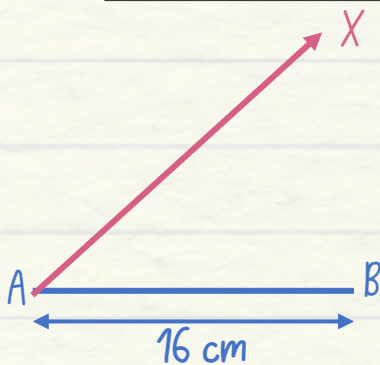
Let's divide a line segment of length 16 cm in the ratio 5:3.

Step 1: Draw $AB = 16$ cm.



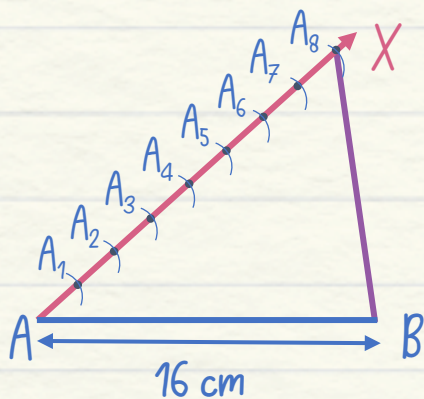
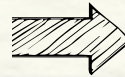
Step 2:

Draw a ray AX making an acute angle with AB .

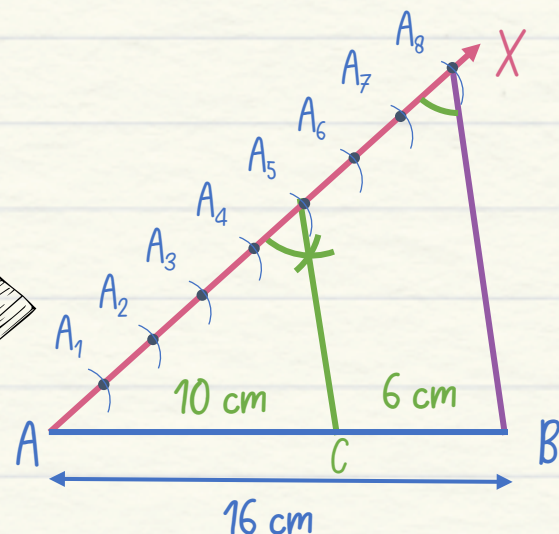


Step 3:

Locate 8 ($= 5 + 3$) points on ray AX such that $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = \dots = A_7A_8$.



Step 4: Join BA_8 .



Step 5:

Draw a line parallel to BA_8 from point A_5 (by making an angle equal to $\angle AA_8B$) intersecting AB at the point C .

Then, $AC:CB = 5:3$

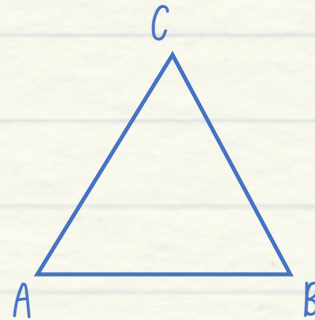
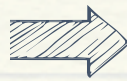
2. Construction of Similar Triangles

2.1 Scale Factor > 1

To construct a triangle whose sides are $\frac{5}{2}$ times the corresponding sides of the given $\triangle ABC$.

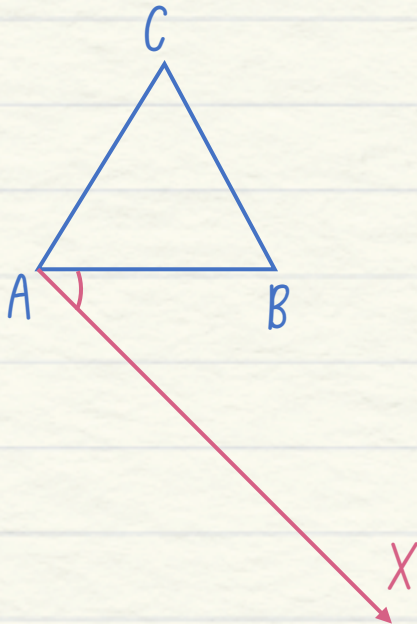
Step 1:

Draw given $\triangle ABC$.



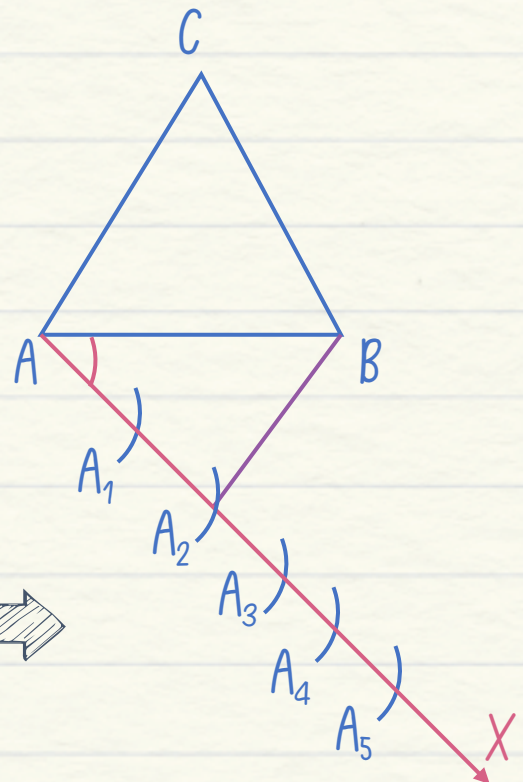
Step 2:

Draw any ray AX making an acute angle with AB on the side opposite of the vertex C .



