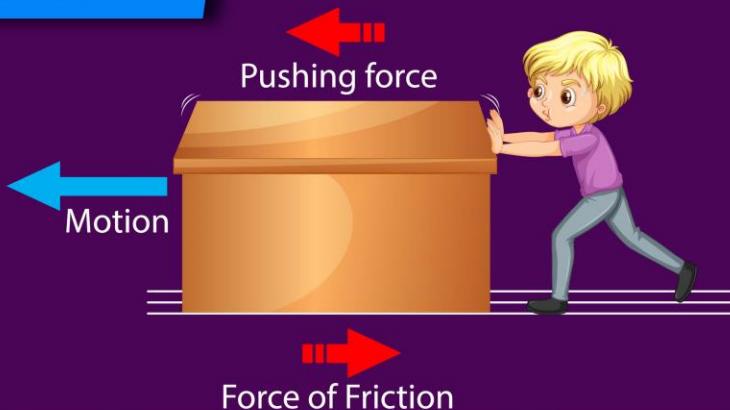


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**PHYSICS**



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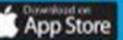
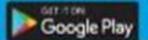
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**VIKAS SIR**

**CHEMISTRY | 3:00 PM**



**AKASH SIR**

**PHYSICS | 4:00 PM**



**SACHIN SIR**

**ZOOLOGY | 5:00 PM**



**PANKHURI MA'AM**

**BOTANY | 5:00, 6:00 PM**



**PUSHPENDU SIR**

**ZOOLOGY | 6:00 PM**





**Aakash**

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TUESDAY AND THURSDAY | 2 PM CHEMISTRY, 3 PM ZOOLOGY



AKASH SIR

PHYSICS | 2:00 PM



PANKHURI MA'AM

BOTANY | 3:00 PM



VIKAS SIR

CHEMISTRY | 2:00 PM



SACHIN SIR

ZOOLOGY | 3:00 PM



$\mu$  0.5

9/21/2022

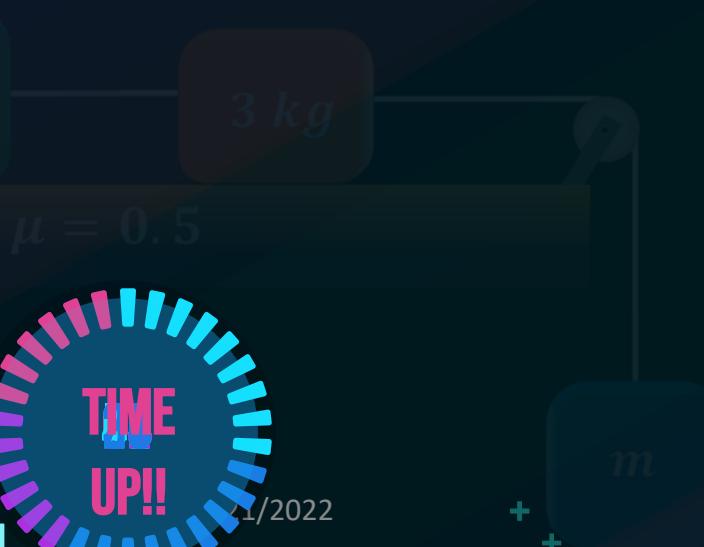
# EXAMPLE



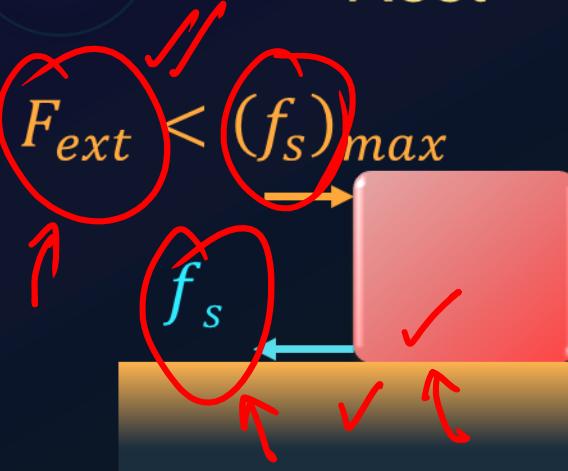
Which one of the following statements is incorrect ?

- a. Rolling friction is smaller than sliding friction.
- b. Limiting value of static friction is directly proportional to normal reaction.
- c. Frictional force opposes the relative motion.
- d. Coefficient of sliding friction has dimensions of length.

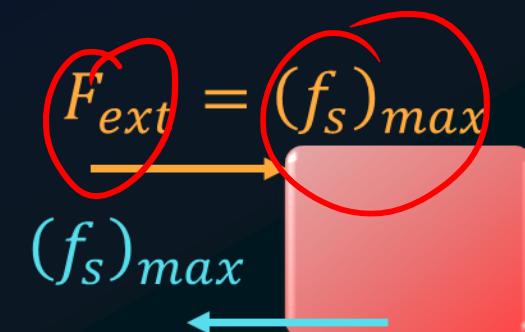
NEET-2018



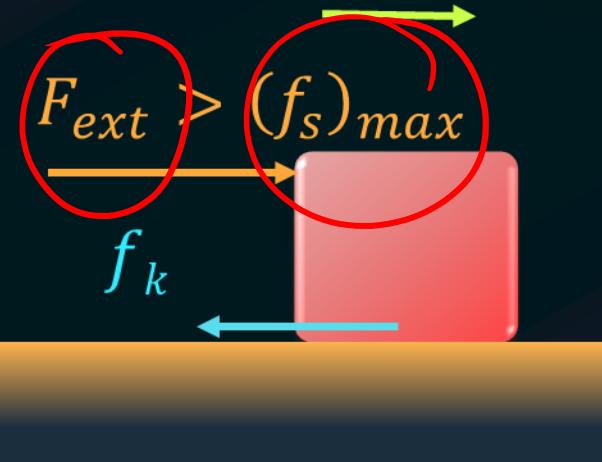
Rest



Just Slipping



Slipping



Coefficient of sliding friction has no dimension.

$$\mu = 0.5$$



# ANSWER



Which one of the following statements is incorrect ?

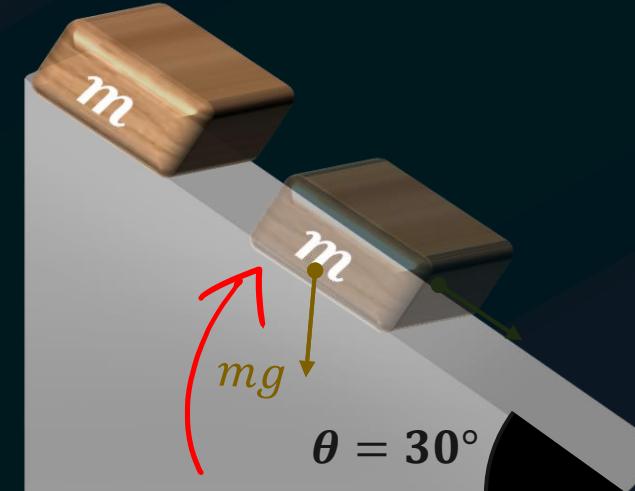
- a. Rolling friction is smaller than sliding friction.
- b. Limiting value of static friction is directly proportional to normal reaction.
- c. Frictional force opposes the relative motion.
- d. Coefficient of sliding friction has dimensions of length.



## EXAMPLE

A plank with a box on it at one end is gradually raised about the other end. As the angle of inclination with the horizontal reaches  $30^\circ$ , the box starts to slip and slides  $4 \text{ m}$  down the plank in  $4 \text{ s}$ . The coefficients of static and kinetic friction between the box and the plank will be, respectively

- a. 0.4 and 0.3
- b. 0.6 and 0.6
- c. 0.6 and 0.5
- d. 0.5 and 0.6



NEET-2015



# SOLUTION



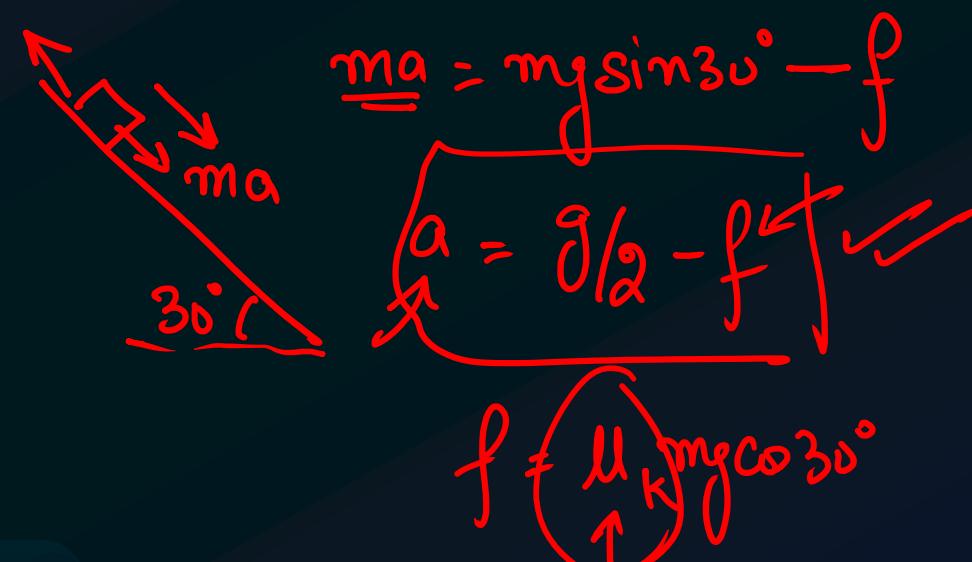
Given:  $t = 4 \text{ s}$ ,  $\theta = 30^\circ$ ,  $l = 4 \text{ m}$

