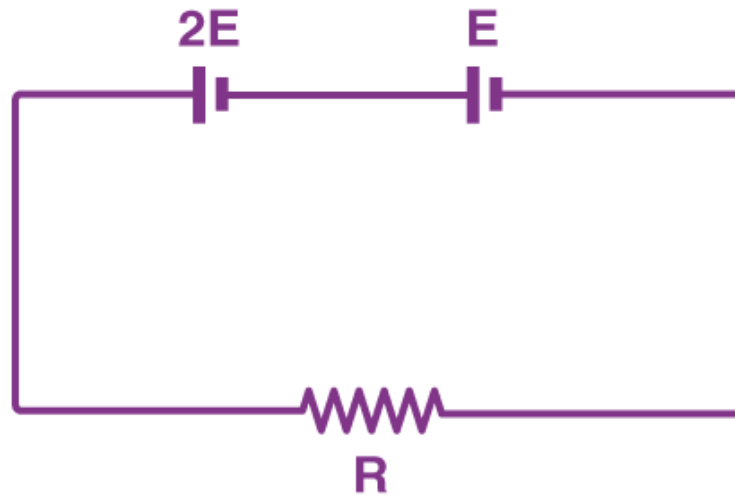


Question 1) Two cells of emf $2E$ and E with internal resistance r_1 and r_2 respectively are connected in series to an external resistor R (see figure). The value of R , at which the potential difference across the terminals of the first cell becomes zero is



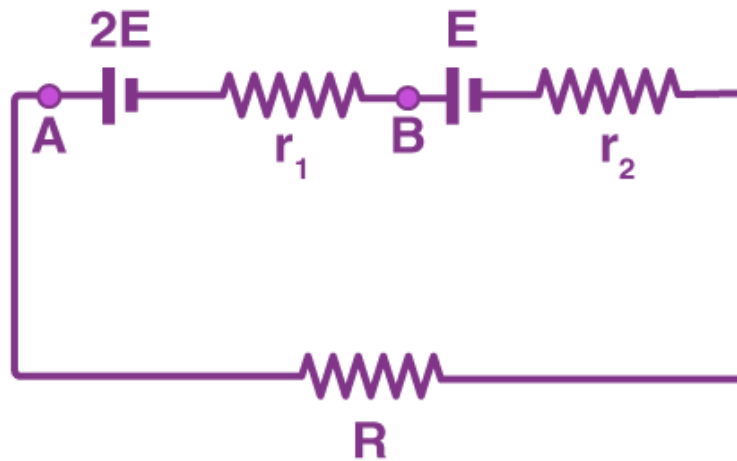
- (A) $r_1 - r_2$
- (B) $r_1 + r_2$
- (C) $(r_1/2) + r_2$
- (D) $(r_1/2) - r_2$

Answer (D)

