

**BONUS
SESSION**

LC
Oscillation



ALTERNATING

CURRENT L-5

GRADE 12 | PHYSICS

MRINAL SIR



<https://t.me/neetaakashdigital>



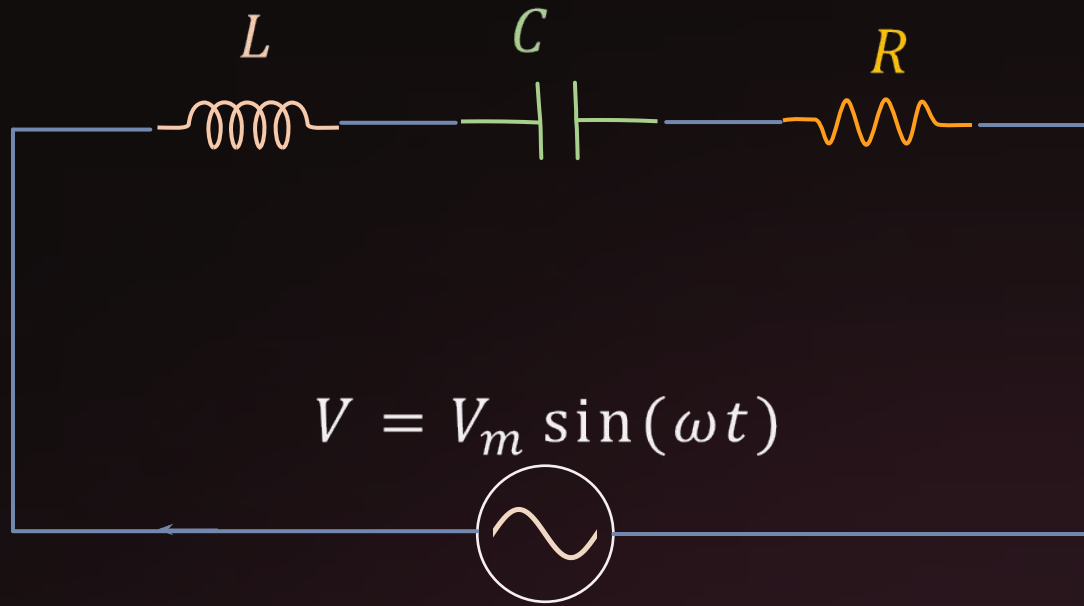
CONTENTS

Resonance

Resonance in Radio tuning

Lc oscillation

RESONANCE



$$i_m = \frac{V_m}{\sqrt{R^2 + (X_C - X_L)^2}}$$

$$X_C = \frac{1}{\omega C}$$

$$X_L = \omega L$$

If ω is varied, then at a particular frequency (ω_0), $X_C = X_L$

RESONANCE

$$i_m = \frac{V_m}{\sqrt{R^2 + (X_C - X_L)^2}}$$

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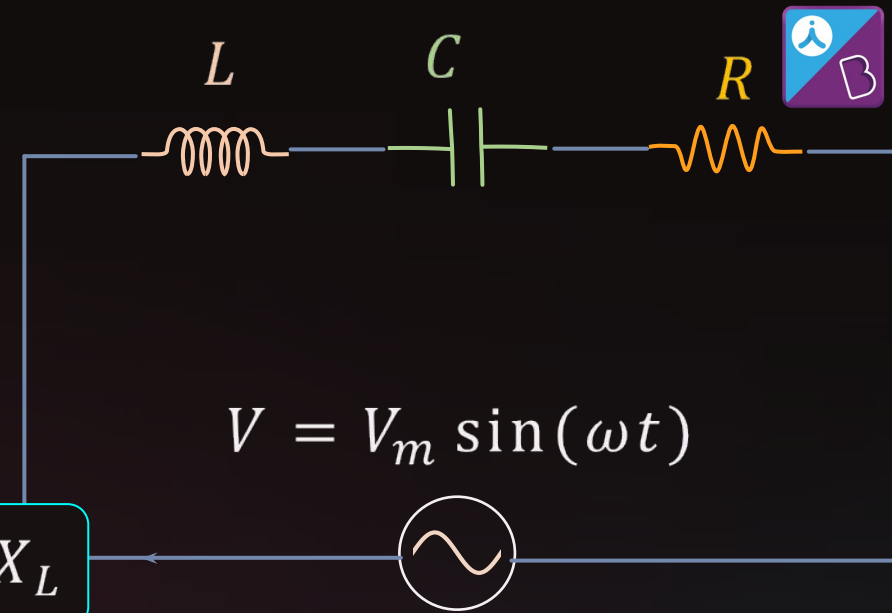
$$X_L = \omega L$$

If ω is varied, then at a particular frequency (ω_0), $X_C = X_L$

ω_0 is resonant angular frequency

Impedance is minimum ($Z = \sqrt{R^2 + 0^2} = R$)
and purely resistive circuit

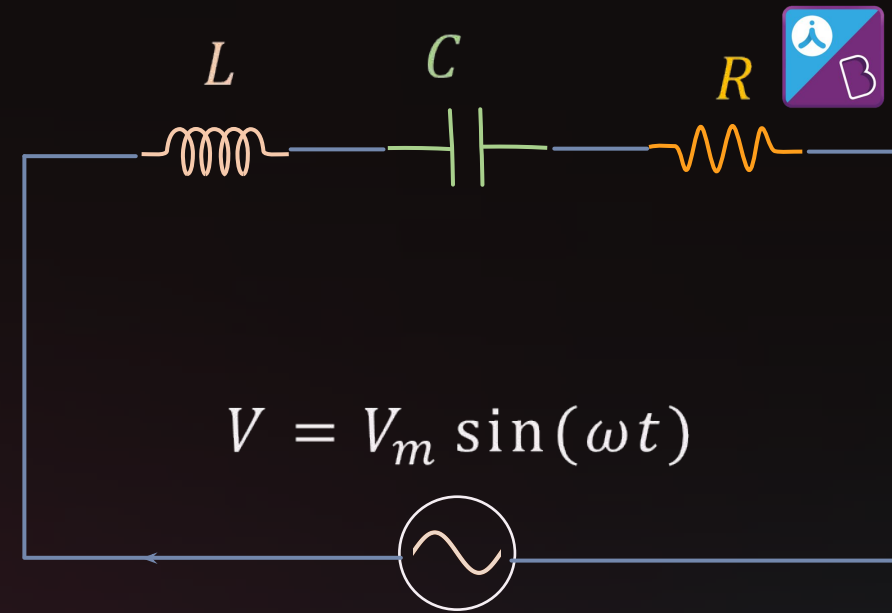
Current is maximum ($i_m = V_m / R$)



RESONANCE

$$X_C = \frac{1}{\omega C}$$

$$X_L = \omega L$$



RESONANCE

$$X_C = \frac{1}{\omega C}$$

$$X_L = \omega L$$

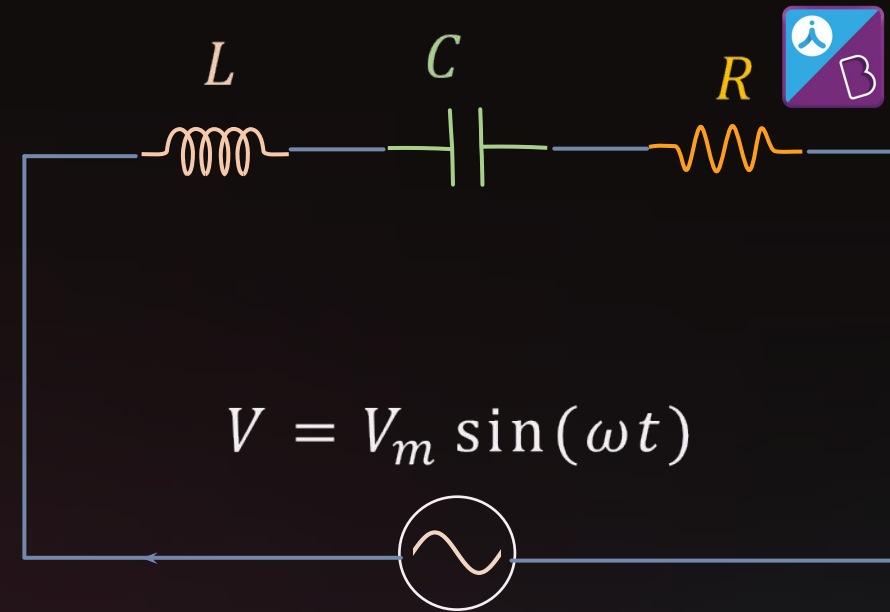
For resonance condition, $X_C = X_L$

$$\frac{1}{\omega_0 C} = \omega_0 L$$

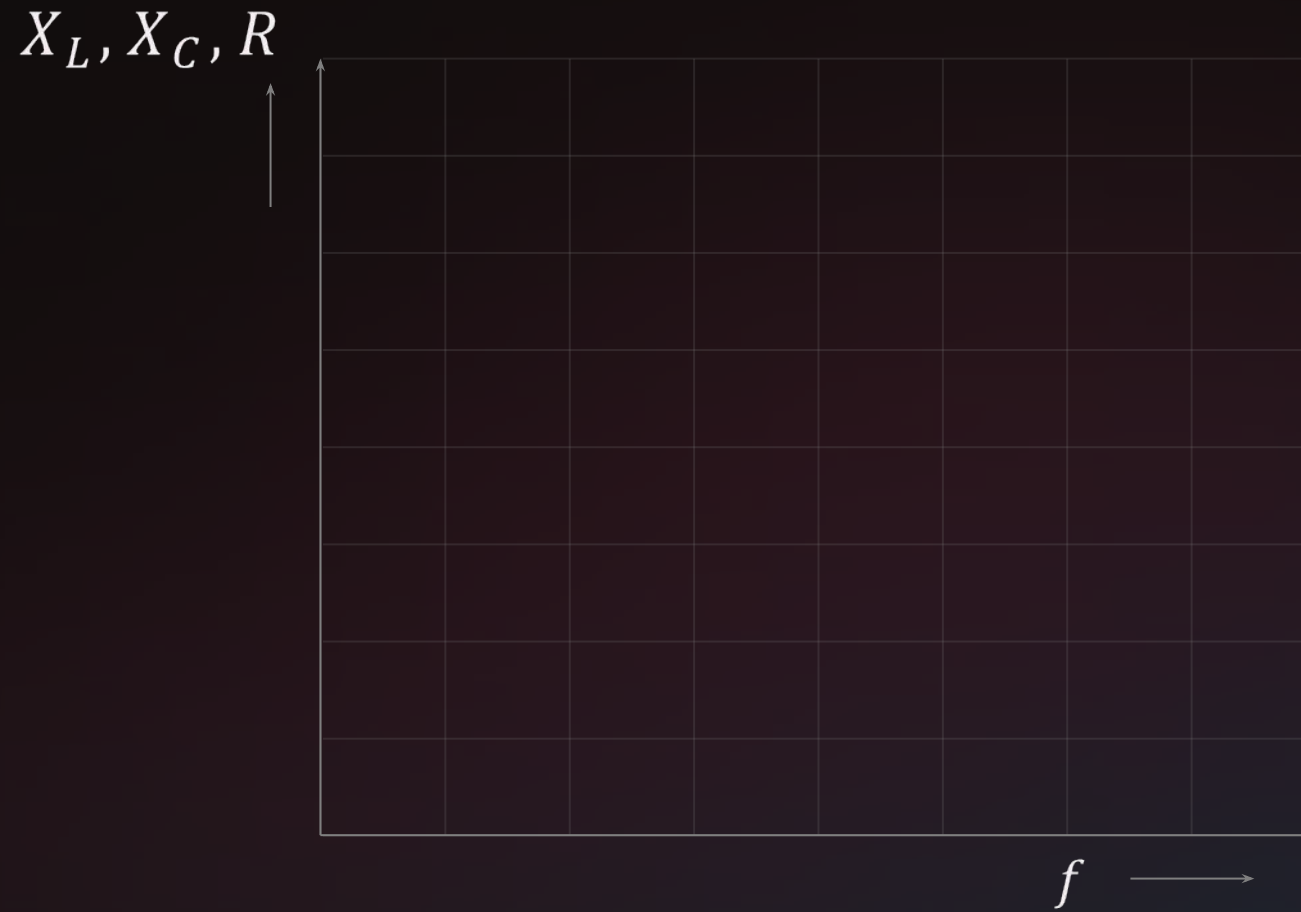
$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