Coefficient of static friction,

$$\mu_s = \tan 30^\circ$$

Coefficient of kinetic friction,

$$ma = mgs \sin 30^\circ - f$$


$$\begin{aligned} \cancel{ma} &= mgs \sin 30^\circ - f \\ a &= g/2 - f \\ f &= \mu_k m g \cos 30^\circ \end{aligned}$$

$$\mu = 0.5$$

# SOLUTION



Given:  $t = 4 \text{ s}$ ,  $\theta = 30^\circ$ ,  $l = 4 \text{ m}$

Coefficient of static friction is,

$$\underline{\underline{\mu_s}} = \tan 30^\circ = 0.577 \approx \underline{\underline{0.6}}$$

For coefficient of kinetic friction,

$$\begin{aligned} ma &= m g \sin 30^\circ - f \\ &= m g \sin 30^\circ - \mu_k m g \cos 30^\circ \dots \dots (1) \end{aligned}$$

and also using,  $S = ut + \frac{1}{2}at^2$   $\underline{\underline{a = 0.5 \text{ m/s}^2}}$

$$\Rightarrow 4 = 0 + \frac{1}{2}a(4)^2 \text{ or } a = 0.5 \text{ m/s}^2$$

Now from (1)

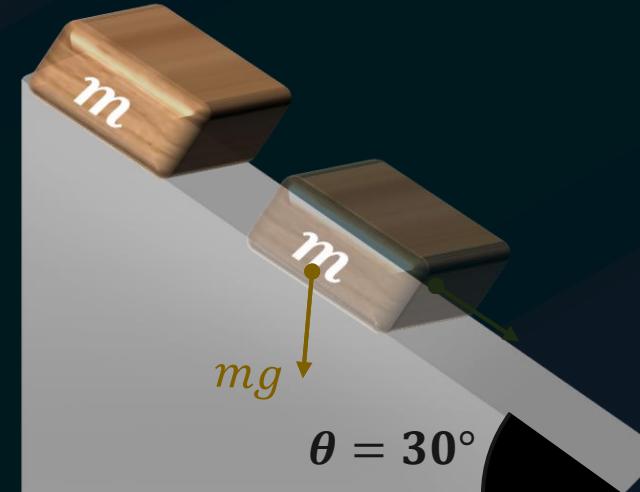
$$\begin{aligned} 0.5 &= 10 \times \frac{1}{2} - \mu_k (10) \left( \frac{\sqrt{3}}{2} \right) \\ \text{or } \mu_k &= \frac{4.5}{5\sqrt{3}} = \underline{\underline{0.5}} \end{aligned}$$

# ANSWER



A plank with a box on it at one end is gradually raised about the other end. As the angle of inclination with the horizontal reaches  $30^\circ$ , the box starts to slip and slides  $4\text{ m}$  down the plank in  $4\text{ s}$ . The coefficients of static and kinetic friction between the box and the plank will be, respectively

- a. 0.4 and 0.3
- b. 0.6 and 0.6
- c. 0.6 and 0.5**
- d. 0.5 and 0.6



# EXAMPLE

A system consists of three identical masses  $m_1, m_2$  and  $m_3$  connected by a string passing over a pulley  $P$ . The mass  $m_1$  hangs freely and  $m_2$  and  $m_3$  are on a rough horizontal table (the coefficient of friction =  $\mu$ ). The pulley is frictionless and of negligible mass. The downward acceleration of mass  $m_1$  is

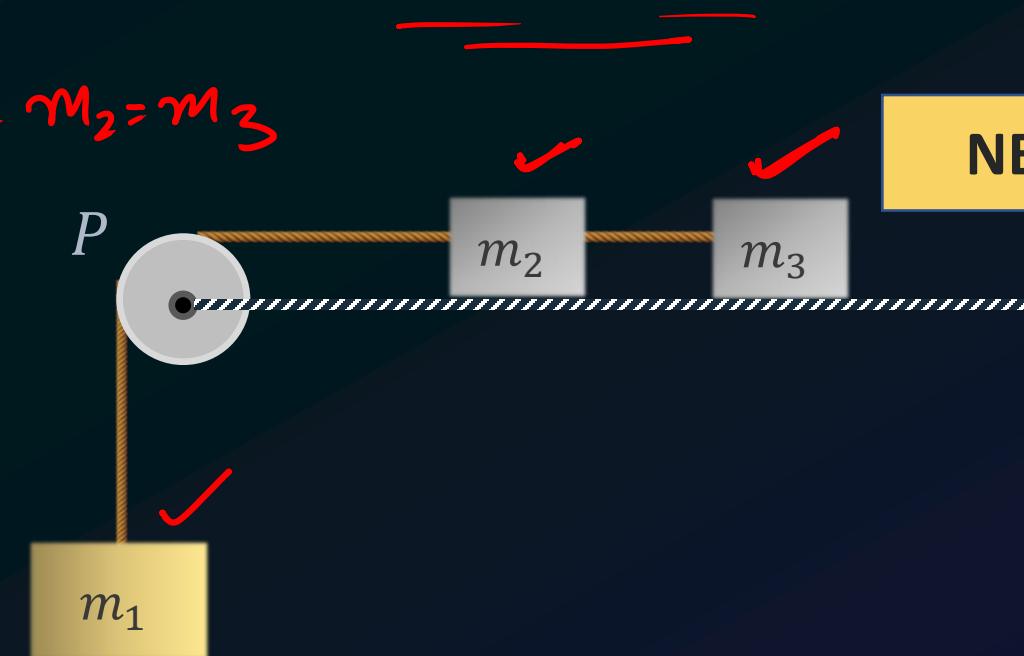
$$m_1 = m_2 = m_3$$

a.  $\frac{g(1 - 2\mu)}{g}$

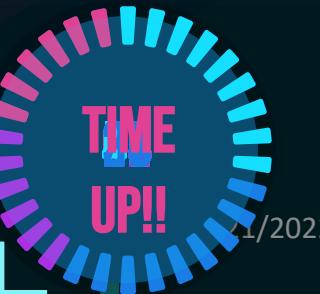
b.  $\frac{2g\mu}{3}$

c.  $\frac{g(1 - 2\mu)}{3}$

d.  $\frac{g(1 - 2\mu)}{2}$



NEET-2014



# SOLUTION



$$T - mg = ma \quad \checkmark$$

$$T - T' - f = ma \quad \checkmark$$

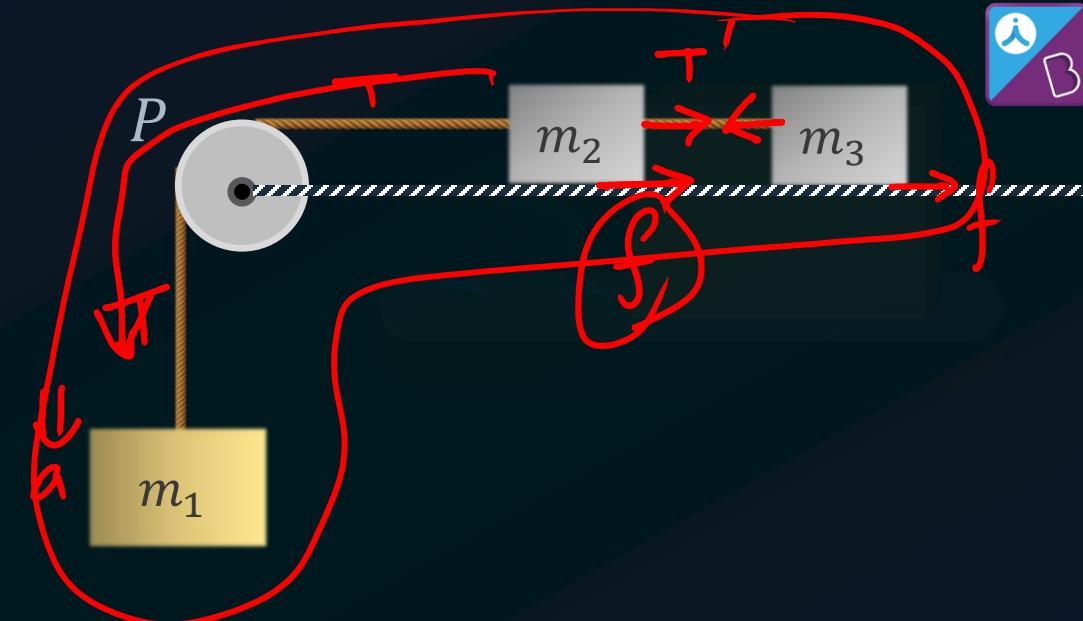
$$T' - f = ma \quad \checkmark$$

$$f = \mu mg \quad \checkmark$$

$\boxed{a}$

$$\frac{m_1g - (m_2 + m_3)g\mu}{m_1 + m_2 + m_3}$$

$$a = \frac{g - 2\mu g}{3} = \frac{g(1 - 2\mu)}{3}$$



$$\mu = 0.5$$

Tension in the string attached to mass  $m_1$  is  $T_1$  Tension in the string attached to mass  $m_3$  is  $T_2$