Step 3:

Locate 5 (the greater part of 5 and 2 in $\frac{5}{2}$) points A_1, A_2, A_3, A_4 and A_5 on AX such that $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5$.



Step 4:

Step 4: Join A_2B .

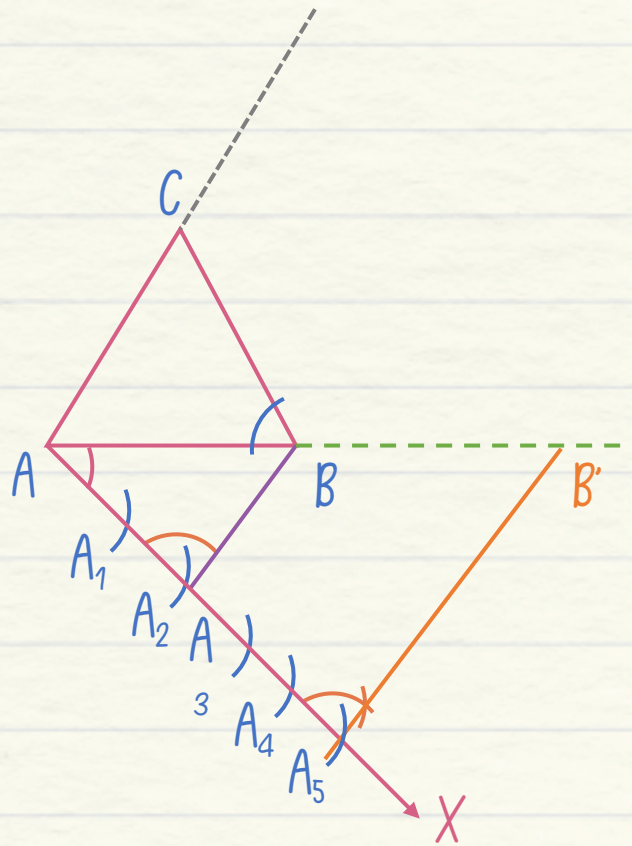
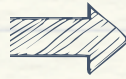


Step 5:

Extend AB to right side of point B .

Step 6:

Draw a line through A_5 parallel to A_2B which intersects AB at B' .

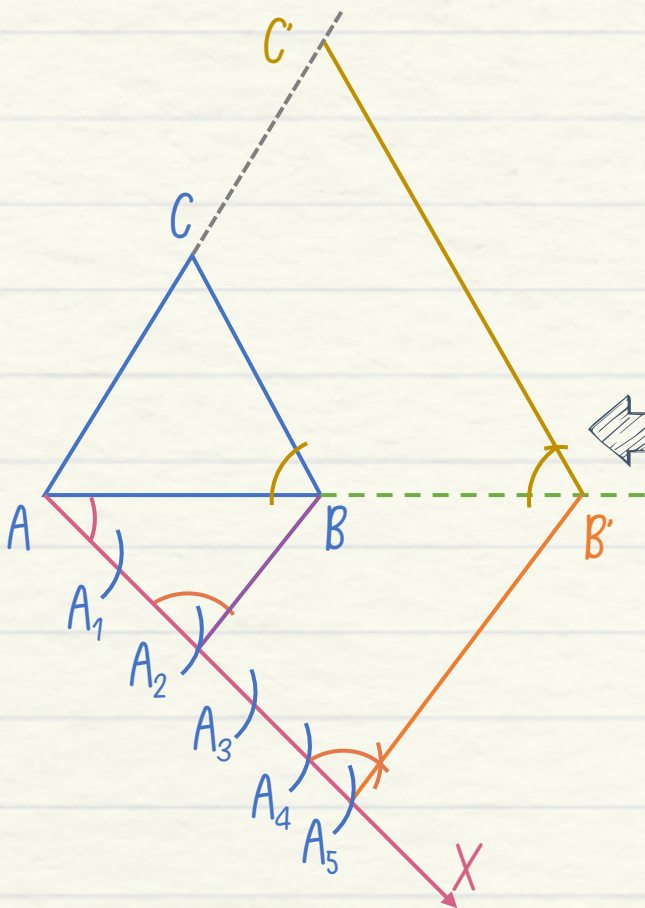


Step 7:

Produce the line AC to the right of point C .

Step 8:

Draw a line through B' parallel to the line BC to intersect AC at C' .



The $\triangle AB'C'$ has sides that are $\frac{5}{2}$ times the corresponding sides of the given $\triangle ABC$.

2.2 Scale Factor < 1

To construct a triangle whose sides are $\frac{2}{5}$ times the corresponding sides of the given $\triangle ABC$.