Resonant
frequency

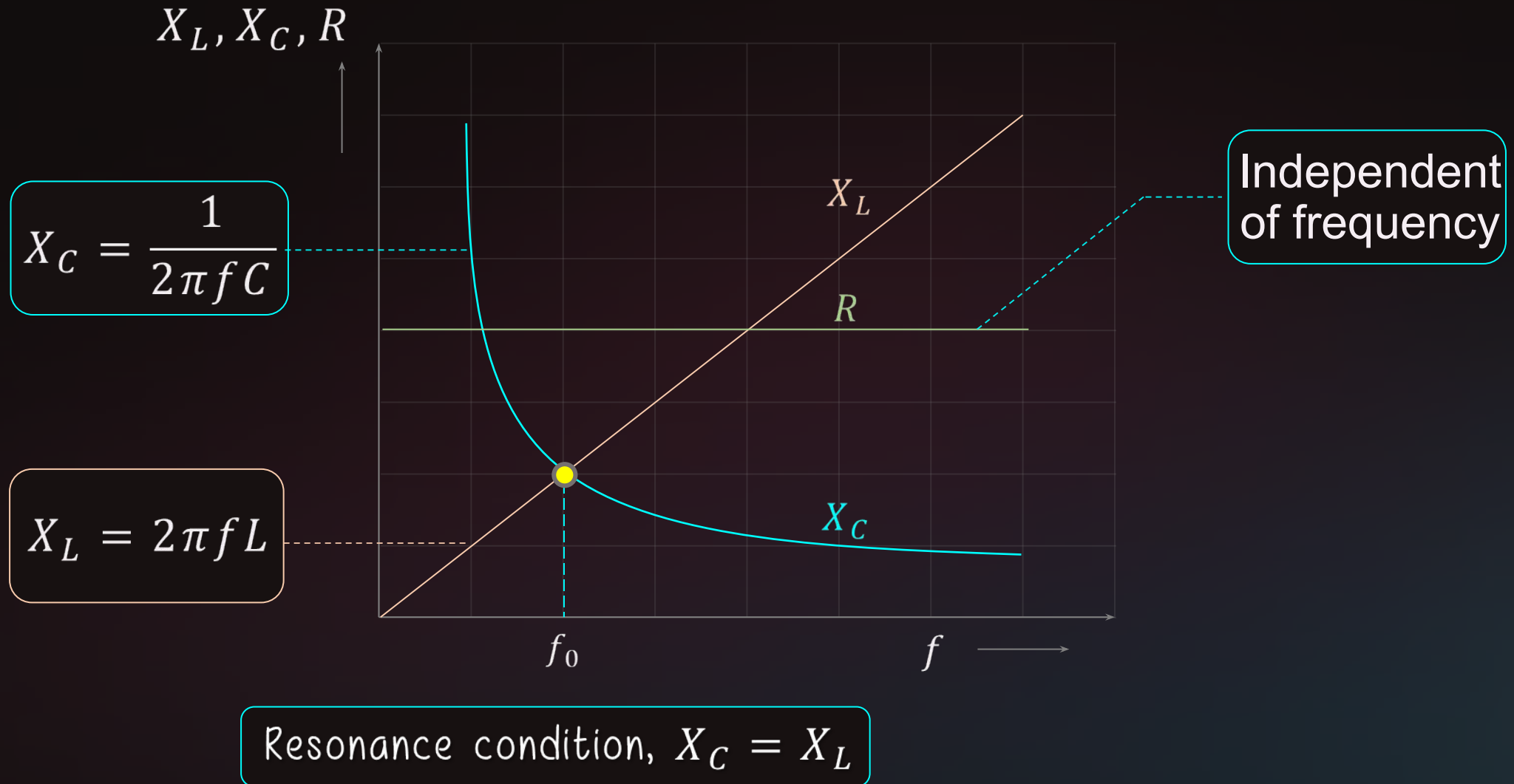


Graphical representation



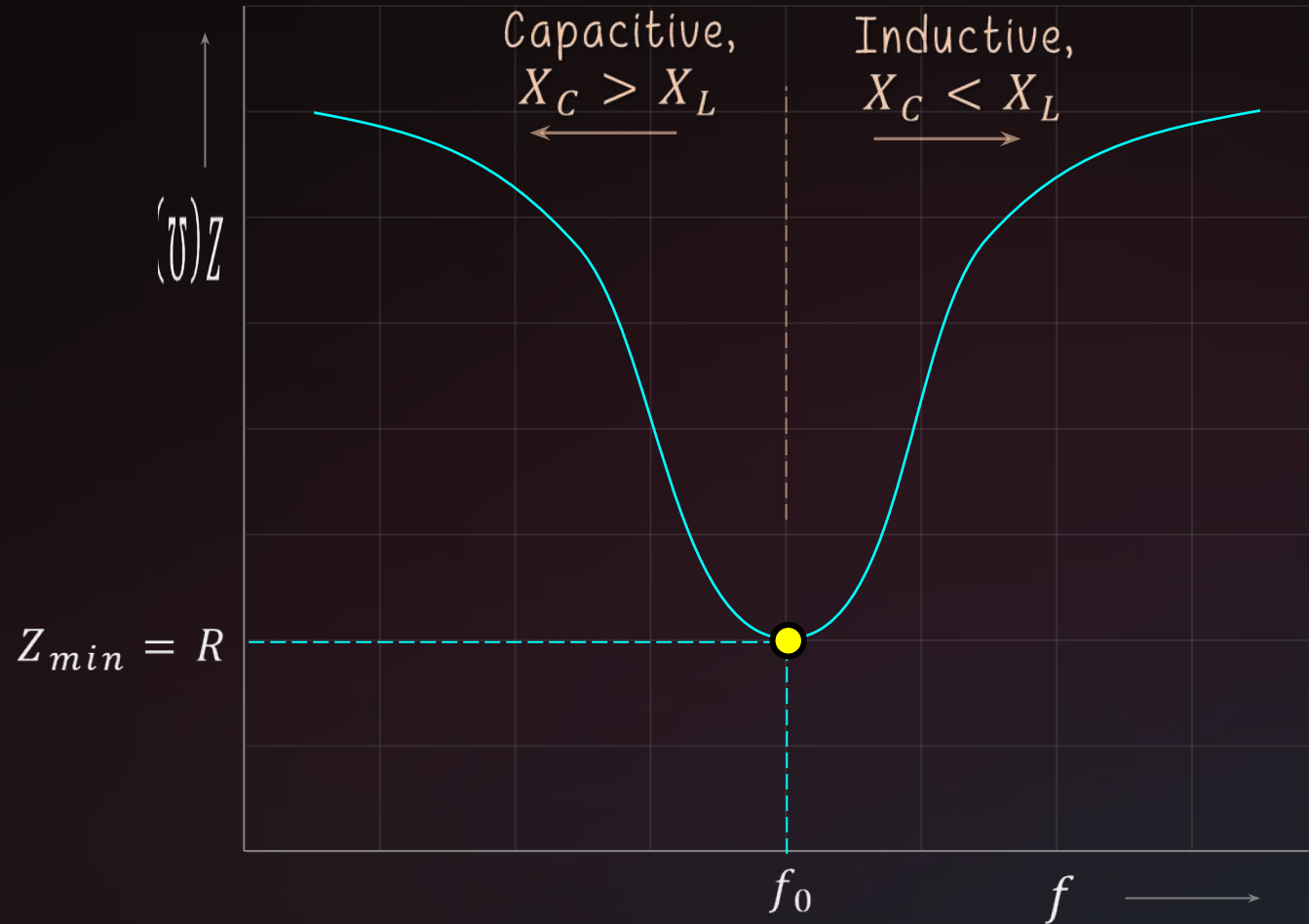
Resonance condition, $X_C = X_L$

Graphical representation

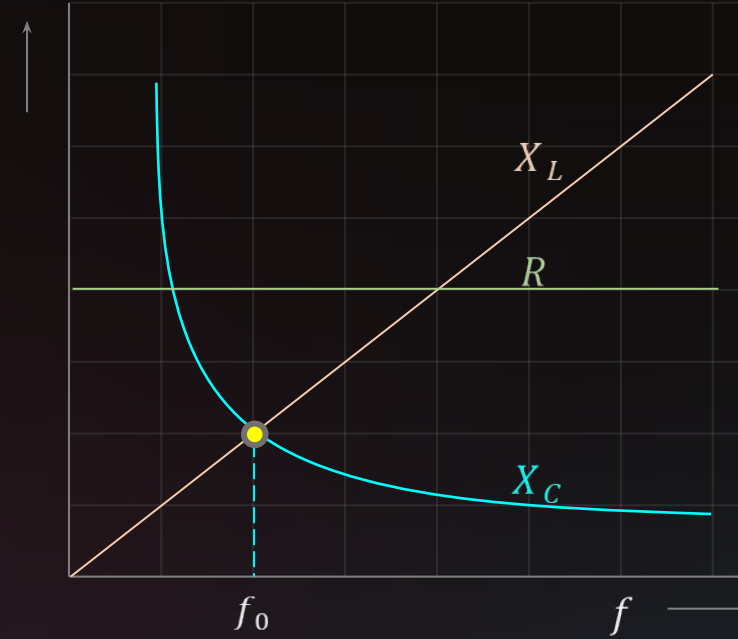


Graphical representation

$$Z = \sqrt{R^2 + \left(\frac{1}{2\pi f C} - 2\pi f L \right)^2}$$



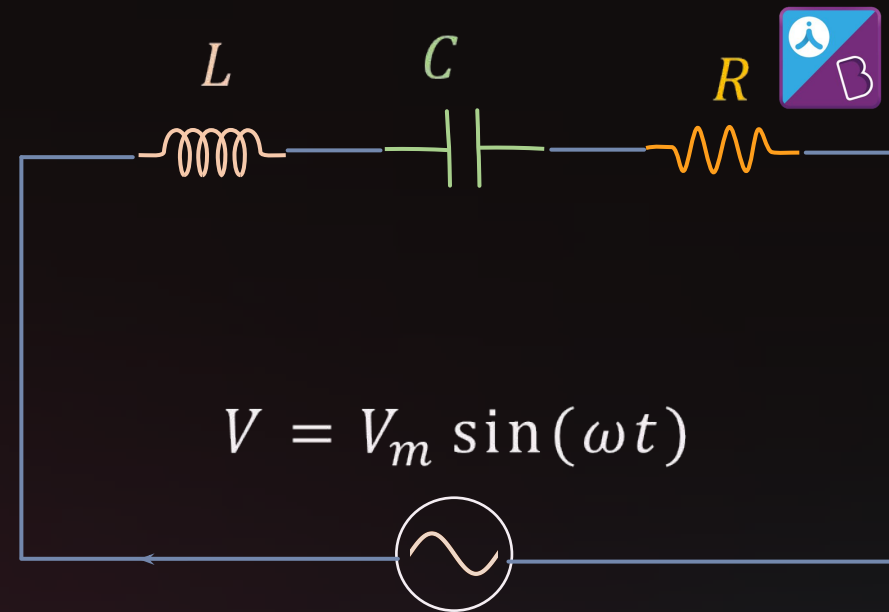
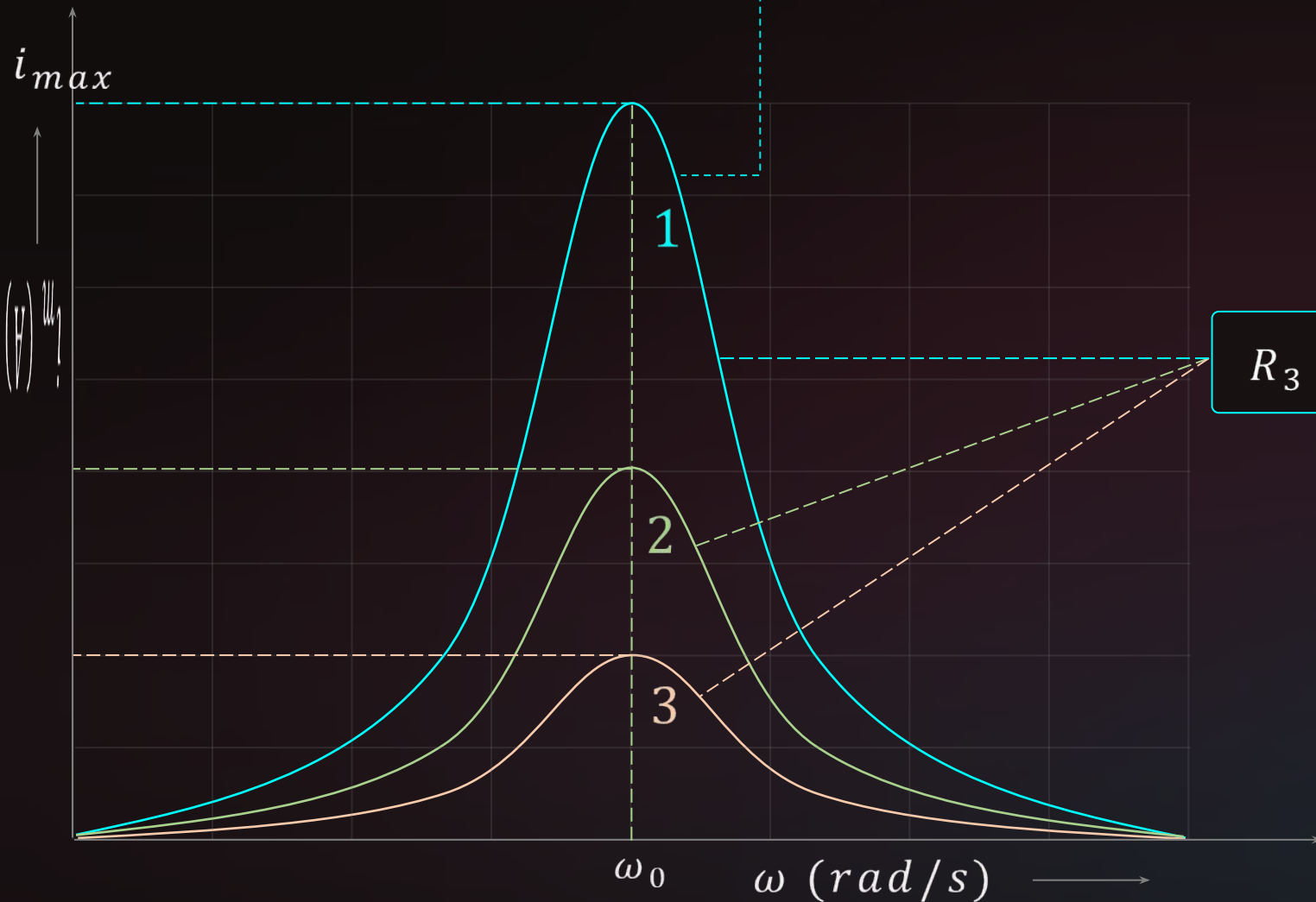
Resonance condition, $X_C = X_L$



RESONANCE

$$Z = \sqrt{R^2 + \left(\frac{1}{\omega C} - \omega L\right)^2}$$

$$i_m = V_m / Z$$





Question



What is the value of inductance L for which the current is maximum in a series LCR circuit with $C = 10 \mu F$ and $\omega = 1000 s^{-1}$?



$1 mH$



$10 mH$



$100 mH$



Cannot be calculated
unless R is known



Y