Apply newtons Second law, for each mass

$$m_1g - T_1 = m_1a \dots (1)$$

$$T_1 - f_2 - T_2 = m_2a \dots (2)$$

$$T_3 - f_3 = m_3a \dots (3)$$

Adding above equations,

$$m_1g - f_2 - f_3 = (m_1 + m_2 + m_3)a$$

As  $m_1 = m_2 = m_3 = m$  and  $f_2 = f_3 = \mu mg$

$$mg - 2\mu mg = 3ma$$
$$a = \frac{g(1-2\mu)}{3} \checkmark$$

# ANSWER



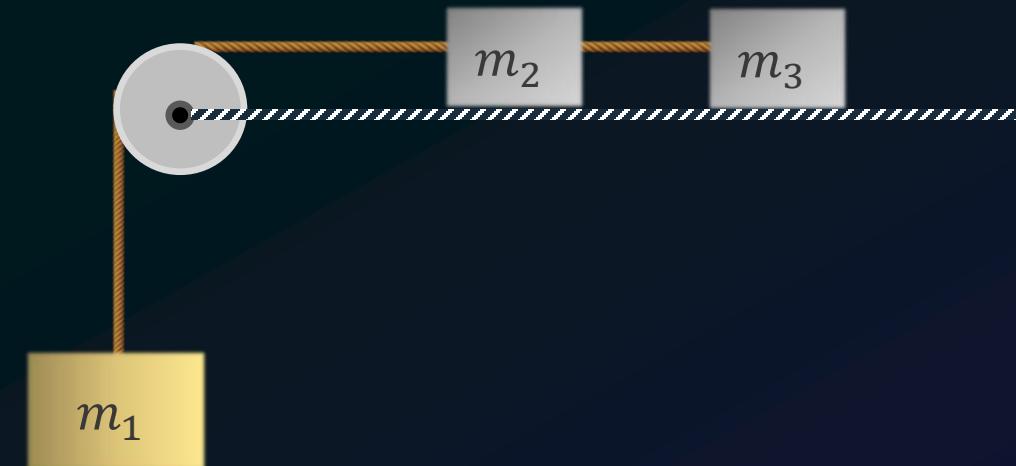
A system consists of three identical masses  $m_1$ ,  $m_2$  and  $m_3$  connected by a string passing over a pulley  $P$ . The mass  $m_1$  hangs freely and  $m_2$  and  $m_3$  are on a rough horizontal table (the coefficient of friction =  $\mu$ ). The pulley is frictionless and of negligible mass. The downward acceleration of mass  $m_1$  is

a.  $\frac{g(1 - 2\mu)}{g}$

b.  $\frac{2g\mu}{3}$

c.  ~~$\frac{g(1 - 2\mu)}{3}$~~

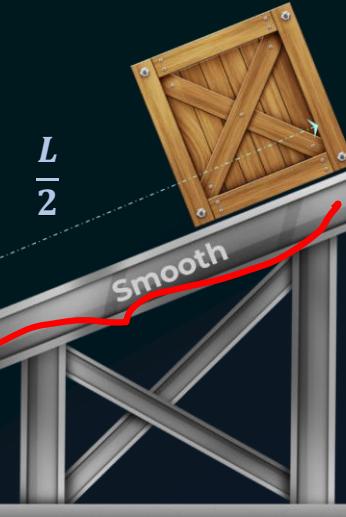
d.  $\frac{g(1 - 2\mu)}{2}$



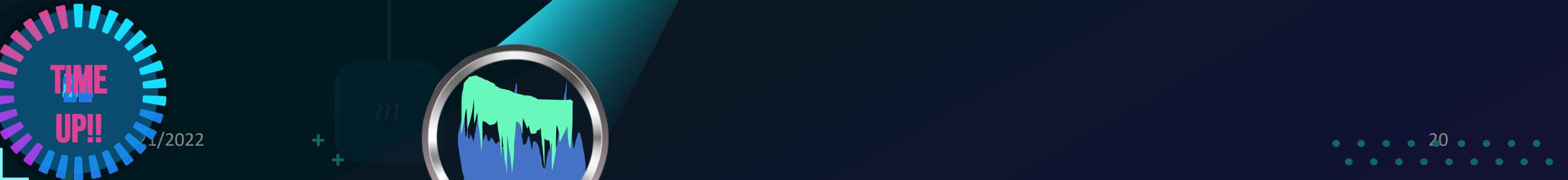
# EXAMPLE

The upper half of an inclined plane of inclination  $\theta$  is perfectly smooth, while the lower half is rough. A block, starting from rest at the top of the plane, again comes to rest at the bottom. The coefficient of friction between the block and lower half of the plane is -

- a.  $\mu = \tan \theta$
- b.  $\mu = \frac{1}{\tan \theta}$
- c.  $\mu = \frac{2}{\tan \theta}$
- d.  $\mu = 2 \tan \theta$



NEET-2013



# SOLUTION

$$2g \sin \theta \frac{L}{2} = v^2 \quad \checkmark$$

$$2(\mu g \cos \theta - g \sin \theta) \frac{L}{2} = v^2 \quad \checkmark$$

$$g \sin \theta = \mu g \cos \theta - g \sin \theta$$

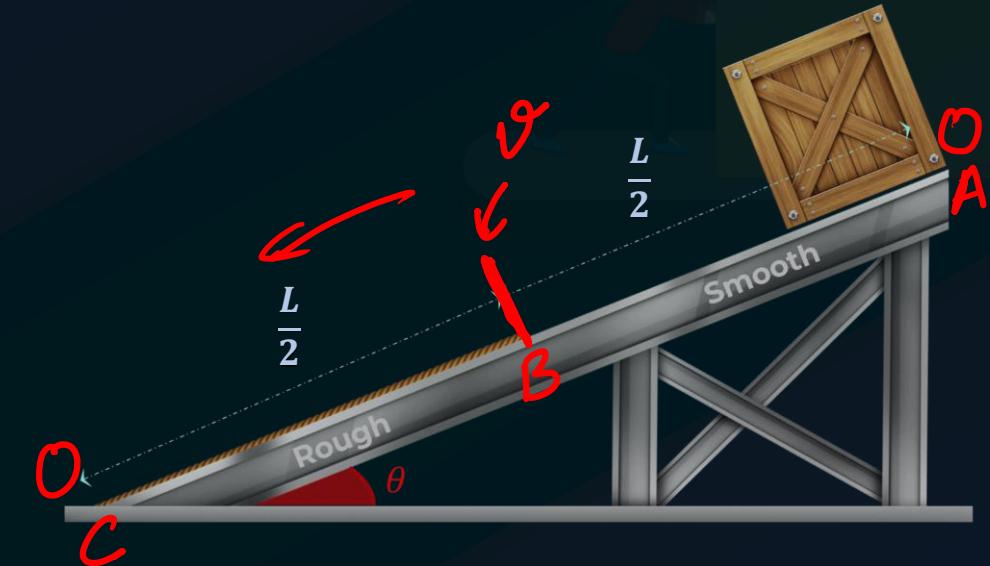
$$\mu = 2 \tan \theta$$

3 kg

$\mu = 0.5$



9/21/2022



# SOLUTION



From work energy theorem ( $W = \Delta KE$ )

As the block starts from rest and finally comes to rest,

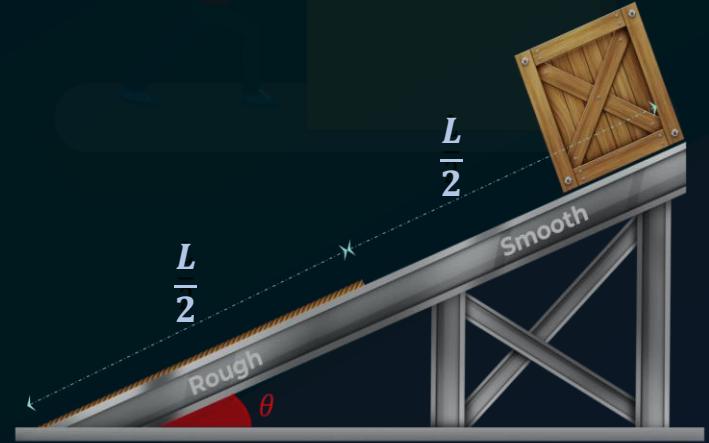
so  $\Delta KE = 0$ , so that we can write,