Solution

$$i = \frac{3E}{R+r_1+r_2}$$

$$i = \frac{3E}{R+r_1+r_2}$$



$$i = \frac{3E}{R+r_1+r_2}$$



If potential difference across terminals of first cell is zero

$$V_A = V_B$$

$$2E = i r_1$$

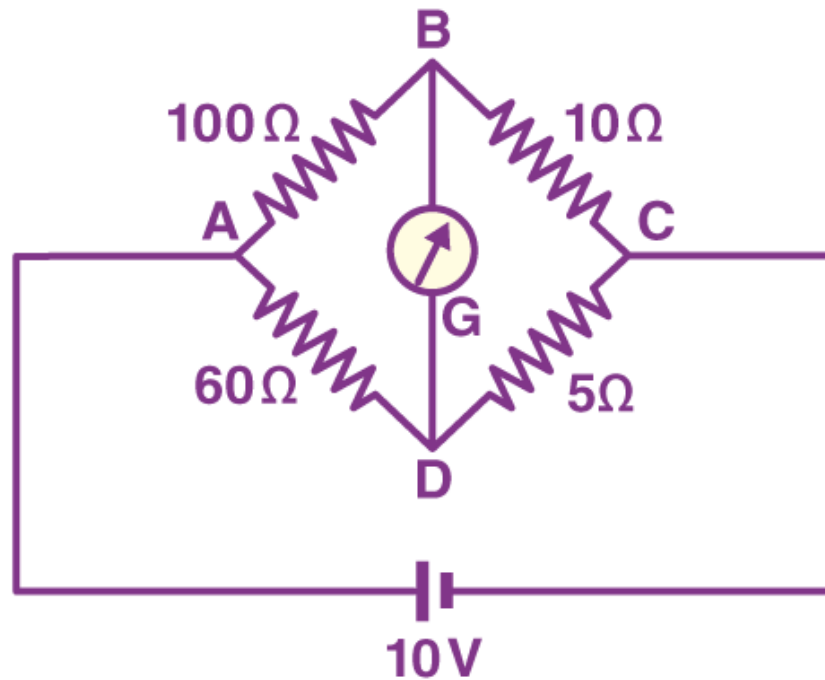
$$2E = \frac{3E}{R+r_1+r_2} r_1$$

$$2R + 2r_1 + 2r_2 = 3r_1$$

$$R = (r_1/2) - r_2$$

Question 2) The four arms of a Wheatstone bridge have resistances as shown in the figure. A galvanometer

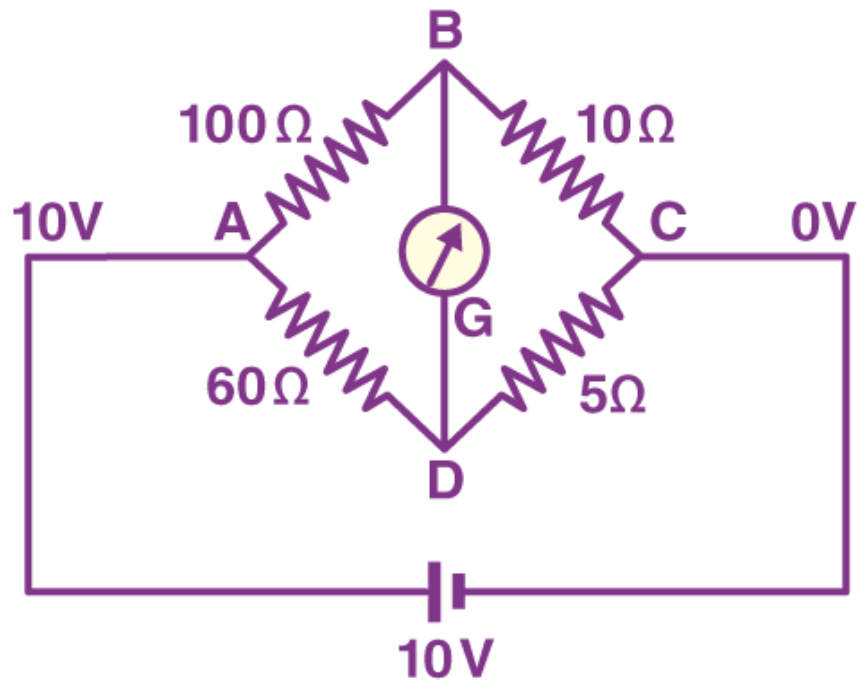
of 15 resistance is connected across BD. Calculate the current through the galvanometer when a potential difference of 10 V is maintained across AC.



- (A) 4.87 mA
- (B) 4.87 μ A
- (C) 2.44 μ A
- (D) 2.44 mA

Answer (A)

Solution:



Applying KCL for point B,

$$\frac{V_B - 10}{100} + \frac{V_B - V_D}{10} + \frac{V_B - 0}{60} = 0$$

$$\frac{V_B - 10}{20} + \frac{15(V_B - V_D)}{3} + \frac{V_B - 0}{2} = 0$$

$$3V_B - 30 + 20V_B - 20V_D + 30V_B = 0$$

$$53V_B - 20V_D = 30 \quad (1)$$

Similarly applying KCL for point D,

$$\frac{V_D - 10}{60} + \frac{V_D - V_B}{15} + \frac{V_D - 0}{5} = 0$$

$$V_D - 10 + 4V_D - 4V_B + 12V_D = 0$$

$$-4V_B + 17V_D = 10 \quad (2)$$

after solving equation (1) & (2)

$$V_D = 0.792 \text{ volt}$$

$$V_B = 0.865 \text{ volt}$$

Then the current through the galvanometer

$$= \frac{V_B - V_D}{R}$$

$$= \frac{0.865 - 0.792}{15}$$

$$= 4.67 \text{ mA}$$

Question 3) What happens to the inductive reactance and the current in a purely inductive circuit if the frequency is halved?

- (A) Both , including reactance and current will be doubled
- (B) Both, inductive reactance and current will be halved
- (C) Inductive reactance will be halved and current will be doubled
- (D) Inductive reactance will be doubled and current will be halved.

Answer: (C)

Solution

$$X_L = \omega L$$

If frequency is halved, $X'_L = (X_L/2)$

[inductive reactance is halved]

Therefore, $I = V/X_L$

& $I' = 2V/X_L = 2I$ [current will be doubled]

Question 4) The electric field intensity produced by the radiation coming from a 100 W bulb at a distance of 3 m is E. The electric field intensity produced by the radiation coming from 60 W at the same distance is $\sqrt{x/5}E$. Where the value of x = _____

Answer (3)

Solution:

The intensity of electromagnetic radiation

$$I = 1/2(C\epsilon_0 E^2)$$

where E is electric field intensity at a point

$$E^2 \propto I$$

$$I = \text{Power/Area}$$

$$E^2 \propto (P/A)$$

$$E \propto \sqrt{P}$$

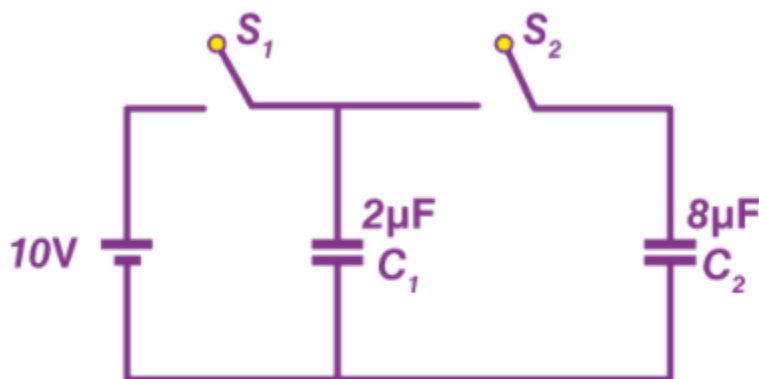
[at the same distance, A will be the same]

$$\frac{E'}{E} = \sqrt{\frac{60}{100}}$$

$$E' = \sqrt{\frac{3}{5}} E$$

So the value of $x = 3$

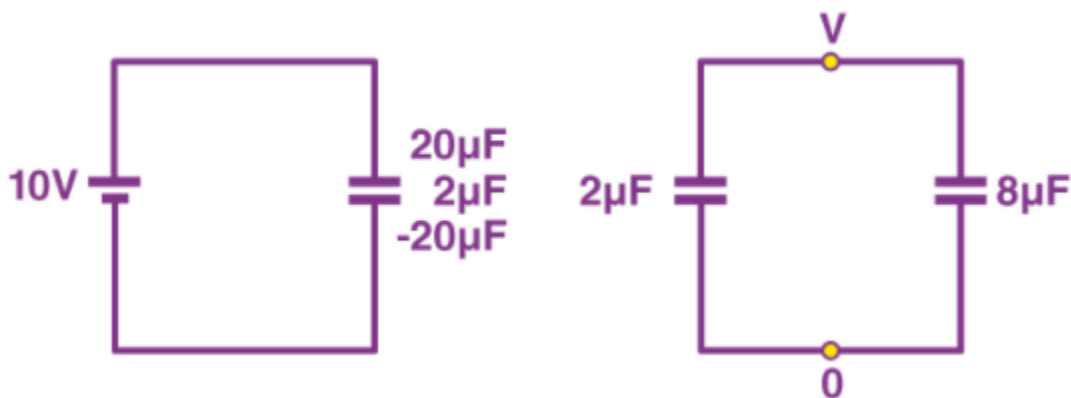
Question 5) A $2\mu\text{F}$ capacitor C_1 is first charged to a potential difference of 10V using a battery. Then the battery is removed and the capacitor is connected to an uncharged capacitor C_2 of $8\mu\text{F}$. The charge in C_2 on equilibrium conditions is _____ μC . (Round off to the Nearest Integer)