For maximum current in series LCR circuit,

$$X_L = X_C \Rightarrow \omega L = \frac{1}{\omega C}$$



For maximum current in series LCR circuit,

$$X_L = X_C \Rightarrow \omega L = \frac{1}{\omega C}$$

$$L = \frac{1}{\omega^2 C} = \frac{1}{(1000)^2 \times 10 \times 10^{-6}}$$

$$L = \frac{1}{10} = 0.1 \text{ H} = 100 \text{ mH}$$



Answer



What is the value of inductance L for which the current is maximum in a series LCR circuit with $C = 10 \mu F$ and $\omega = 1000 s^{-1}$?



1 mH



10 mH



100 mH



Cannot be calculated
unless R is known

RESONANCE

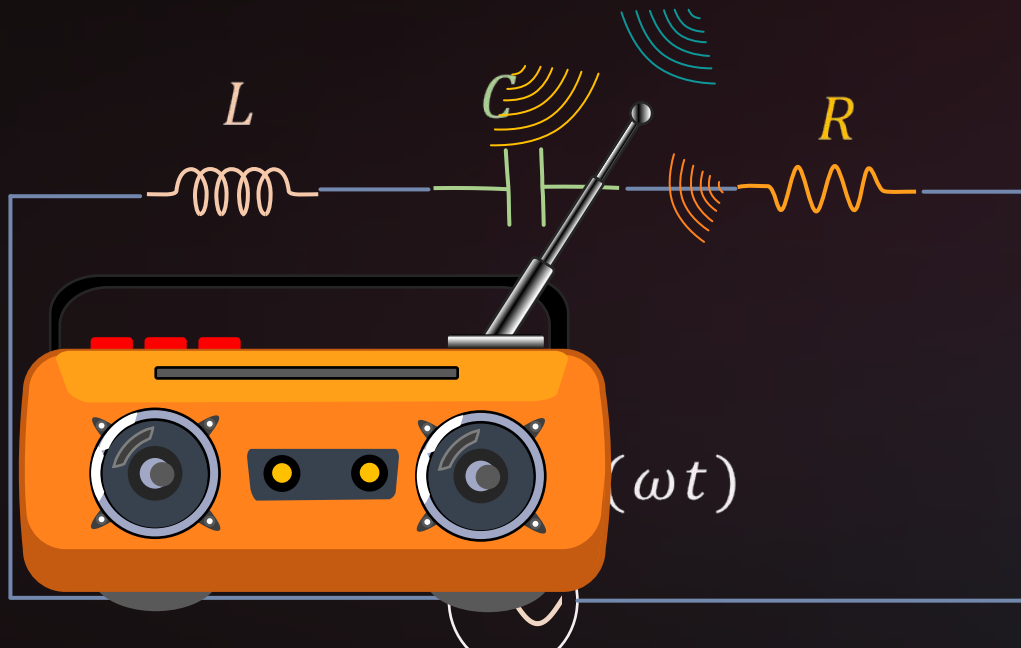
Radio Tuning

To hear one particular radio station, radio tuning is required.



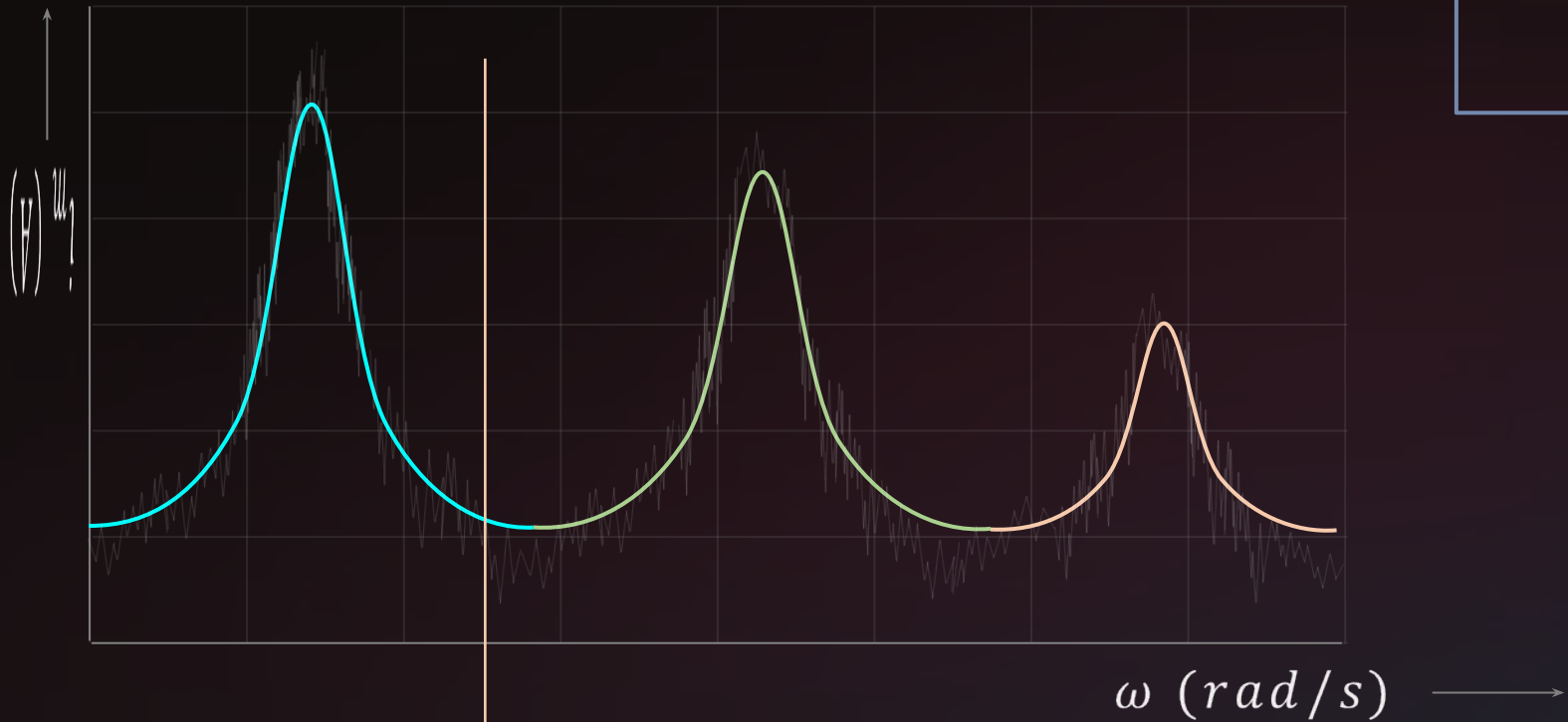
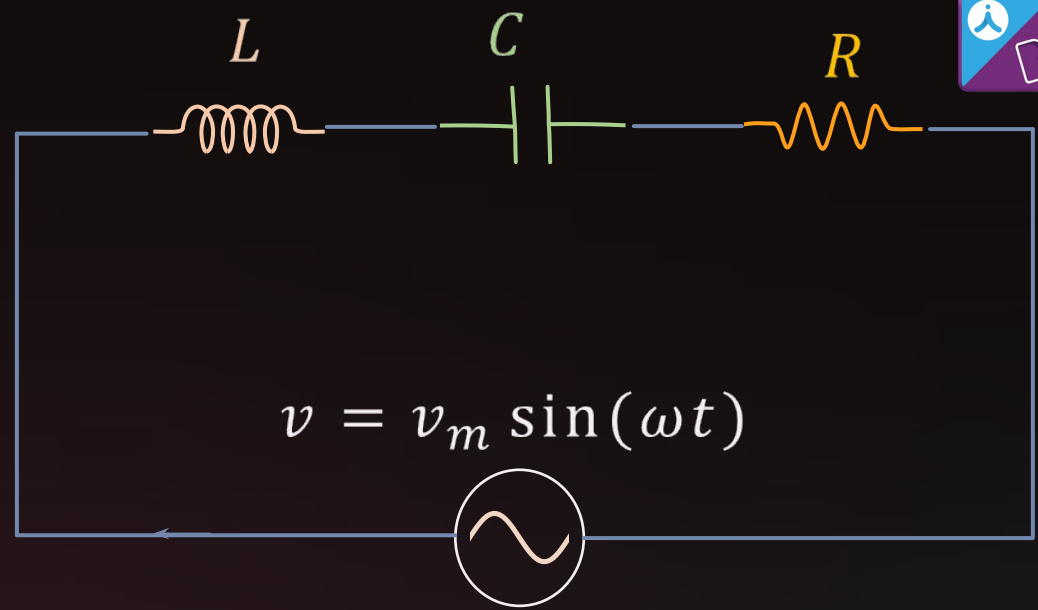
RESONANCE