Work done by friction + work done gravity = 0

$$(mg \sin\theta)(2s) - (\mu mg \cos\theta)(s) = 0$$

$$2mgs \sin\theta = \mu mgs \cos\theta$$

$$\Rightarrow \mu = 2 \tan \theta \quad \checkmark$$



3 kg

$\mu = 0.5$

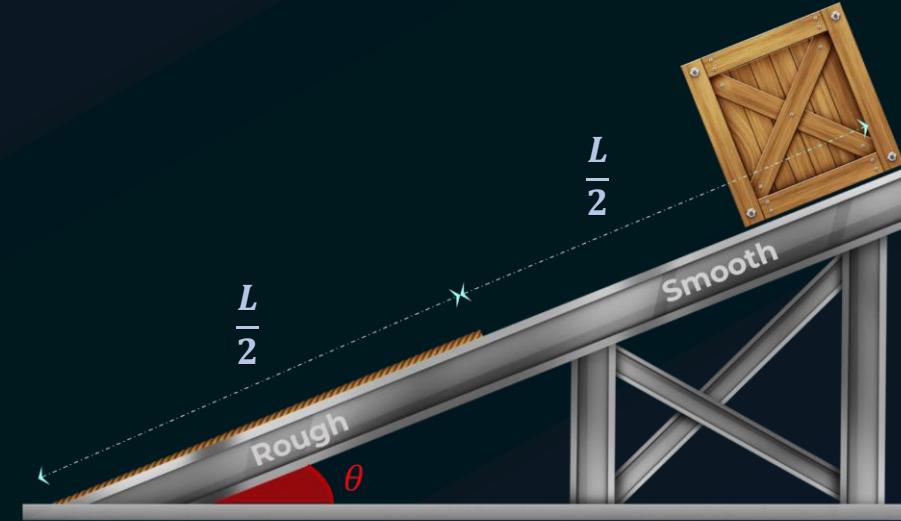


9/21/2022

# ANSWER

The upper half of an inclined plane of inclination  $\theta$  is perfectly smooth, while the lower half is rough. A block, starting from rest at the top of the plane, again comes to rest at the bottom. The coefficient of friction between the block and lower half of the plane is -

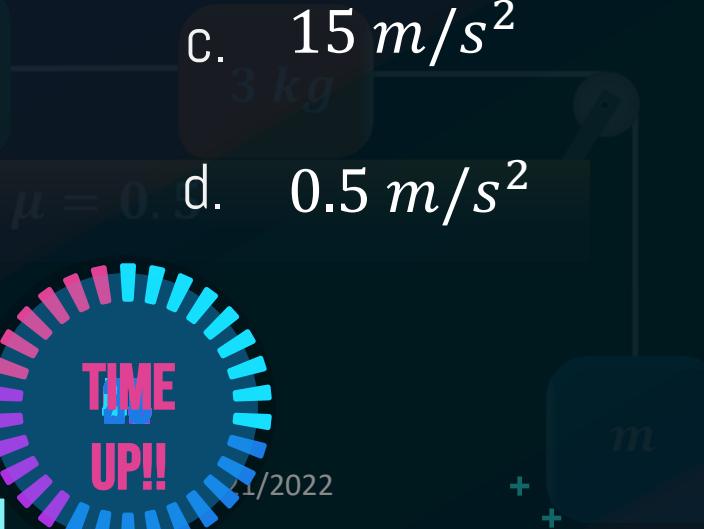
- a.  $\mu = \tan \theta$
- b.  $\mu = \frac{1}{\tan \theta}$
- c. ~~3~~  $\mu g = \frac{2}{\tan \theta}$
- d. ~~✓~~  $\mu = 2 \tan \theta$



## EXAMPLE

A block of mass  $10 \text{ kg}$  is placed on a rough horizontal surface whose coefficient of friction is  $0.5$ . If a horizontal force of magnitude  $100 \text{ N}$  is applied on the block, then acceleration of the block will be  
[Take  $g = 10 \text{ m/s}^2$ ]

- a.  $10 \text{ m/s}^2$
- b.  $5 \text{ m/s}^2$
- c.  $15 \text{ m/s}^2$
- d.  $0.5 \text{ m/s}^2$

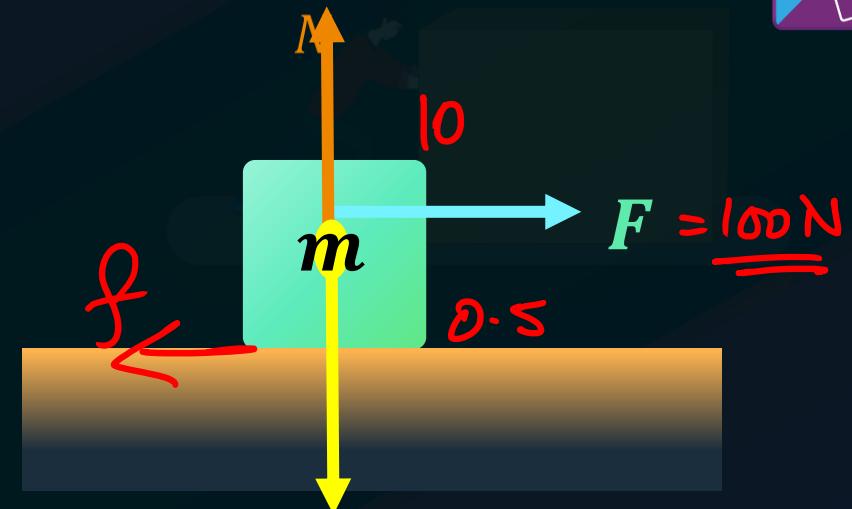


# SOLUTION

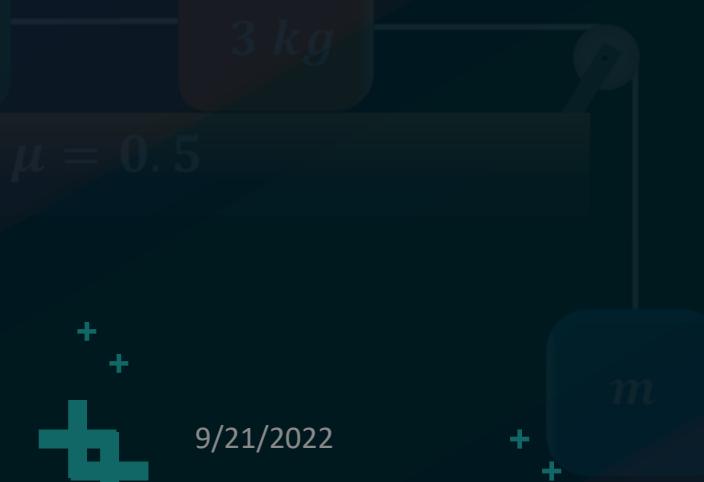
$$\mu mg$$
$$(0.5)(10)(10) = \boxed{50}$$

50N

$$a = \frac{50}{10} = 5 \text{ m/s}^2$$



$mg$



$\mu = 0.5$

# SOLUTION



Given:  $m = 10 \text{ kg}$ ,  $g = 10 \text{ ms}^{-2}$ ,  $\mu = 0.5$  and  $F = 100 \text{ N}$

$\therefore$  Force of friction,  $f = \mu N = \mu mg$

$$\Rightarrow f = 0.5 \times 10 \times 10 = 50 \text{ N}$$

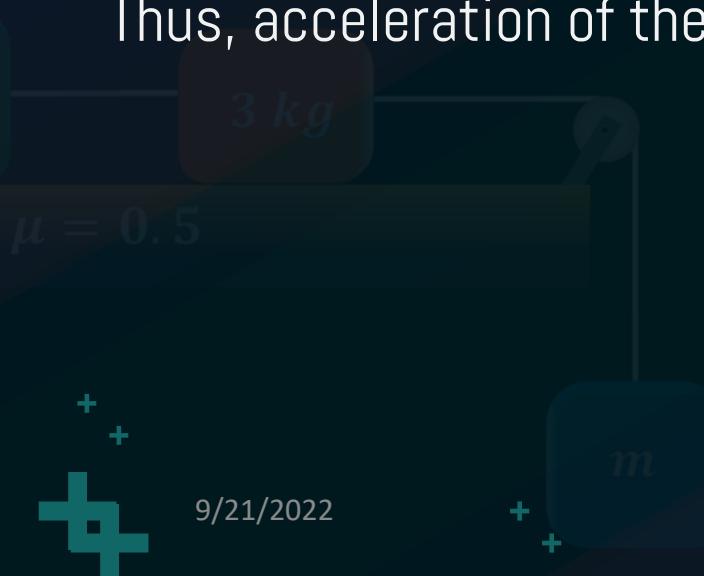
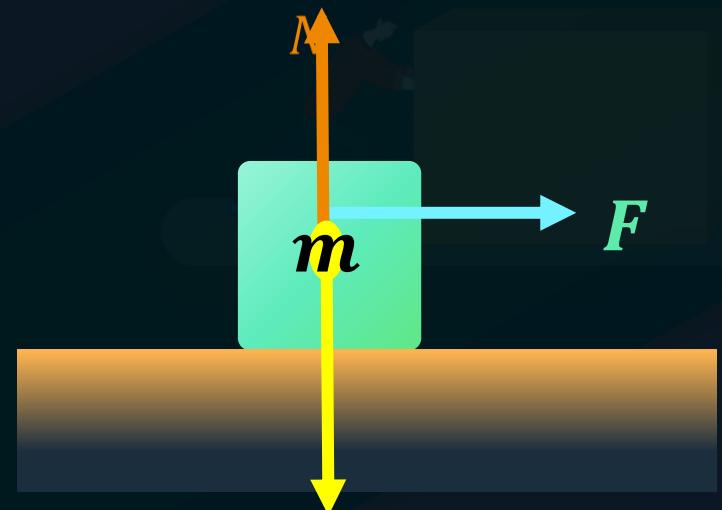
Force that produces acceleration,