Same first 3 steps as the construction of triangle with $SF > 1$.

Step 4:

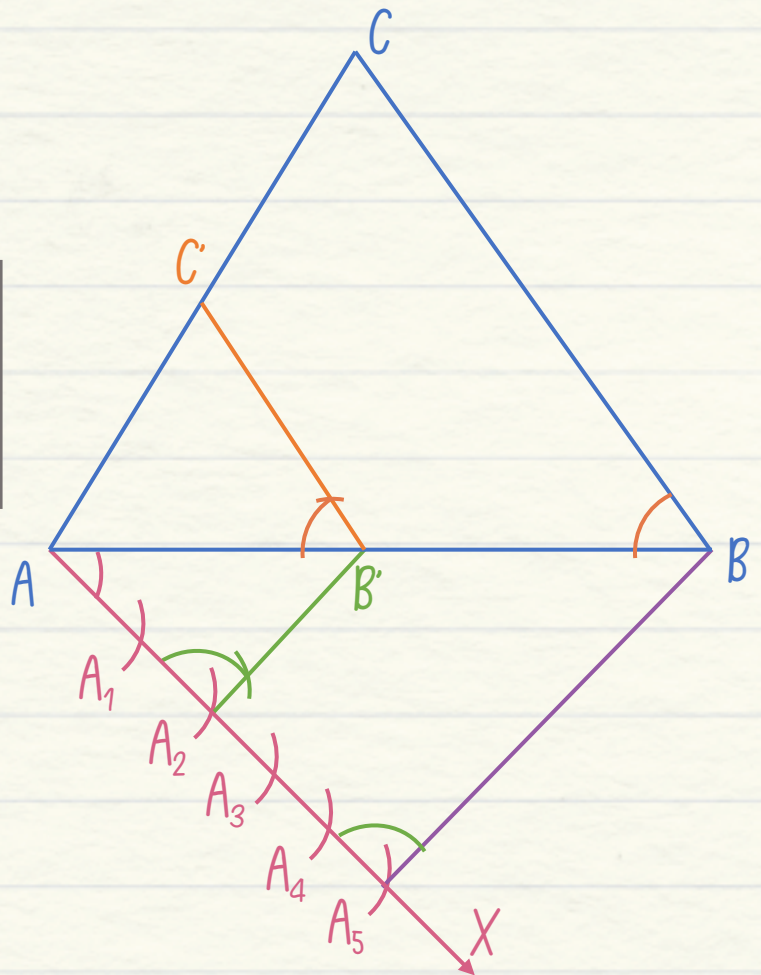
Join A_5B .

Step 5:

Draw a line through A_2 parallel to A_5B to intersect AB at B' .

Step 6:

Draw a line through B' parallel to the line BC to intersect AC at C' .

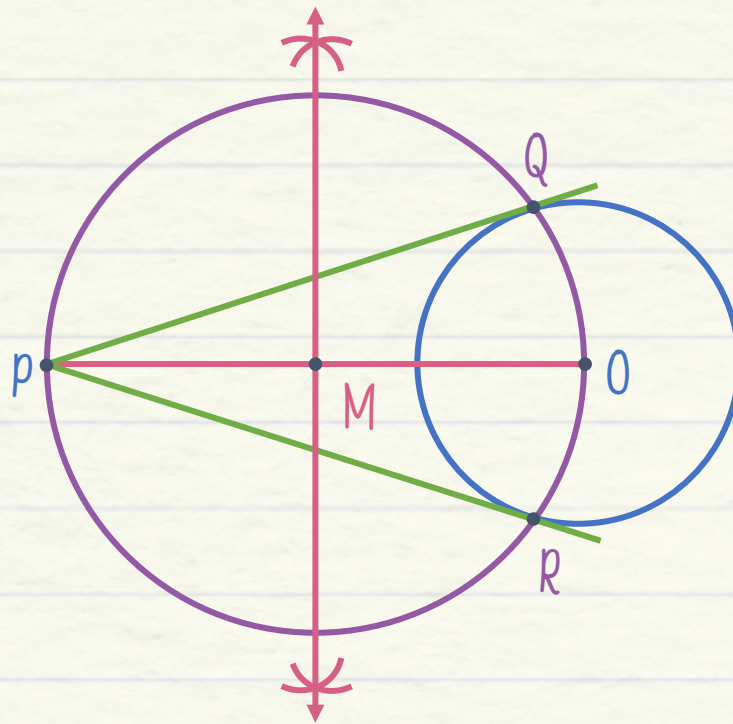


The $\triangle AB'C'$ has sides that are $\frac{2}{5}$ times the corresponding sides of the given $\triangle ABC$.

3. Construction of Pair of Tangents

To construct the tangents to a circle from a point (say P) outside it.

Given: A point P outside the circle of centre O .



Step 1:

Join PO and draw a perpendicular bisector of PO in order to locate its midpoint. Let's say M is the midpoint of PO .

Step 2:

Taking M as centre and MO (or MP) as radius, draw a circle. Let it intersect the given circle at the points Q and R .

Step 3:

Join PQ and PR .



Mind Map