Radio Tuning



RESONANCE

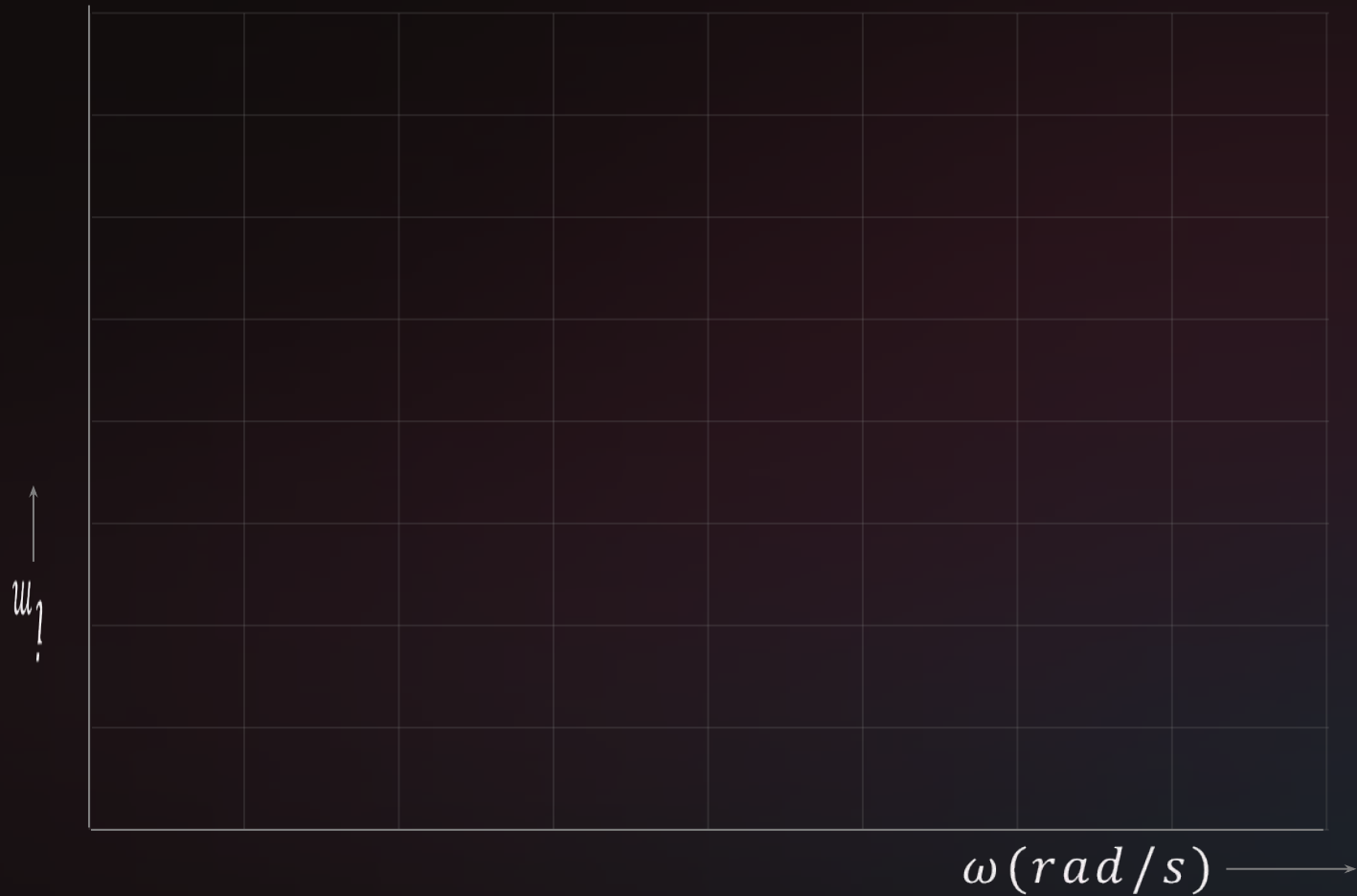
Radio Tuning



$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

RESONANCE

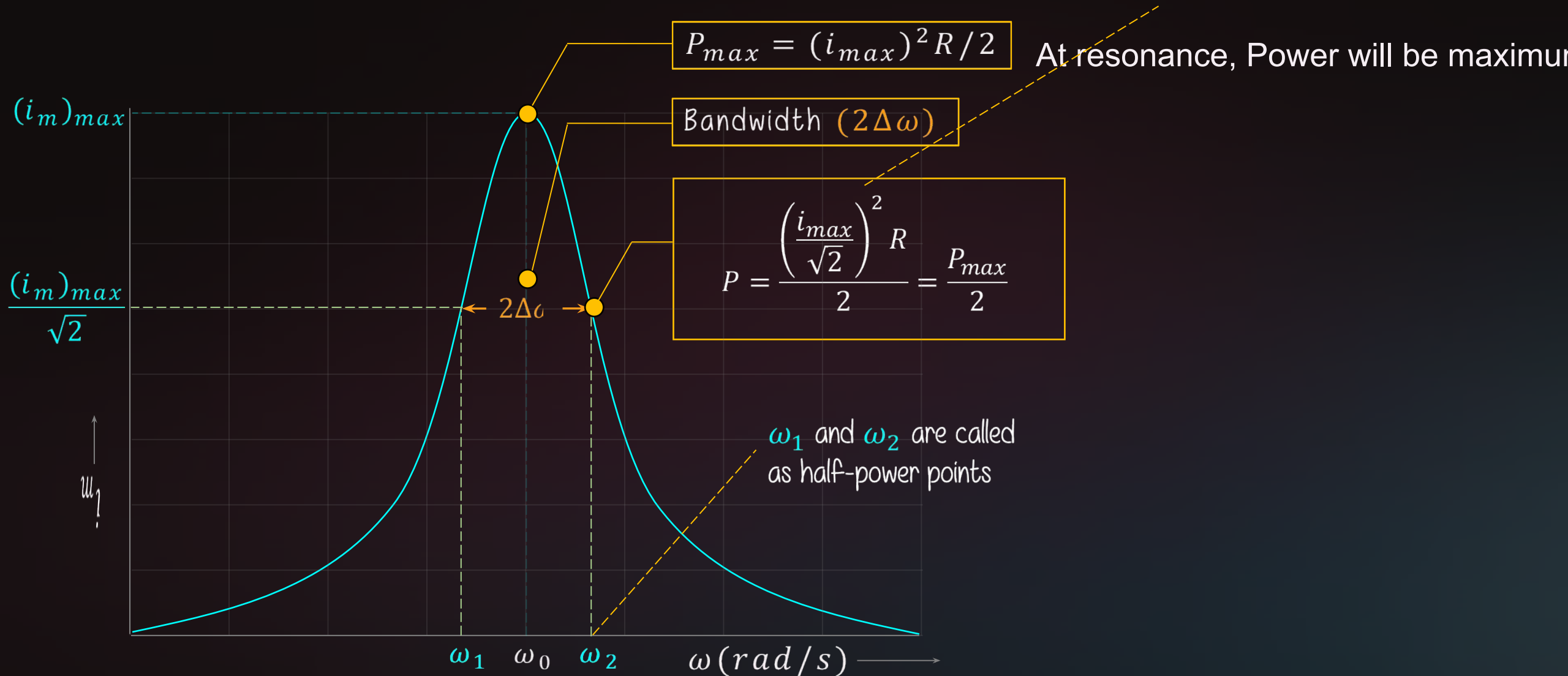
BANDWIDTH & POWER



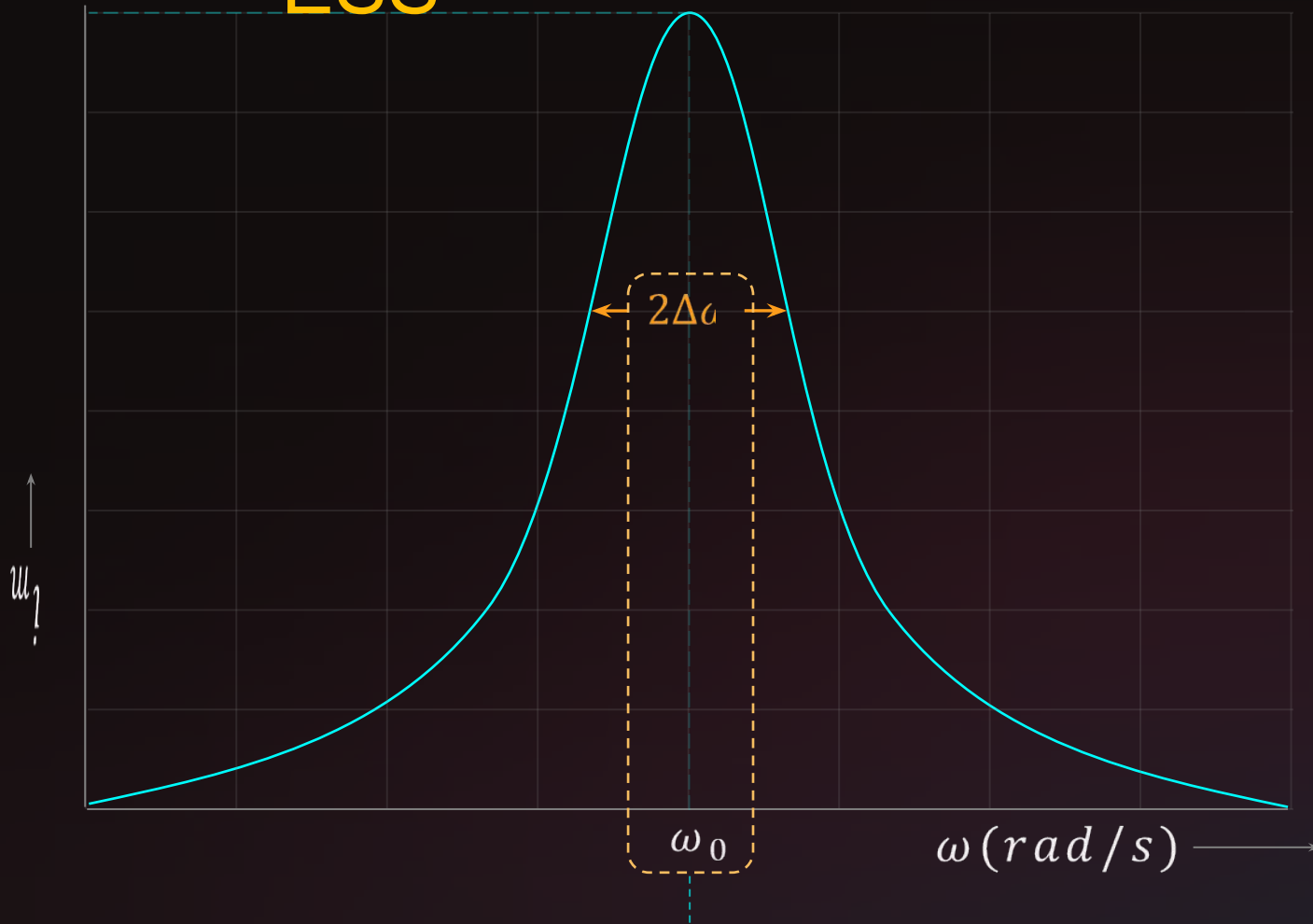
RESONANCE BANDWIDTH & POWER



- The current will be $1/\sqrt{2}$ times the maximum value of current at ω_1 and ω_2 .