$$F' = F - f = 100 \text{ N} - 50 \text{ N} = 50 \text{ N}$$

$$mg$$

Thus, acceleration of the block,

$$a = \frac{F'}{m} = \frac{50}{10} = 5 \text{ ms}^{-2} \quad \checkmark$$



# ANSWER



A block of mass  $10\text{ kg}$  is placed on a rough horizontal surface whose coefficient of friction is  $0.5$ . If a horizontal force of magnitude  $100\text{ N}$  is applied on the block, then acceleration of the block will be  
[Take  $g = 10\text{ m/s}^2$ ]

a.  $10\text{ m/s}^2$

~~b.~~  $5\text{ m/s}^2$

c.  $15\text{ m/s}^2$

$3\text{ kg}$

d.  $0.5\text{ m/s}^2$

$\mu = 0.5$



$\mu = 0.3$

$3 \text{ kg}$

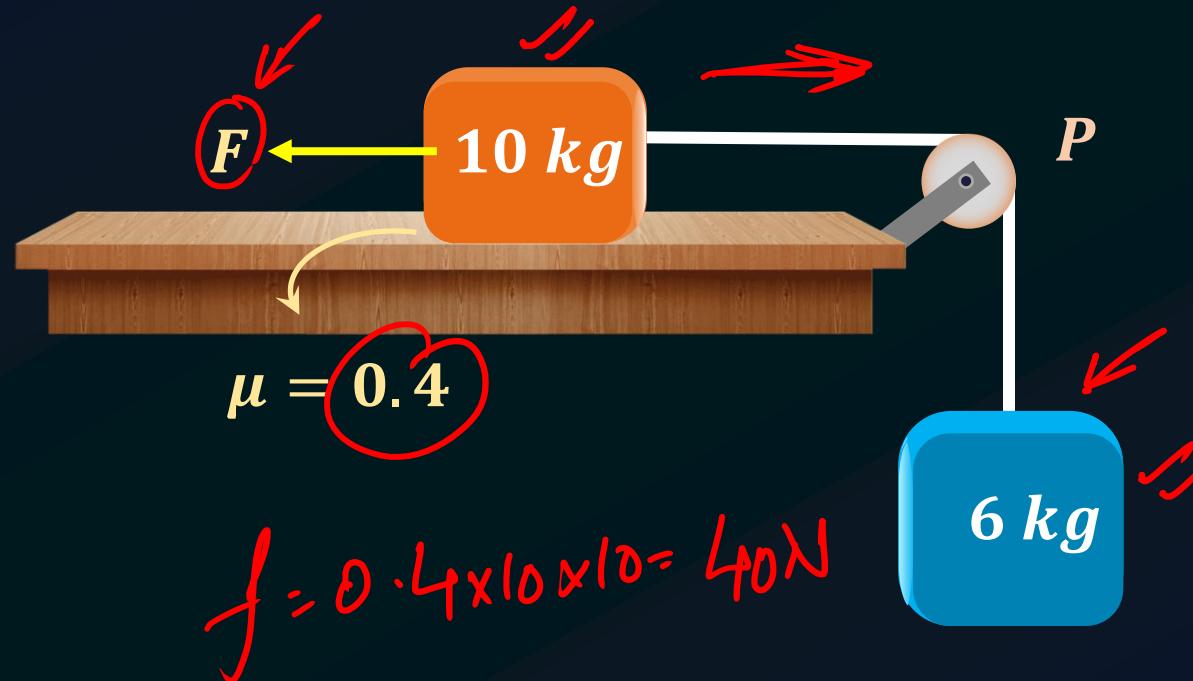


9/21/2022

# EXAMPLE

Find the minimum value of  $F$  for which the system is in equilibrium?  
[ Take  $g = 10 \text{ m/s}^2$ ]

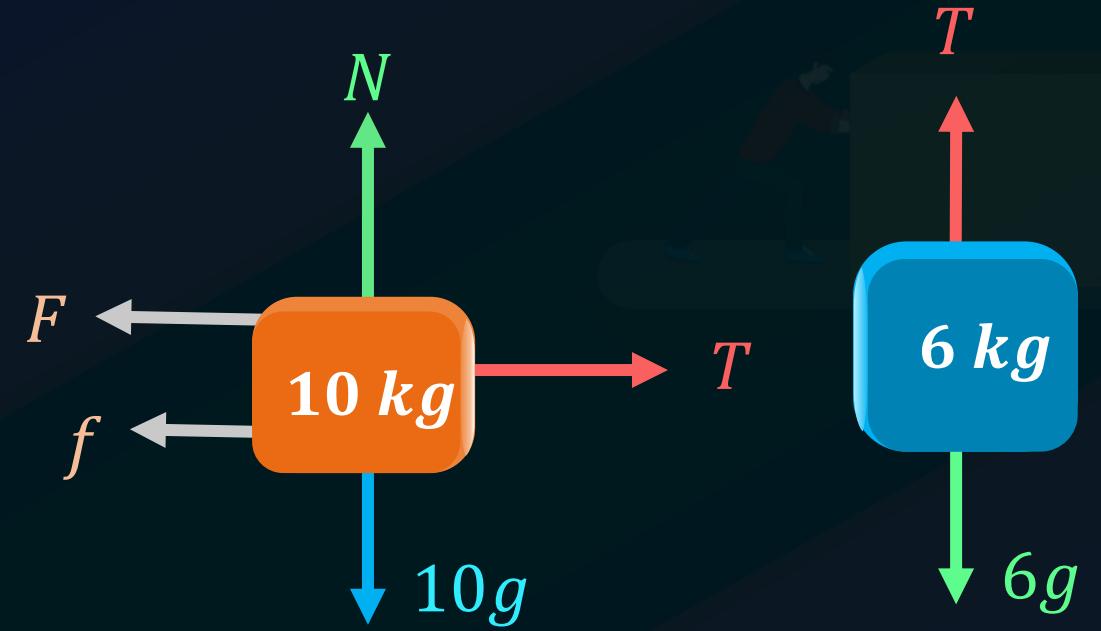
- a.  $5 \text{ N}$
- b.  $10 \text{ N}$
- c.  $15 \text{ N}$
- d.  $20 \text{ N}$



$$f = 0.4 \times 10 \times 10 = 40 \text{ N}$$



# SOLUTION

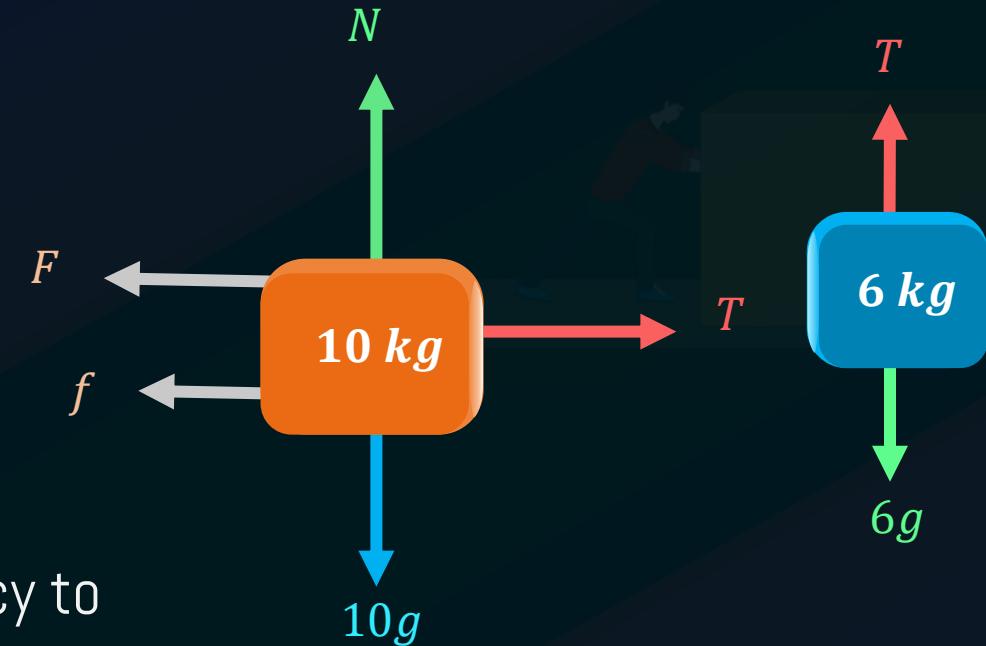


# SOLUTION



By FBD of the blocks

As the system is in equilibrium and the 10 kg block will have the frictional force  $f$  in the backward direction as the block has the tendency to move forward