Answer (16)

Solution

After capacitor C_1 is fully charged,



When battery is removed & the capacitor is connected

At equilibrium condition, let voltage across each capacitor be V .

Then, using conservation of charge

$$2V + 8V = 20$$

$$10V = 20$$

$$V = 2 \text{ volt}$$

$$Q = CV$$

$$Q = 8 \times 2 = 16 \mu\text{C}$$

Question 6) The electric field in a region is given by $\vec{E} = \frac{2}{3}E_0\hat{i} + \frac{3}{5}E_0\hat{j}$ with $E_0 = 4.0 \times 10^3 \text{ N/C}$. The flux of this field through a rectangular surface are 0.4 m^2 parallel to $Y-Z$ plane is _____ Nm^2C^{-1} .

Answer (640)

Solution:

From Gauss' law

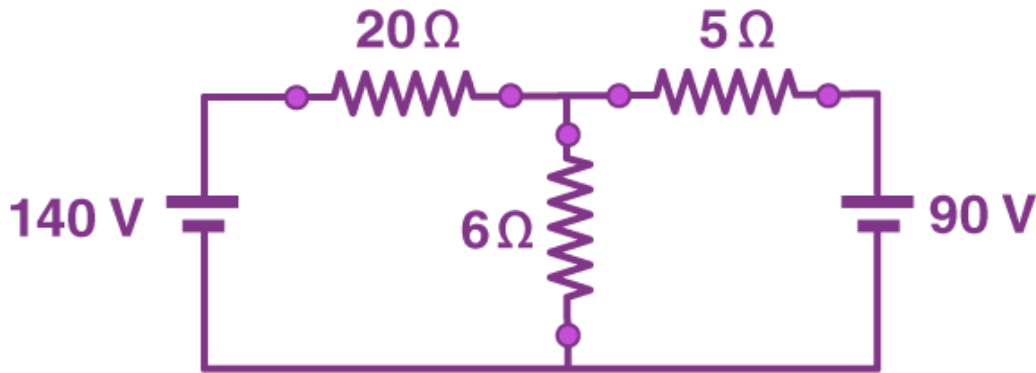
$$\phi = \oint \vec{E} \cdot d\vec{A}$$

$$= \left(\frac{2}{3}\right)E_0 \times (0.4)$$

$$= \left(\frac{2}{3}\right) \times 4 \times 10^3 \times 0.4$$

$$\Phi = 640 \text{ Nm}^2 \text{ c}^{-1}$$

Question 7) In the given circuit find the current through 6Ω resistance



- (A) 10 A
- (B) 7 A
- (C) 25 A
- (D) 30 A

Answer: (A) 10 A

Solution:

Applying Kirchoff's law,

$$\frac{V-140}{20} + \frac{V-0}{6} + \frac{V-90}{5} = 0$$

$$3(V-140)+10V+(V-90)=0$$

$$3V-420+10V+12V-1080=0$$

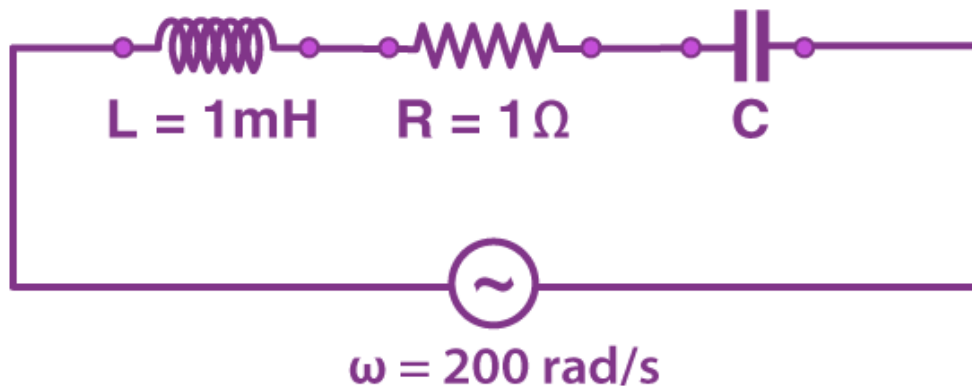
$$25V=1500$$

$$V=60$$

Current through 6Ω resistance, $I = V/R = 60/6 = 10 \text{ A}$

Question 8) An AC circuit consists of a series combination of an inductance L 1 mH, a resistance $R = 1\Omega$ and a capacitance C . It is observed that the current leads the voltage by 45° . Find the value of capacitance

'C' if the angular frequency of applied AC is 200 rad/s.



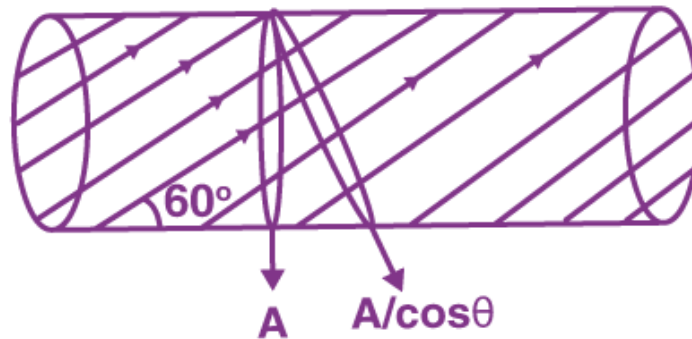
- (A) 5.6 mF
- (B) 3.92 mF
- (C) 4.16 mF
- (D) 5.2 mF

Answer: (C) 4.16 mF

Solution

$$\begin{aligned} \tan\Phi &= \frac{X_C - X_L}{R} = \frac{\frac{1}{\omega C} - \omega L}{R} \\ 1(1) &= \frac{1}{200C} - 200(10^{-3}) \\ \frac{1}{200C} &= 1 + 0.2 = 1.2 \\ C &= \frac{1}{200 \times 1.2} = 0.00416 \text{ F} = 4.16 \text{ mF} \end{aligned}$$

Question 9) In a magnesium rod of area 3 m^2 , current $I = 5 \text{ A}$ is flowing angle of 60° from the axis of the rod. The resistivity of the material is $44 \times 10^{-2} \text{ ohm x m}$. Find an electric field inside the rod



- (A) 0.567
- (B) 0.367
- (C) 0.667
- (D) 0.767

Answer: (B) 0.367

Solution

$$\frac{I}{A_{\text{effective}}} = \frac{E}{\rho}$$

$$E = \frac{\rho I}{A} \cos 60^\circ = \frac{44 \times 10^{-2} \times 5}{3 \times 2}$$

$$E = 0.367$$

Question 10) A RLC circuit is in its resonance condition. Its circuit components have value

$$R = 5\Omega, L = 2H, C = 0.5mF, V = 250V$$

Then find the power in the circuit.

- (A) 6 kW
- (B) 10 kW
- (C) 12 kW
- (D) 12.5 kW

Answer: (D)

Solution

A circuit is in resonance. Thus

$$\begin{aligned}X_L &= X_C \\ \therefore Z &= R \text{ so, } i_{rms} = \frac{V}{Z} = \frac{V}{R} \\ P &= i_{rms}^2 R \\ P &= \frac{V^2}{R} = \frac{250 \times 250}{5} = 12500 \frac{\text{J}}{\text{s}} = 12.5 \text{ kW}\end{aligned}$$