RESONANCE SHARPNESS



$$\Delta\omega = \frac{R}{2L}$$

SMALL $\Delta\omega$

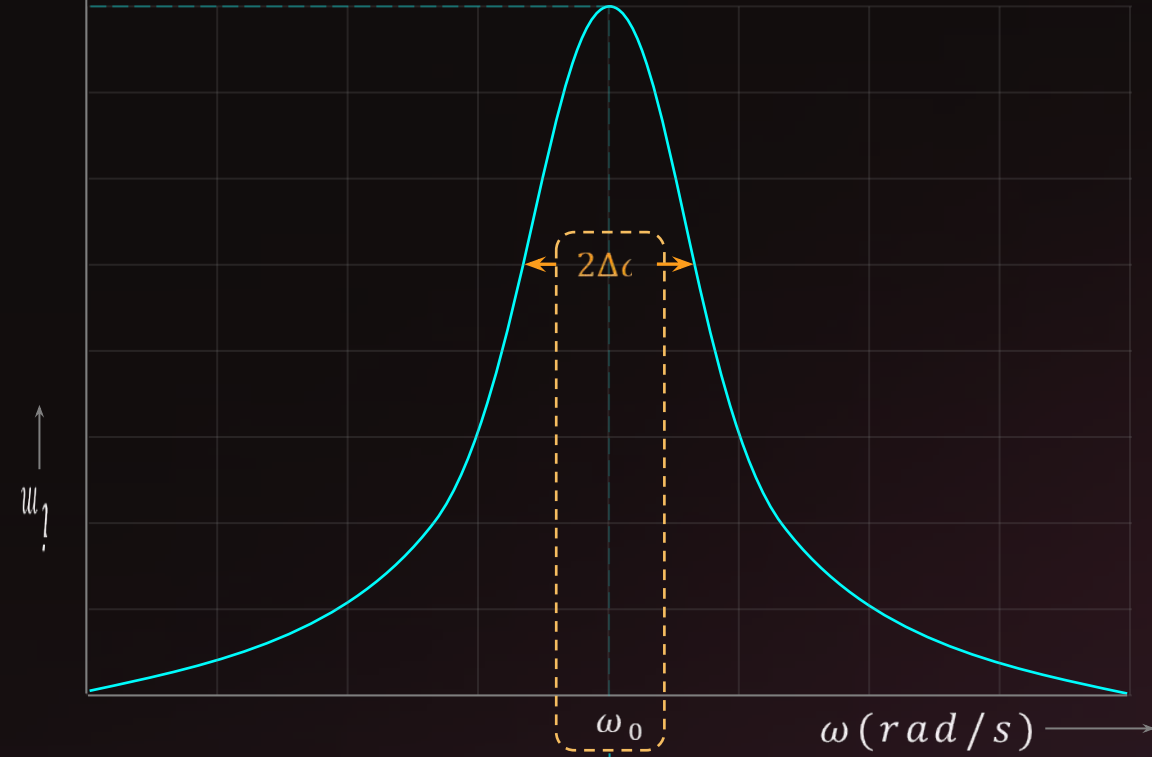
GOOD
TUNNING

HIGH
SHARPNESS

LOW
BANDWIDTH

The quantity $(\omega_0/2\Delta\omega)$ is regarded as a measure of sharpness of resonance.

RESONANCE SHARPNESS



Sharpness of resonance

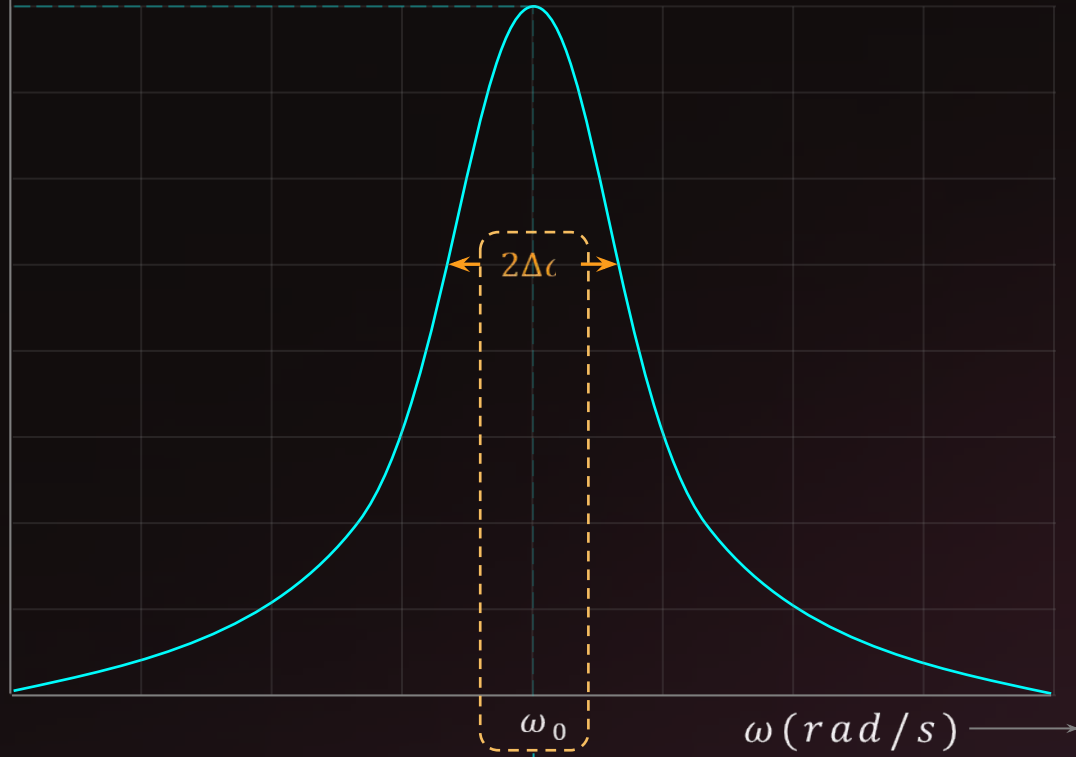
$$\frac{\omega_0}{2\Delta\omega} = \frac{\omega_0 L}{R}$$

Quality Factor, Q

The quantity $(\omega_0/2\Delta\omega)$ is regarded as a measure of sharpness of resonance.

$$\Delta\omega = \frac{R}{2L}$$

RESONANCE SHARPNESS



The quantity $(\omega_0/2\Delta\omega)$ is regarded as a measure of sharpness of resonance.

$$\Delta\omega = \frac{R}{2L}$$

Sharpness of resonance $\frac{\omega_0}{2\Delta\omega} = \boxed{\frac{\omega_0 L}{R}}$

Quality Factor, Q

At resonance, Q can also be defined as

$$Q = \frac{V_L}{V_R} = \frac{V_C}{V_R}$$

$$Q = \frac{i_0 \omega_0 L}{i_0 R} = \frac{i_0}{\omega_0 C i_0 R}$$

$$Q = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 R C} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

RESONANCE QUALITY FACTOR

$$Q = \frac{\omega_0}{2\Delta\omega}$$

$$(\because \Delta\omega = \frac{R}{2L})$$

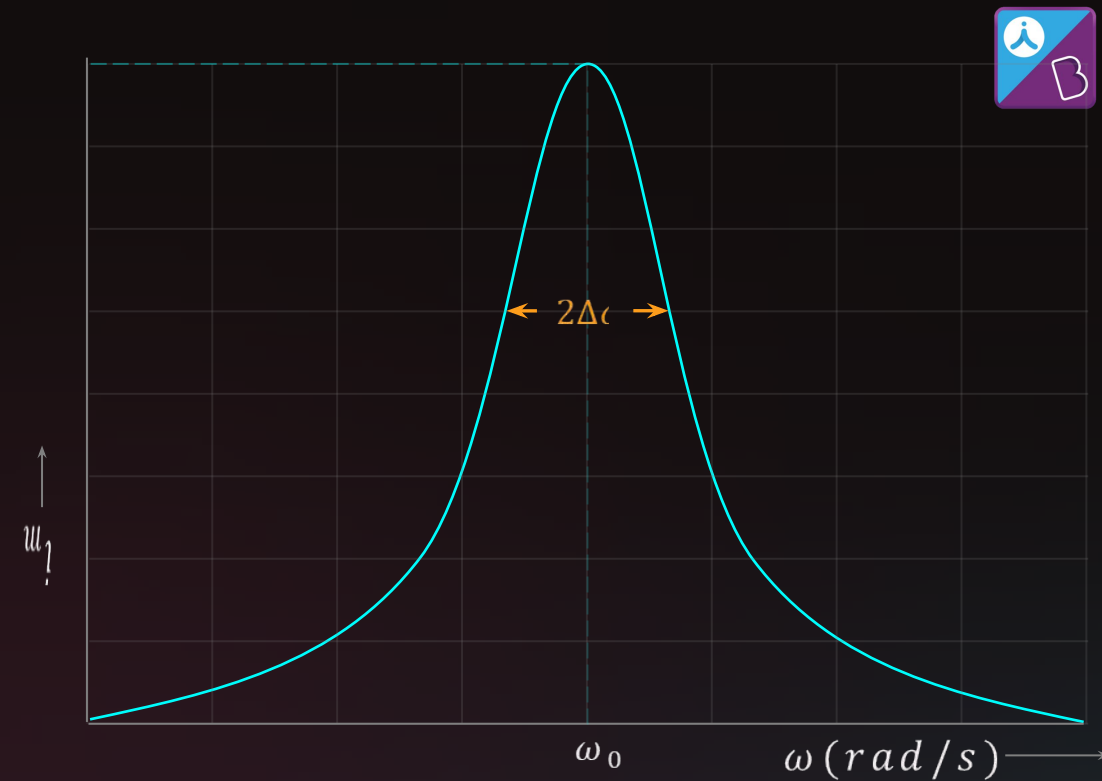
$$Q = \frac{\omega_0 L}{R}$$

$$(\because \omega_0^2 = 1/LC)$$

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$(\because L = 1/\omega_0^2 C)$$

$$Q = \frac{1}{\omega_0 RC}$$





Question



Which of the following combination should be selected for better tuning of an L-C-R circuit used for communication?



$$\begin{aligned} R &= 25 \, \Omega, \\ L &= 1.5 \, H, \\ C &= 45 \, \mu F \end{aligned}$$



$$\begin{aligned} R &= 20 \, \Omega, \\ L &= 1.5 \, H, \\ C &= 35 \, \mu F \end{aligned}$$



$$\begin{aligned} R &= 25 \, \Omega, \\ L &= 2.5 \, H, \\ C &= 45 \, \mu F \end{aligned}$$



$$\begin{aligned} R &= 15 \, \Omega, \\ L &= 3.5 \, H, \\ C &= 30 \, \mu F \end{aligned}$$



Y



For better tuning, the quality factor of the circuit should be high.



$R = 25 \Omega,$
 $L = 1.5 H,$
 $C = 45 \mu F$



$R = 20 \Omega,$
 $L = 1.5 H,$
 $C = 35 \mu F$



$R = 25 \Omega,$
 $L = 2.5 H,$
 $C = 45 \mu F$



L should be high.

$$Q = \frac{1}{\overline{R}} \sqrt{\frac{\overline{L}}{\overline{C}}}$$

L should be high.

Value of R and C should be minimum



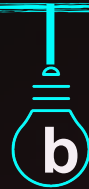
Answer



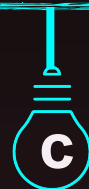
Which of the following combination should be selected for better tuning of an L-C-R circuit used for communication?