$$T = 6g, \quad f = \mu mg$$

$$F + f = T$$

$$\Rightarrow 6g = F + 0.4(10)g$$

$$\therefore F = 2g = 2 \times 10 = 20 \text{ N} \quad \checkmark$$

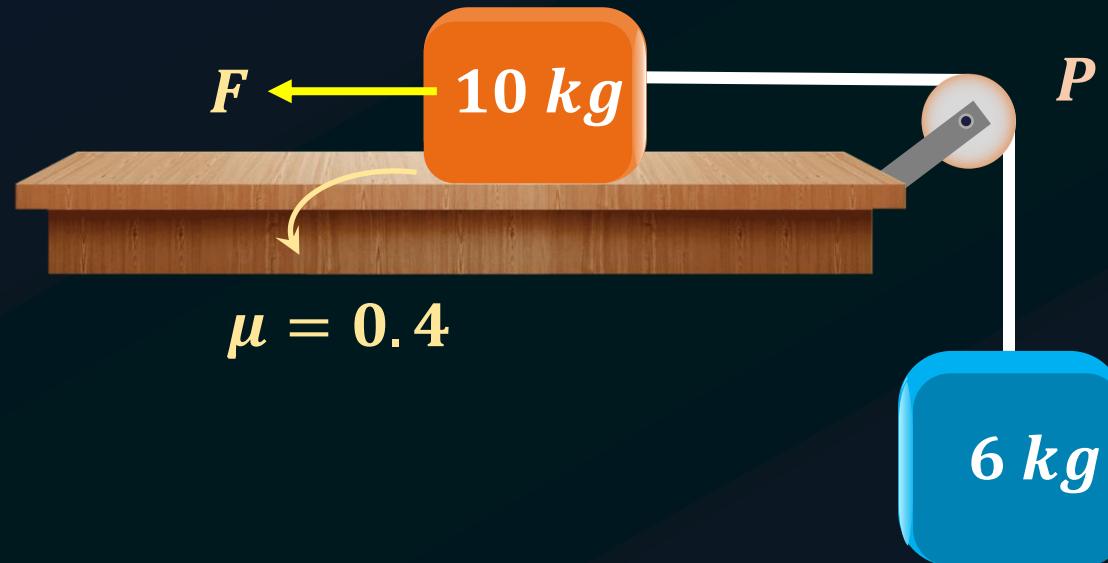
$$\mu = 0.5$$

# ANSWER



Find the value of  $F$  for which the system is in equilibrium?  
[ Take  $g = 10 \text{ m/s}^2$ ]

- a.  $5 \text{ N}$
- b.  $10 \text{ N}$
- c.  $15 \text{ N}$
- d.  $20 \text{ N}$



## EXAMPLE

A cubical block rests on a plane of  $\mu = \sqrt{3}$ . The angle through which the plane be inclined to the horizontal so that the block just slides down will be

- a.  $30^\circ$
- b.  $45^\circ$
- c.  $60^\circ$
- d.  $75^\circ$

$\mu = 0.5$



# SOLUTION



$$\mu = \tan \theta$$

$$\sqrt{3} = \tan \theta$$

$$\theta = 60^\circ$$



# SOLUTION



The block will have force  $mgsin\theta$  along the incline plane and the frictional force will have

$$f_s = \mu N$$

where,  $N = mgcos\theta$

$$f_s = mgsin\theta$$

For equilibrium,  $\mu mgcos\theta = mgsin\theta$

$$\tan\theta = \mu = \sqrt{3}$$

$$\Rightarrow \theta = 60^\circ \checkmark$$

$\mu = 0.5$

3 kg



# ANSWER



A cubical block rests on a plane of  $\mu = \sqrt{3}$ . The angle through which the plane be inclined to the horizontal so that the block just slides down will be

a.  $30^\circ$

b.  $45^\circ$

~~c.~~  $60^\circ$

d.  $75^\circ$

$\mu = 0.5$



## EXAMPLE

A marble block of mass  $2 \text{ kg}$  lying on ice when given a velocity of  $6 \text{ m/s}$  is stopped by friction in  $10 \text{ s}$ . Then the coefficient of friction is

- a. 0.01
- b. 0.02
- c. 0.03
- d. 0.06

$$a = \frac{\mu mg}{m}$$

$$v = u + at$$
$$0 = 6 - \mu g(10)$$
$$= \mu g$$

$$\mu = \frac{6}{100} = 0.01 \times 6$$
$$= 0.06$$



$\mu = 0.5$

TIME  
UP!!

21/2022

# SOLUTION



# SOLUTION



As we know that,  $v = u + at$

$$\Rightarrow u - at = 0$$

$$a = \frac{6}{10}$$

$\Rightarrow a = -0.6 \text{ m/s}^2$  (*-ive* means retardation)

As block is stopped due to friction so,

$$F_{friction} = ma$$

$$\mu = \frac{0.6}{10} = 0.06 \quad \checkmark$$

$$\mu = 0.5$$



# ANSWER



A marble block of mass  $2 \text{ kg}$  lying on ice when given a velocity of  $6 \text{ m/s}$  is stopped by friction in  $10 \text{ s}$ . Then the coefficient of friction is

- a. 0.01
- b. 0.02
- c. 0.03
- d. 0.06

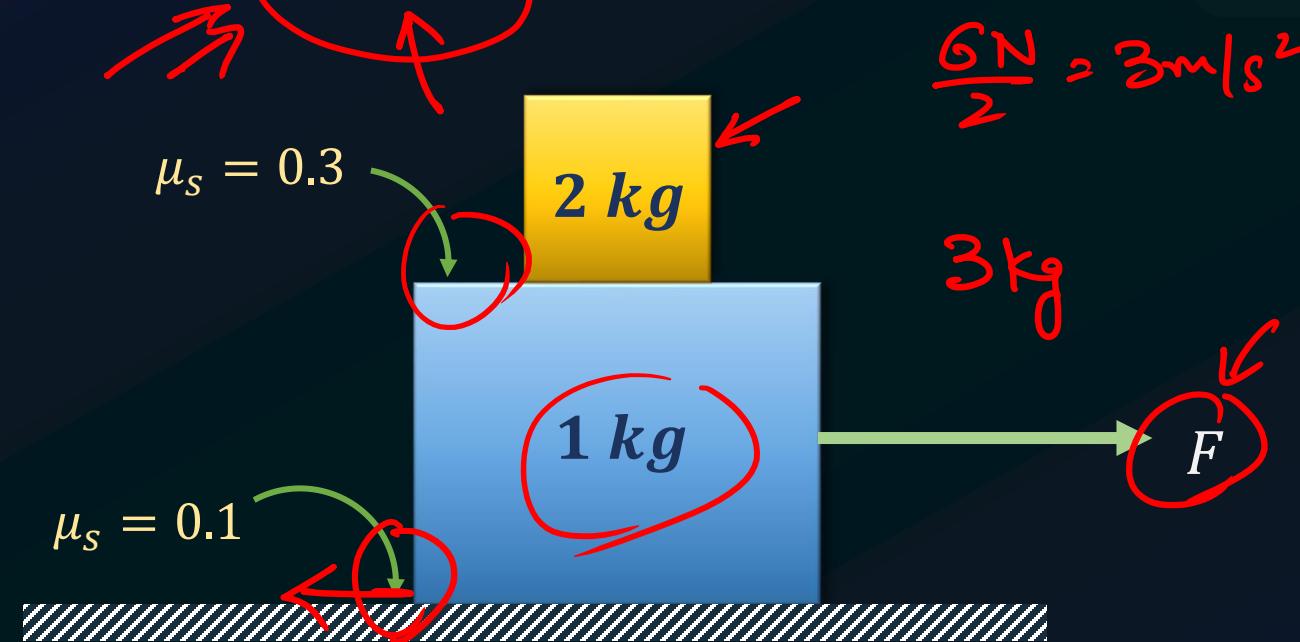
$$\mu = 0.5$$



# EXAMPLE

Find the maximum force that should act on the 1 kg body for the system to accelerate together with  $2 \text{ m/s}^2$ . [Take  $g = 10 \text{ m/s}^2$ ].

