Exercise 1.1

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1. Using appropriate properties find.

(i) $-2/3 \times 3/5 + 5/2 - 3/5 \times 1/6$ Solution: $-2/3 \times 3/5 + 5/2 - 3/5 \times 1/6$ $= -2/3 \times 3/5 - 3/5 \times 1/6 + 5/2$ (by commutativity) = 3/5 (-2/3 - 1/6) + 5/2= 3/5 ((-4 - 1)/6) + 5/2= 3/5 ((-5)/6) + 5/2 (by distributivity) = -15/30 + 5/2= -1/2 + 5/2= 4/2= 2(ii) $2/5 \times (-3/7) - 1/6 \times 3/2 + 1/14 \times 2/5$ Solution:

Solution: $2/5 \times (-3/7) - 1/6 \times 3/2 + 1/14 \times 2/5$ $= 2/5 \times (-3/7) + 1/14 \times 2/5 - (1/6 \times 3/2)$ (by commutativity) $= 2/5 \times (-3/7 + 1/14) - 3/12$ $= 2/5 \times ((-6 + 1)/14) - 3/12$ $= 2/5 \times ((-5)/14)) - 1/4$ = (-10/70) - 1/4 = -1/7 - 1/4 = (-4-7)/28= -11/28

2. Write the additive inverse of each of the following

Solution:

(i) 2/8Additive inverse of 2/8 is - 2/8(ii) -5/9Additive inverse of -5/9 is 5/9(iii) -6/-5 = 6/5Additive inverse of 6/5 is -6/5(iv) 2/-9 = -2/9Additive inverse of -2/9 is 2/9(v) 19/-16 = -19/16Additive inverse of -19/16 is 19/16

3. Verify that: -(-x) = x for.
(i) x = 11/15
(ii) x = -13/17

Solution:

(i) x = 11/15We have, x = 11/15The additive inverse of x is - x (as x + (-x) = 0)Then, the additive inverse of 11/15 is -11/15(as 11/15 + (-11/15) = 0)The same equality 11/15 + (-11/15) = 0, shows that the additive inverse of -11/15 is 11/15. Or, -(-11/15) = 11/15i.e., -(-x) = x(ii) -13/17 We have, x = -13/17The additive inverse of x is – x (as x + (-x) = 0)Then, the additive inverse of -13/17 is 13/17(as 11/15 + (-11/15) = 0)The same equality (-13/17 + 13/17) = 0, shows that the additive inverse of 13/17 is -13/17. Or, -(13/17) = -13/17,i.e., -(-x) = x4. Find the multiplicative inverse of the (i) -13 (ii) -13/19 $(iv) - 5/8 \times (-3/7)$ (iii) 1/5 $(v) - 1 \times (-2/5)$ (vi) -1 Solution: (i) -13 Multiplicative inverse of -13 is -1/13 (ii) -13/19 Multiplicative inverse of -13/19 is -19/13 (iii) 1/5 Multiplicative inverse of 1/5 is 5 $(iv) - 5/8 \times (-3/7) = 15/56$ Multiplicative inverse of 15/56 is 56/15 $(v) - 1 \times (-2/5) = 2/5$ Multiplicative inverse of 2/5 is 5/2(vi) -1 Multiplicative inverse of -1 is -1 5. Name the property under multiplication used in each of the following.

(i) $-4/5 \times 1 = 1 \times (-4/5) = -4/5$ (ii) $-13/17 \times (-2/7) = -2/7 \times (-13/17)$ (iii) $-19/29 \times 29/-19 = 1$ Solution: (i) $-4/5 \times 1 = 1 \times (-4/5) = -4/5$ Here 1 is the multiplicative identity. (ii) $-13/17 \times (-2/7) = -2/7 \times (-13/17)$ The property of commutativity is used in the equation (iii) $-19/29 \times 29/-19 = 1$ Multiplicative inverse is the property used in this equation.

6. Multiply 6/13 by the reciprocal of -7/16 Solution: Reciprocal of -7/16 = 16/-7 = -16/7According to the question, $6/13 \times (\text{Reciprocal of } -7/16)$

7. Tell what property allows you to compute $1/3 \times (6 \times 4/3)$ as $(1/3 \times 6) \times 4/3$ Solution:

 $1/3 \times (6 \times 4/3) = (1/3 \times 6) \times 4/3$

 $6/13 \times (-16/7) = -96/91$

Here, the way in which factors are grouped in a multiplication problem, supposedly, does not change the product. Hence, the Associativity Property is used here.

8. Is 8/9 the multiplication inverse of $-1\frac{1}{8}$? Why or why not?

Solution:

 $-1\frac{1}{8} = -9/8$

[Multiplicative inverse \Rightarrow product should be 1]

According to the question,

 $8/9 \times (-9/8) = -1 \neq 1$

Therefore, 8/9 is not the multiplicative inverse of $-\frac{1}{8}$.

9. If 0.3 the multiplicative inverse of $3\frac{1}{3}$? Why or why not? Solution:

 $3\frac{1}{3} = 10/3$ 0.3 = 3/10[Multiplicative inverse \Rightarrow product should be 1] According to the question, $3/10 \times 10/3 = 1$

Therefore, 0.3 is the multiplicative inverse of $3\frac{1}{3}$.

10. Write

(i) The rational number that does not have a reciprocal.

(ii) The rational numbers that are equal to their reciprocals.

(iii) The rational number that is equal to its negative.

Solution:

(i) The rational number that does not have a reciprocal is 0. Reason:

 $\dot{0} = 0/1$

Reciprocal of 0 = 1/0, which is not defined.