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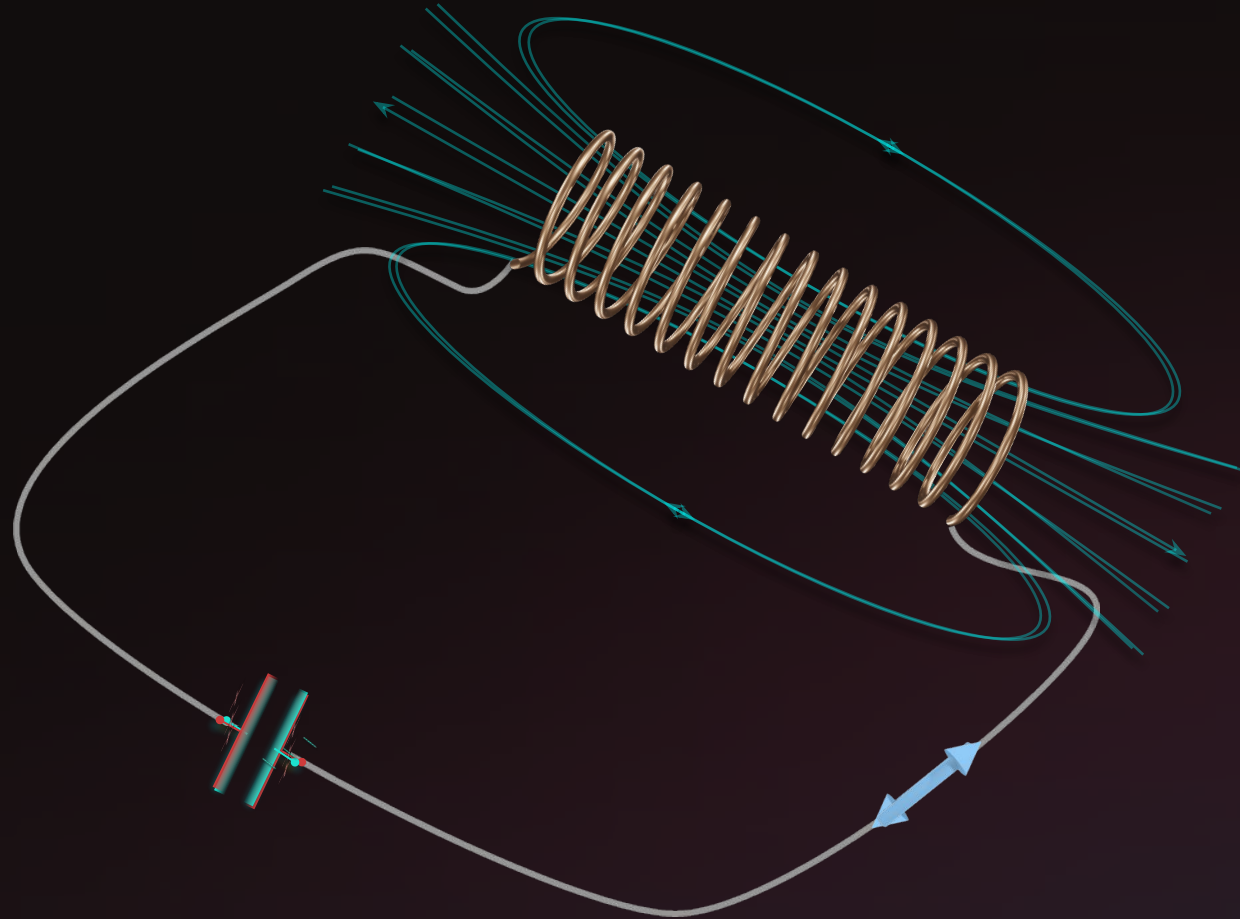


$$\begin{aligned} R &= 25 \, \Omega, \\ L &= 2.5 \, H, \\ C &= 45 \, \mu F \end{aligned}$$

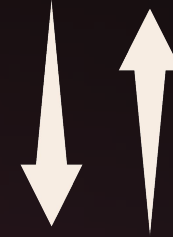


$$\begin{aligned} R &= 15 \, \Omega, \\ L &= 3.5 \, H, \\ C &= 30 \, \mu F \end{aligned}$$

LC OSCILLATION)

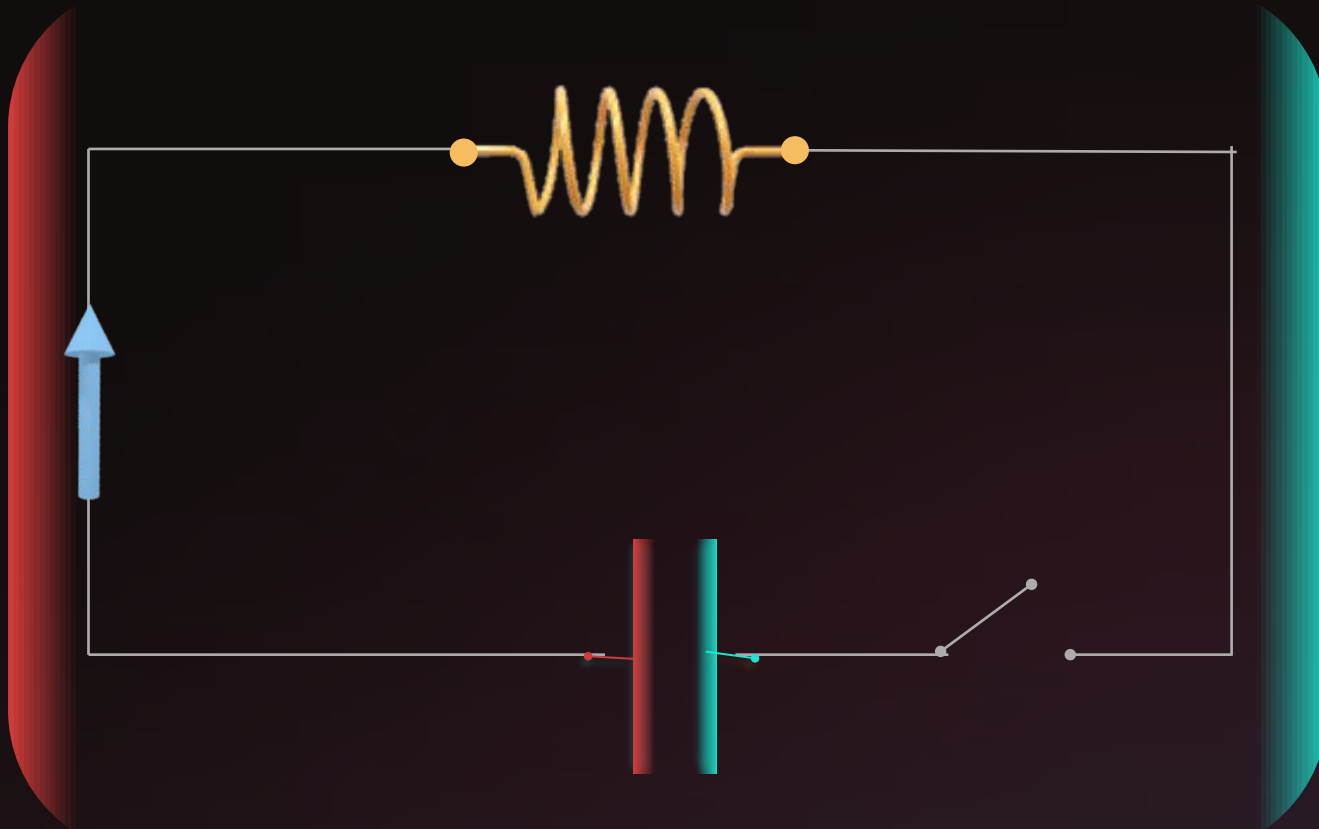


Electric
Energy

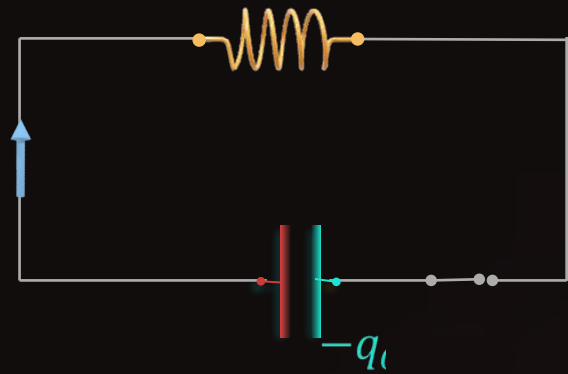


Magnetic
Energy

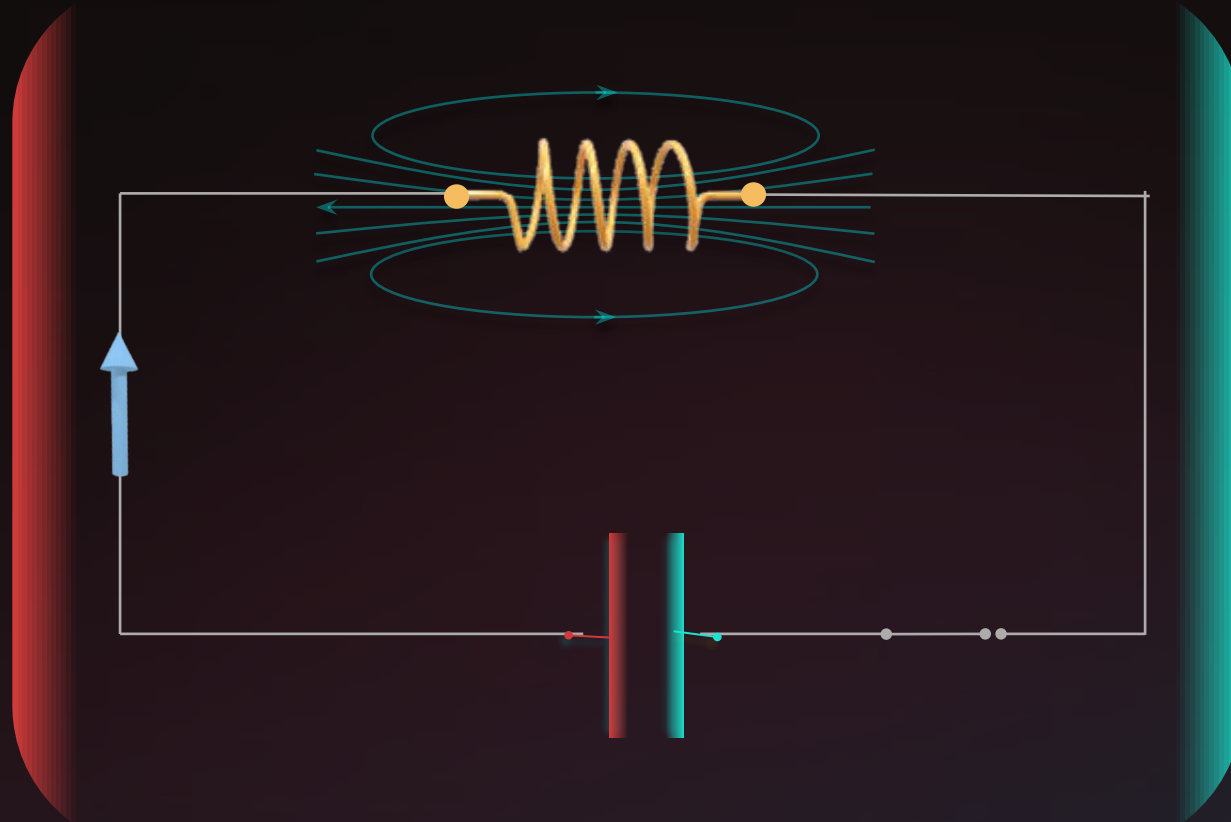
LC OSCILLATION)



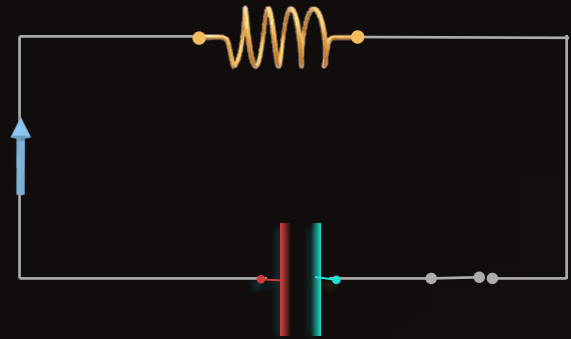
LC OSCILLATION)