- a. 4 N
- b. 5 N
- c. 7 N
- d. 9 N

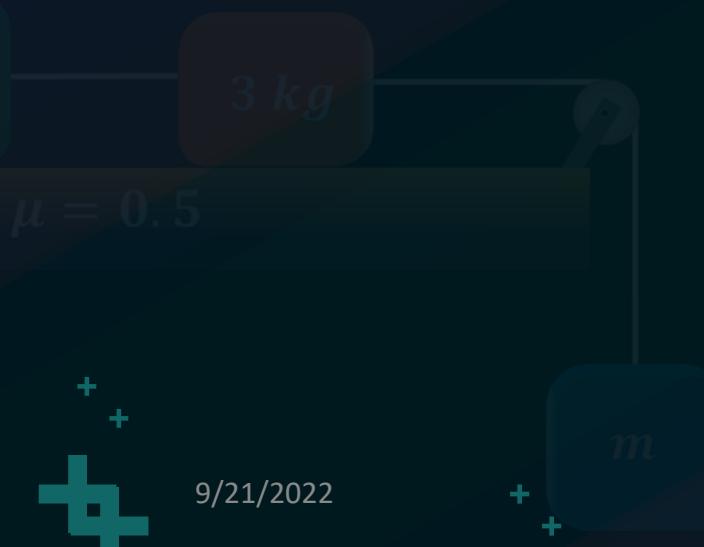
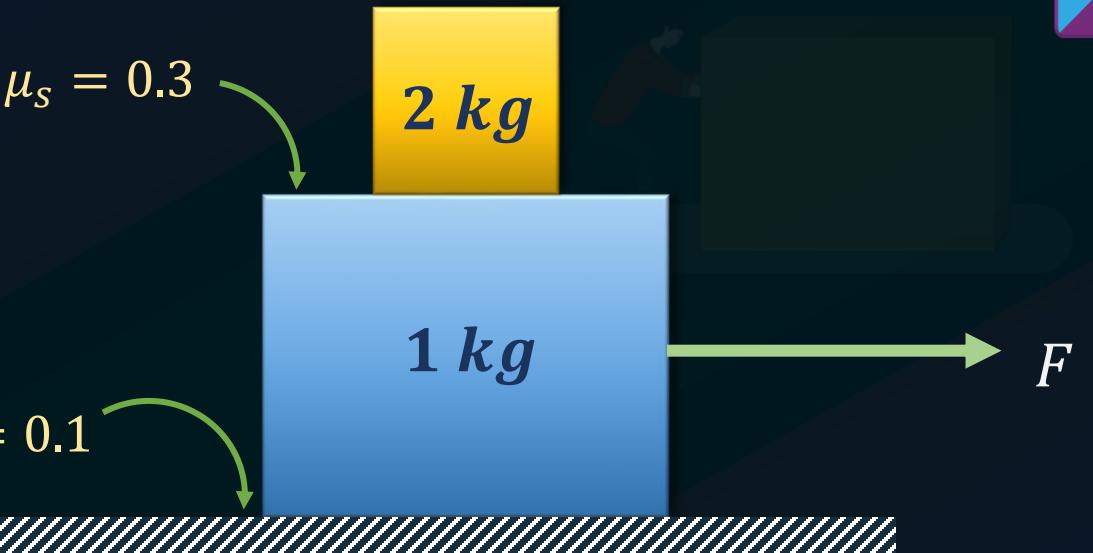


$$F - (0.1)(3)(10) = 3(2)$$

$$F = 9 \text{ N}$$



# SOLUTION



# SOLUTION



From FBD of the system of blocks,

$$F - f = (m_1 + m_2)a_s$$

where  $a_s$  is the acceleration of the system.

For  $F = F_{max}$ ,

friction will have limiting value,

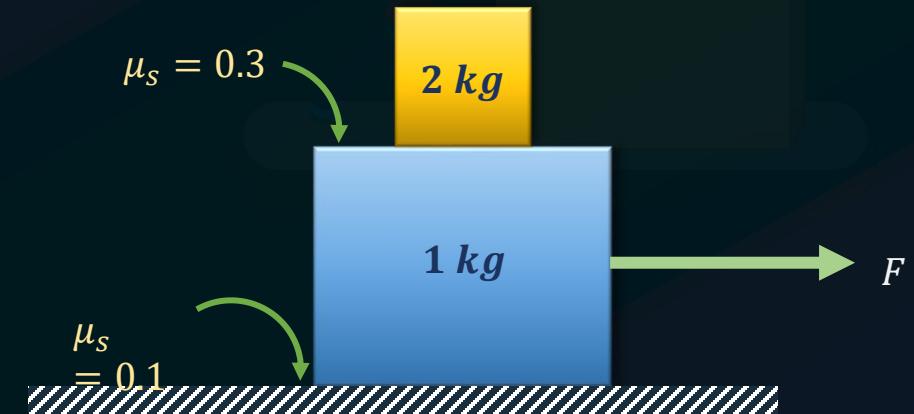
$$f = \mu_1 N = \mu_1 (m_1 + m_2)g$$

$$\text{Then, } F_{max} = (m_1 + m_2)(\mu_1 g + a_s)$$

Given:  $m_1 = 1 \text{ kg}$ ;  $m_2 = 2 \text{ kg}$ ;  $\mu_1 = 0.1$ ;  $a_s = 2 \text{ m/s}^2$

Hence,

$$F_{max} = (2 + 1)(0.1 \times 10 + 2) = 3 \times 3 = 9 \text{ N} \checkmark$$



# ANSWER

Find the maximum force that should act on the  $1 \text{ kg}$  body for the system to accelerate together with  $2 \text{ m/s}^2$ . [Take  $g = 10 \text{ m/s}^2$ ].

a.  $4 \text{ N}$

b.  $5 \text{ N}$

c.  $7 \text{ N}$

d.  $9 \text{ N}$



$$\mu = 0.5$$



$\mu$  = 0.3

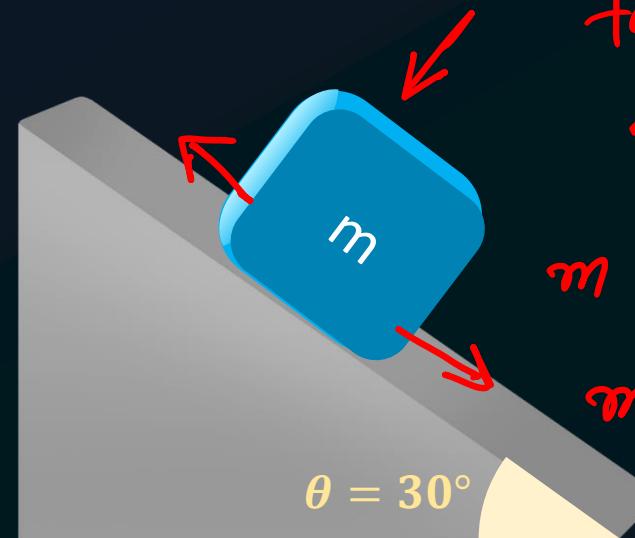
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# EXAMPLE

A block rests on a rough inclined plane making an angle of  $30^\circ$  with the horizontal. The coefficient of static friction between the block and the plane is 0.8. If the frictional force on the block is 10 N, the mass of the block (in kg) is (take  $g = 10 \text{ m/s}^2$ )

- a.  $2.5 \text{ kg}$
- b.  $4 \text{ kg}$
- c.  $1.5 \text{ kg}$
- d.  $2 \text{ kg}$

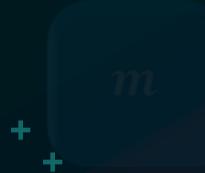


$$\begin{aligned}N &= \cancel{\cancel{m}} \\ \tan(30^\circ) &= \boxed{0.6} \\ mg \sin 30^\circ &= 10 \\ m &= \frac{10}{5} \\ m &= 2\end{aligned}$$

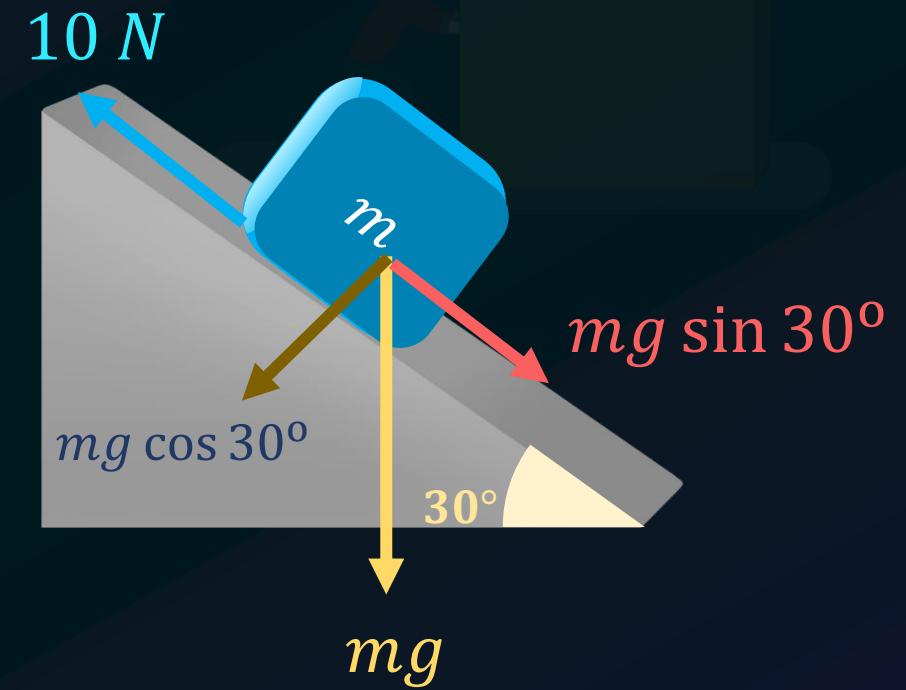


$$\mu = 0.5$$

$$3 \text{ kg}$$



# SOLUTION



# SOLUTION

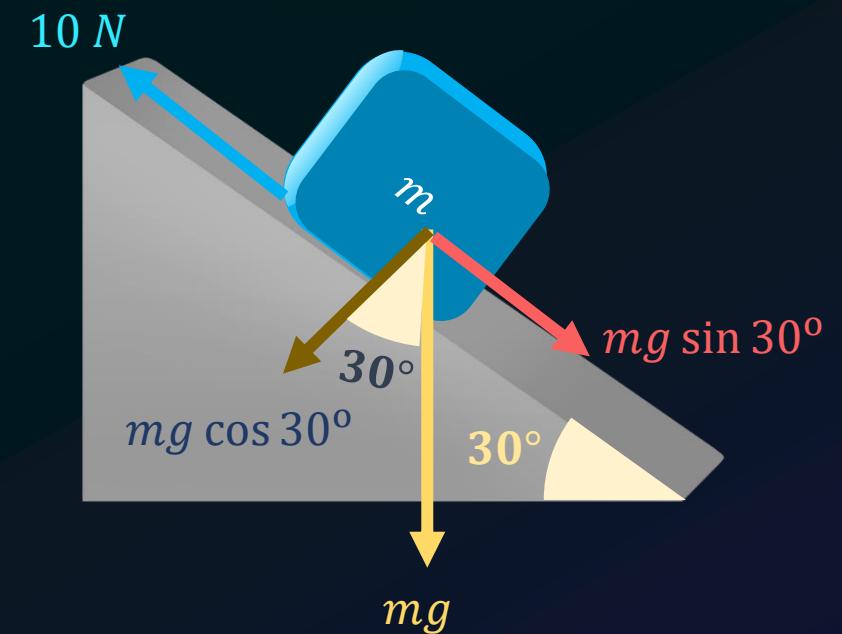


By the FBD, It is given that the body is in rest and so the frictional force 10 N will be acting on the block opposite to the direction of component of  $mg$  along the incline plane.