(ii) The rational numbers that are equal to their reciprocals are 1 and -1. Reason:

1 = 1/1

Reciprocal of 1 = 1/1 = 1 Similarly, Reciprocal of -1 = -1

(iii) The rational number that is equal to its negative is 0. Reason: Negative of 0=-0=0

11. Fill in the blanks.

(i) Zero has _____ reciprocal.

(ii) The numbers ______ and _____ are their own reciprocals

(iii) The reciprocal of – 5 is _____.

(iv) Reciprocal of 1/x, where $x \neq 0$ is _____.

(v) The product of two rational numbers is always a _____.

(vi) The reciprocal of a positive rational number is _____.

Solution:

(i) Zero has <u>no</u> reciprocal.

(ii) The numbers <u>-1</u> and <u>1</u> are their own reciprocals

(iii) The reciprocal of -5 is $-\frac{1}{5}$.

(iv) Reciprocal of 1/x, where $x \neq 0$ is <u>x</u>.

(v) The product of two rational numbers is always a rational number.

(vi) The reciprocal of a positive rational number is <u>positive</u>.

Exercise 1.2

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1. Represent these numbers on the number line.

(i) 7/4

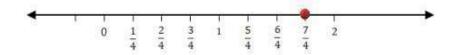
(ii) -5/6

Solution:

(i) 7/4

Dívide the line between the whole numbers into 4 parts. i.e., divide the line between 0 and 1 to 4 parts, 1 and 2 to 4 parts and so on.

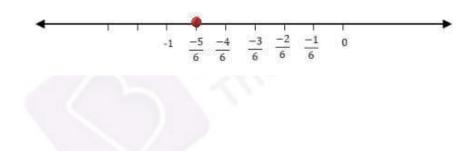
Thus, the rational number 7/4 lies at a distance of 7 points away from 0 towards positive number line.



(ii) -5/6

Divide the line between the integers into 4 parts. i.e., divide the line between 0 and -1 to 6 parts, -1 and -2 to 6 parts and so on. Here since the numerator is less than denominator, dividing 0 to -1 into 6 part is sufficient.

Thus, the rational number -5/6 lies at a distance of 5 points, away from 0, towards negative number line

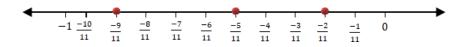


2. Represent -2/11, -5/11, -9/11 on a number line.

Solution:

Divide the line between the integers into 11 parts.

Thus, the rational numbers -2/11, -5/11, -9/11 lies at a distance of 2, 5, 9 points away from 0, towards negative number line respectively.



3. Write five rational numbers which are smaller than 2.

Solution:

The number 2 can be written as 20/10 Hence, we can say that, the five rational numbers which are smaller than 2 are:

2/10, 5/10, 10/10, 15/10, 19/10

4. Find the rational numbers between -2/5 and $\frac{1}{2}$.

Solution:

Let us make the denominators same, say 50. $-2/5 = (-2 \times 10)/(5 \times 10) = -20/50$ $\frac{1}{2} = (1 \times 25)/(2 \times 25) = 25/50$ Ten rational numbers between -2/5 and $\frac{1}{2}$ = ten rational numbers between -20/50 and 25/50Therefore, ten rational numbers between -20/50 and 25/50 = -18/50, -15/50, -5/50, -2/50, 4/50, 5/50, 8/50, 12/50, 15/50, 20/50

5. Find five rational numbers between.

(i) 2/3 and 4/5(ii) -3/2 and 5/3 (iii) $\frac{1}{4}$ and $\frac{1}{2}$ Solution: (i) 2/3 and 4/5Let us make the denominators same, say 60 i.e., 2/3 and 4/5 can be written as: $2/3 = (2 \times 20)/(3 \times 20) = 40/60$ $4/5 = (4 \times 12)/(5 \times 12) = 48/60$ Five rational numbers between 2/3 and 4/5 = five rational numbers between 40/60 and 48/60 Therefore, Five rational numbers between 40/60 and 48/60 = 41/60, 42/60, 43/60, 44/60, 45/60 (ii) -3/2 and 5/3Let us make the denominators same, say 6 i.e., -3/2 and 5/3 can be written as: $-3/2 = (-3 \times 3)/(2 \times 3) = -9/6$

 $5/3 = (5 \times 2)/(3 \times 2) = 10/6$

Five rational numbers between -3/2 and 5/3 = five rational numbers between -9/6 and 10/6

Therefore, Five rational numbers between -9/6 and 10/6 = -1/6, 2/6, 3/6, 4/6, 5/6

(iii) ¹/₄ and ¹/₂ Let us make the denominators same, say 24. i.e., ¹/₄ and ¹/₂ can be written as: $\frac{1}{4} = (1 \times 6)/(4 \times 6) = 6/24$ $\frac{1}{2} = (1 \times 12)/(2 \times 12) = 12/24$ Five rational numbers between ¹/₄ and ¹/₂ = five rational numbers between 6/24 and 12/24 Therefore, Five rational numbers between 6/24 and 12/24 = 7/24, 8/24, 9/24, 10/24, 11/24

6. Write five rational numbers greater than -2.

Solution:

-2 can be written as – 20/10Hence, we can say that, the five rational numbers greater than -2 are -10/10, -5/10, -1/10, 5/10, 7/10

7. Find ten rational numbers between 3/5 and 3/4,

Solution:

Let us make the denominators same, say 80.

 $3/5 = (3 \times 16)/(5 \times 16) = 48/80$

 $3/4 = (3 \times 20)/(4 \times 20) = 60/80$

Ten rational numbers between 3/5 and 3/4 = ten rational numbers between 48/80 and 60/80Therefore, ten rational numbers between 48/80 and 60/80 = 49/80, 50/80, 51/80, 52/80, 54/80, 55/80, 56/80, 57/80, 58/80, 59/80