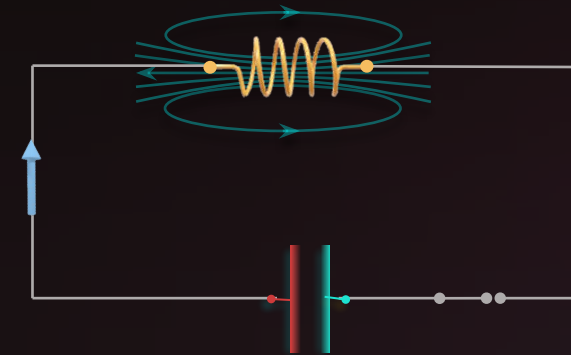
Step 1



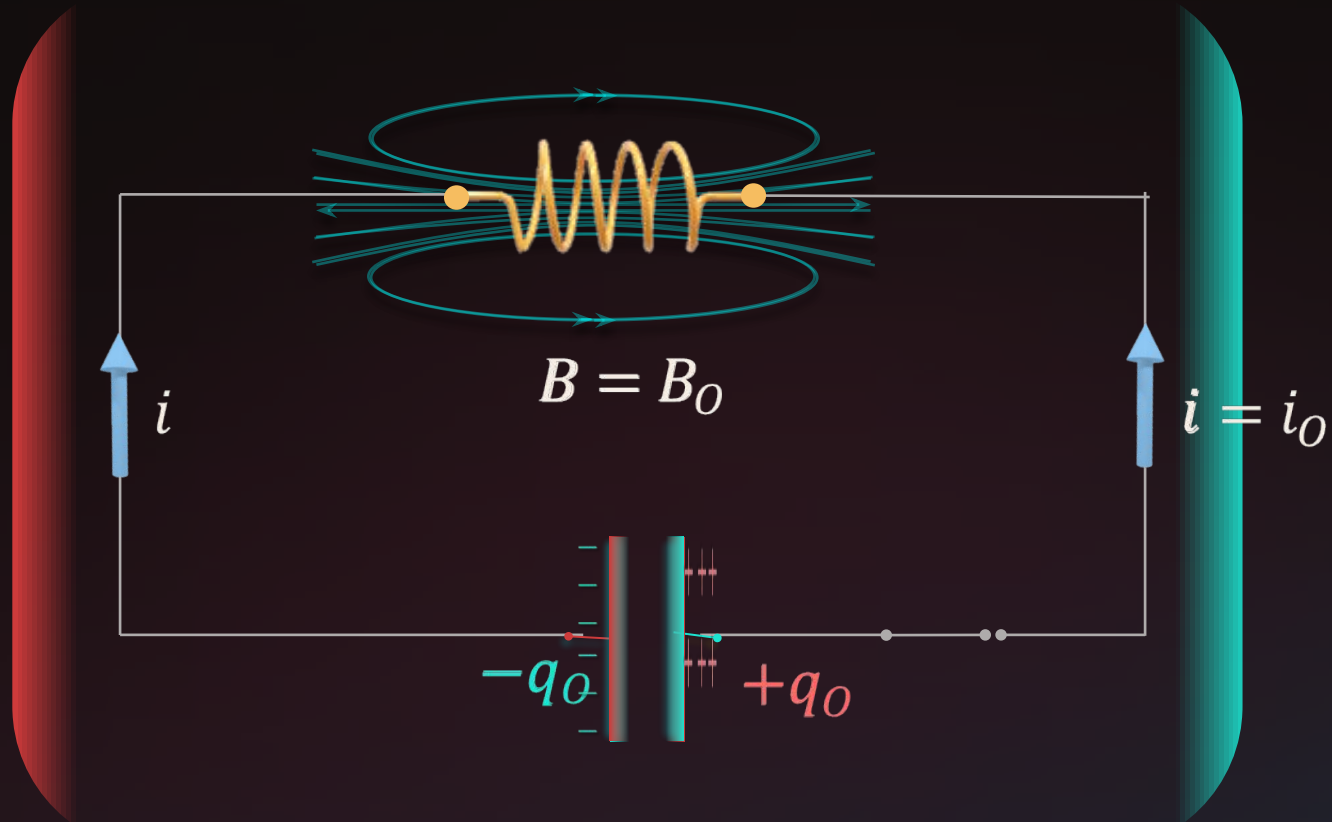
LC OSCILLATION)



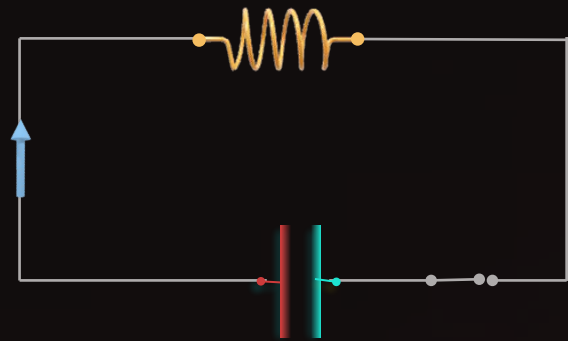
Step 1



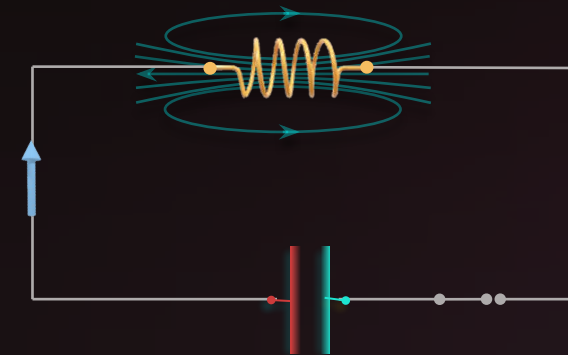
Step 2



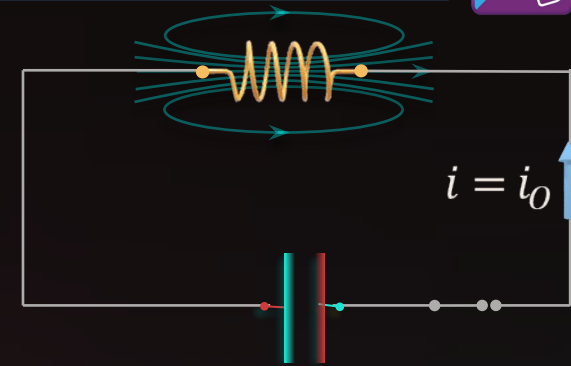
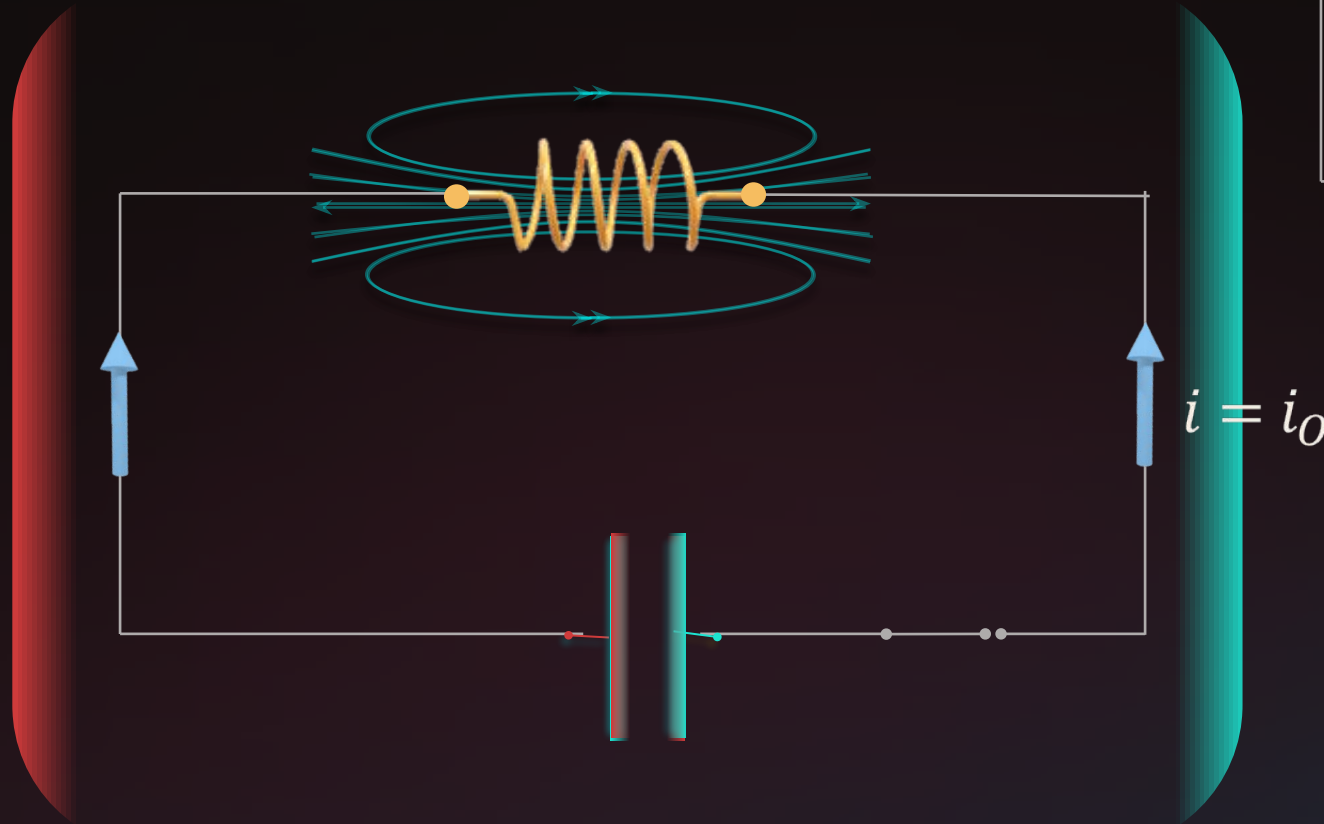
LC OSCILLATION)



Step 1



Step 2



Step 3

Now the same oscillation and steps will occur

LC OSCILLATION

Oscillation period



At $t = 0$,

Current, $i = 0$

Charge on capacitor, $q = q_m$

Induced emf across the inductor, $L \frac{di}{dt} = 0$



LC OSCILLATION

Oscillation period



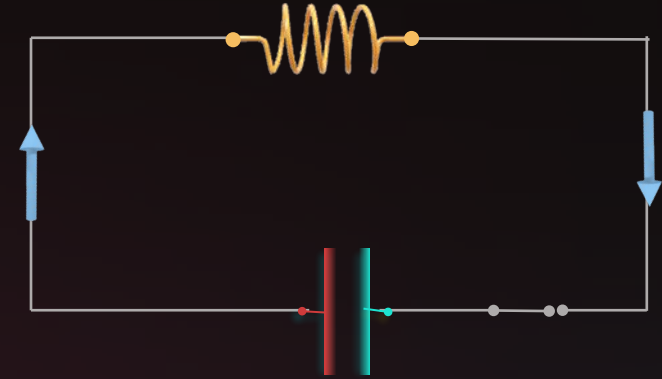
At time, t

Current = i

Charge on capacitor = q

Potential difference = $\frac{q}{c}$

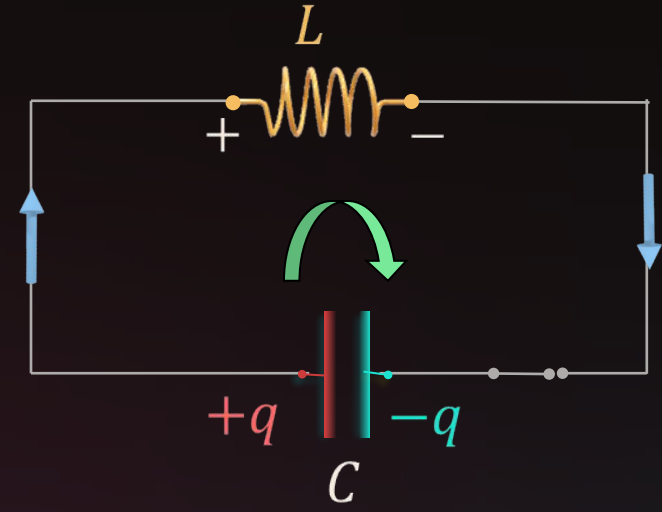
Induced emf across the inductor, $L \frac{di}{dt} = 0$