$$\therefore f = mg \sin 30 = 10 \text{ N}$$

$$\Rightarrow \frac{m \times 10}{2} = 10$$

$$\Rightarrow m = 2 \text{ kg} \checkmark$$



3 kg

$\mu = 0.5$

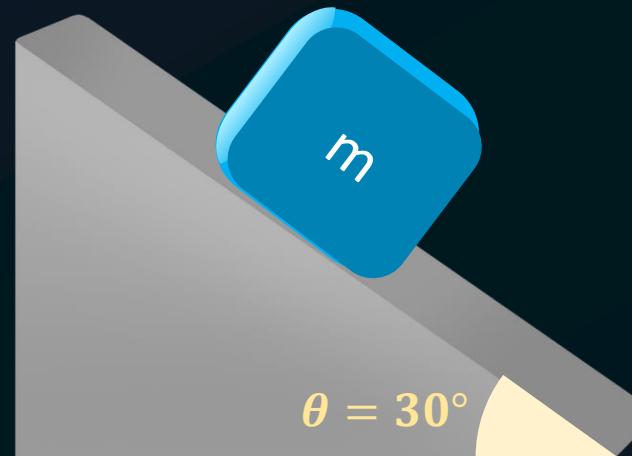


# ANSWER



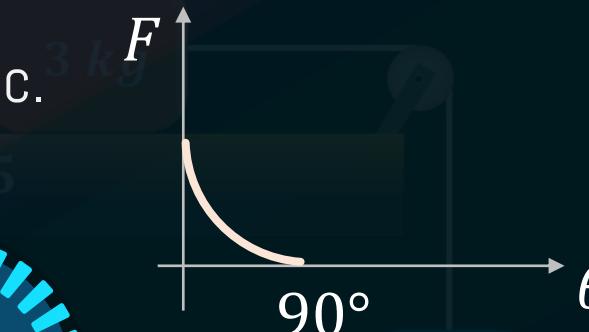
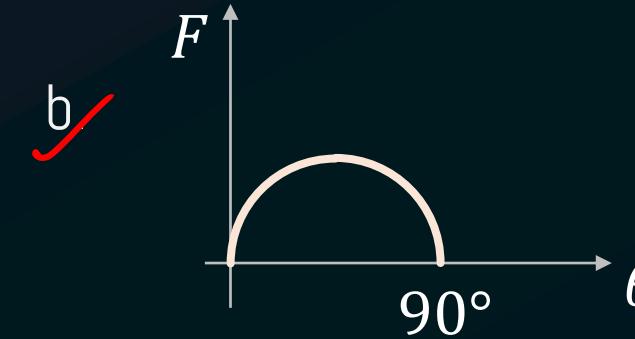
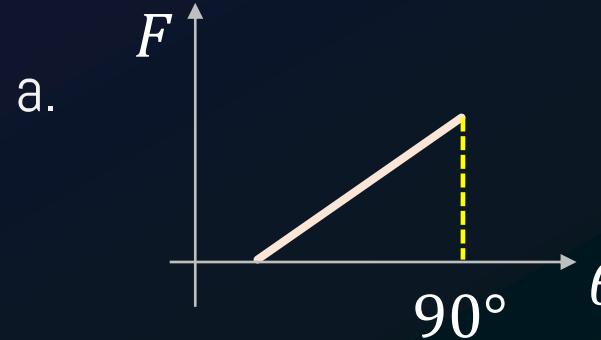
A block rests on a rough inclined plane making an angle of  $30^\circ$  with the horizontal. The coefficient of static friction between the block and the plane is 0.8. If the frictional force on the block is  $10\text{ N}$ , the mass of the block (in  $\text{kg}$ ) is (take  $g = 10\text{ m/s}^2$ )

- a.  $2.5\text{ kg}$
- b.  $4\text{ kg}$
- c.  $1.5\text{ kg}$
- ~~d.~~  $2\text{ kg}$



# EXAMPLE

A block rests on a rough plane whose inclination  $\theta$  to the horizontal can be varied. Which of the following graphs indicates how the frictional force  $F$  between the block and plane varies as  $\theta$  is increased?



$\mu = 0.5$

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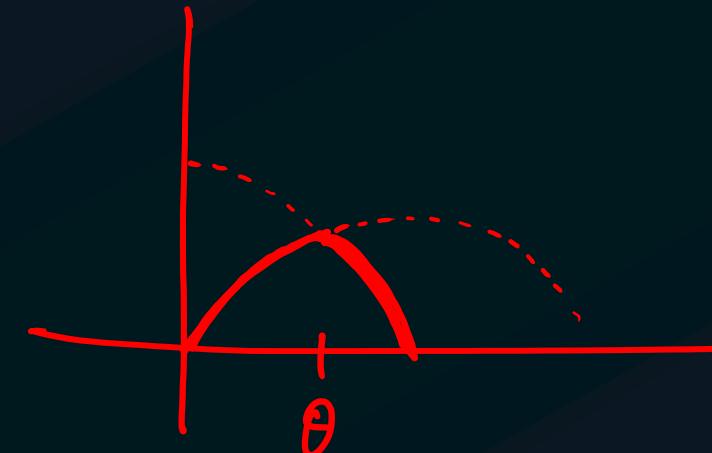
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# SOLUTION



$$f = mg \sin \theta$$

$$f = \mu mg \cos \theta \Rightarrow \mu N$$



3 kg

$\mu = 0.5$

# SOLUTION



When the plane is horizontal there will be no frictional force acting as there will be no driving force. The maximum angle for which the block remains stationary is called the angle of repose

Let  $\alpha$  = angle of repose

For  $\theta \leq \alpha$ , block is stationary and force of friction,

$$f = mg \sin \theta$$

Or  $f \propto \sin \theta$

i.e, now it is **sine graph**

For  $\theta \geq \alpha$  Block slides downwards

$$\therefore f = \mu mg \cos \theta$$

Or,  $f \propto \cos \theta$

i.e, now it is **cosine graph**.

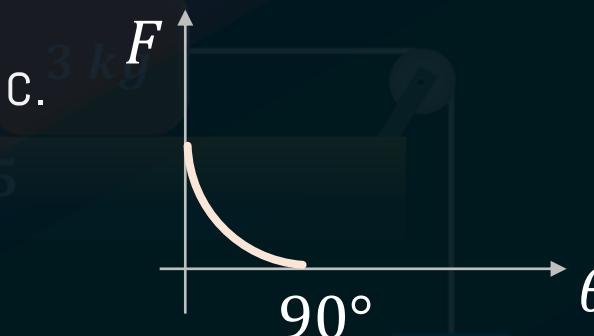
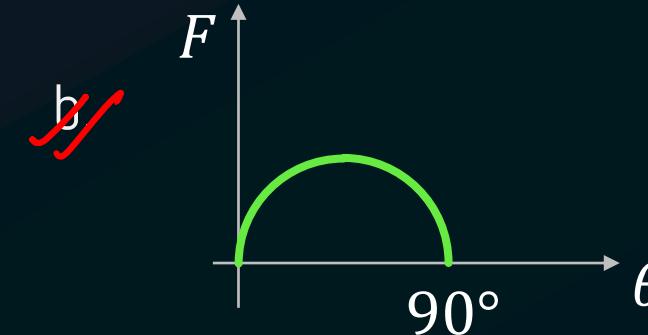
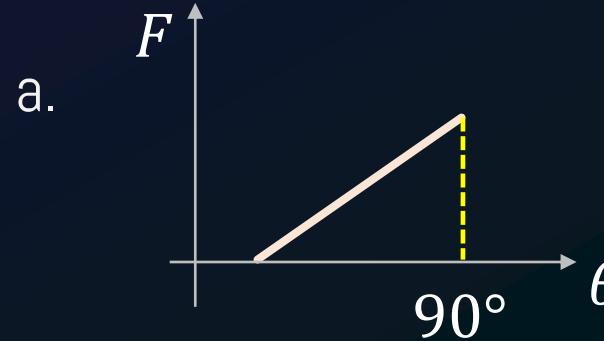
$\mu = 0.5$



# ANSWER



A block rests on a rough plane whose inclination  $\theta$  to the horizontal can be varied. Which of the following graphs indicates how the frictional force  $F$  between the block and plane varies as  $\theta$  is increased?





$\mu$  = 0.3

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