LC OSCILLATION

Oscillation
period

Applying Kirchhoff's Law



LC OSCILLATION



period

Applying Kirchhoff's Law

$$\frac{q}{C} - L \frac{di}{dt} = 0 \dots (1) \quad \left| \quad i = -\frac{dq}{dt} \right.$$

$$\frac{q}{C} - L \frac{d\left(-\frac{dq}{dt}\right)}{dt} = 0 \Rightarrow \frac{q}{LC} + \frac{d^2q}{dt^2} = 0$$

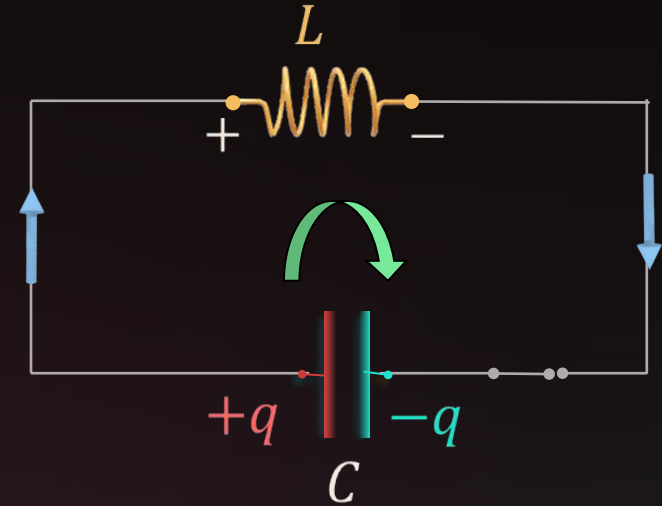
$$\left(\frac{d^2q}{dt^2} + \frac{q}{LC} = 0 \right)$$

For a particle in SHM

$$\frac{d^2x}{dt^2} + \omega_o^2 x = 0 \dots (3)$$

$$\omega = \sqrt{\frac{k}{m}}$$

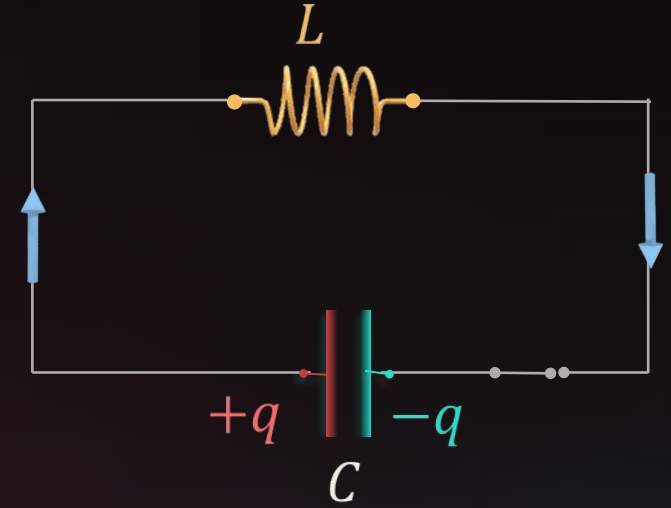
$$\omega^2 = \frac{1}{LC} \Rightarrow \omega = \frac{1}{\sqrt{LC}}$$



LC OSCILLATION

Oscillation period

$$\frac{d^2 q}{dt^2} + \frac{q}{LC} = 0 \dots (2)$$



LC OSCILLATION

period

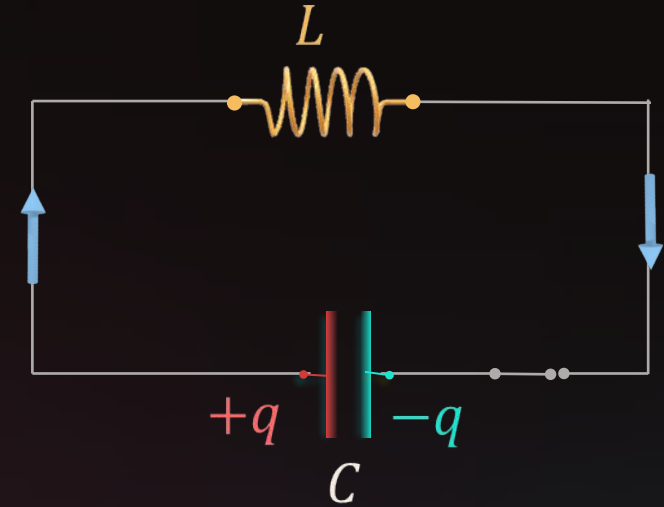


$$\frac{d^2 q}{dt^2} + \frac{q}{LC} = 0 \dots (2)$$

For a particle in SHM

$$\frac{d^2 x}{dt^2} + \omega_o^2 x = 0 \dots (3) \quad \left| \quad \omega = \sqrt{\frac{k}{m}} \right.$$

$$\omega^2 = \frac{1}{LC} \Rightarrow \omega = \frac{1}{\sqrt{LC}}$$

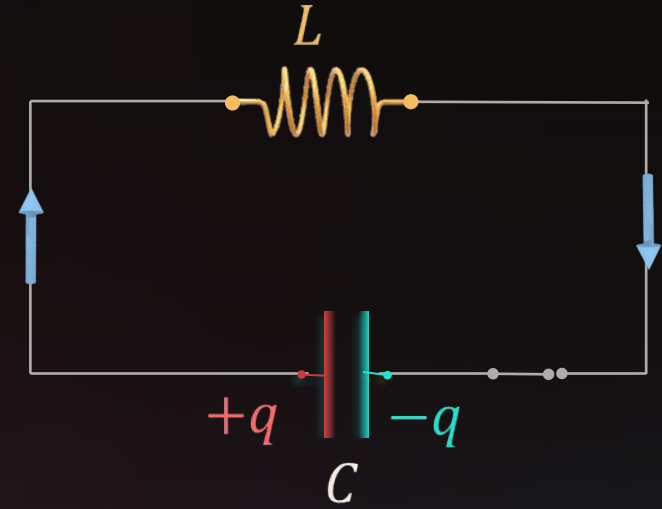


LC OSCILLATION

Oscillation
period

$$\frac{d^2x}{dt^2} + \omega_o^2 x = 0 \dots (3)$$

$$\omega = \frac{1}{\sqrt{LC}}$$



LC OSCILLATION

Oscillation period

$$\frac{d^2x}{dt^2} + \omega_o^2 x = 0 \dots (3)$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$x = A \cos(\omega_o t + \phi)$$

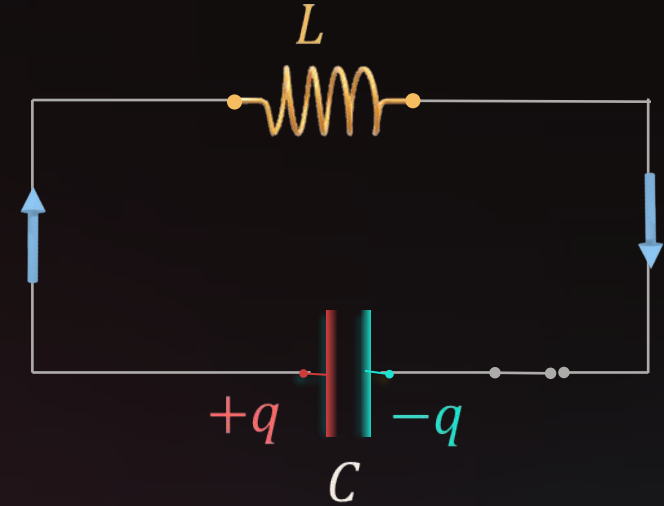
$$q = q_m \cos(\omega_o t + \phi) \dots (4)$$

$$\text{At } t = 0, q = q_m$$

$$\Rightarrow q_m = q_m \cos(\phi)$$

$$\Rightarrow \cos(\phi) = 1 \Rightarrow \phi = 0$$

$$\sim q = q_m \cos(\omega_o t) \sim$$

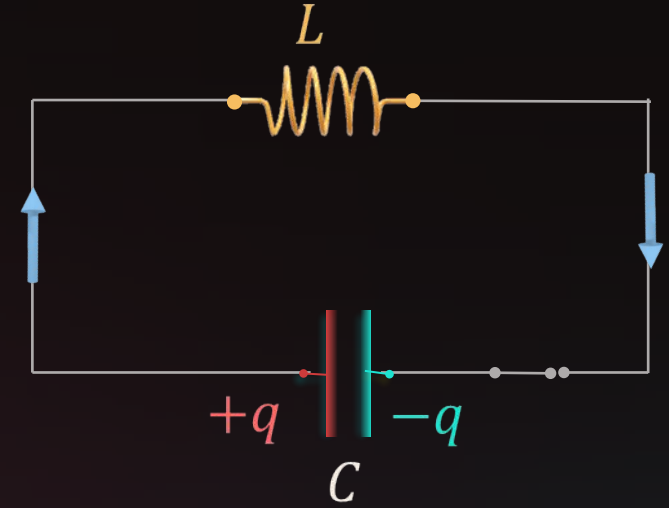


LC OSCILLATION

Oscillation period

$$q = q_m \cos(\omega_o t) \dots (5)$$

$$\omega = \frac{1}{\sqrt{LC}}$$



LC OSCILLATION

period

$$q = q_m \cos(\omega_o t) \dots (5)$$

$$\omega = \frac{1}{\sqrt{LC}}$$

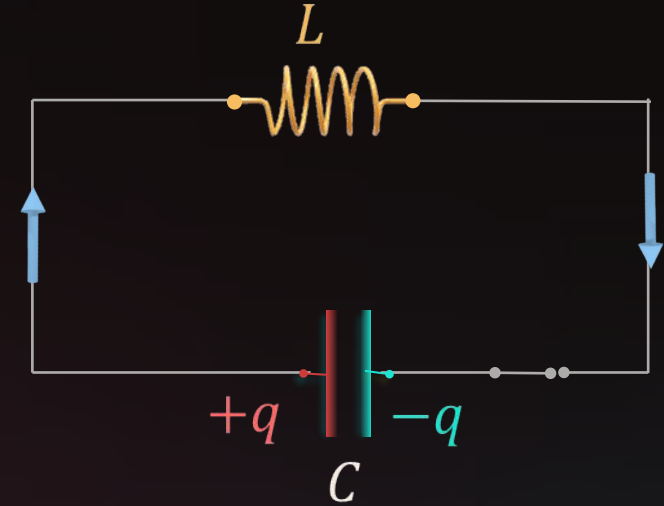
$$\Rightarrow i = -\frac{d}{dt}[q_m \cos(\omega_o t)]$$

$$i = -\frac{dq}{dt}$$

$$\Rightarrow i = \omega_o q_m \sin(\omega_o t)$$

$$i_m = \omega_o q_m$$

$$\sim i = i_m \sin(\omega_o t) \sim$$



LC OSCILLATION

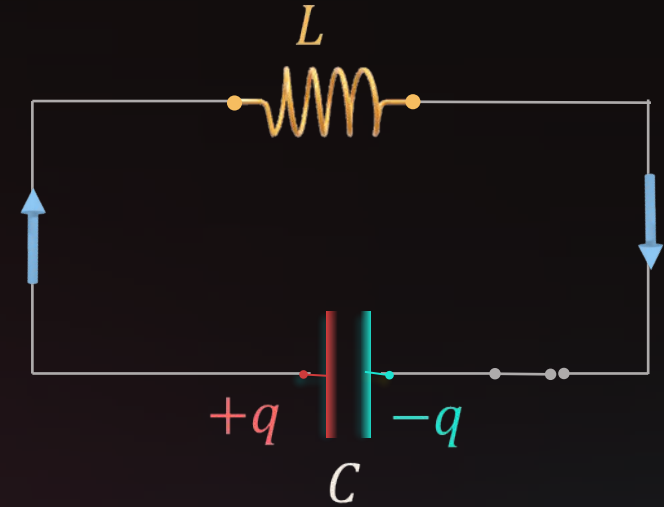
Oscillation period

$$q = q_m \cos(\omega_o t) \dots (5)$$

$$i = i_m \sin(\omega_o t) \dots (6)$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$i_m = \omega_o q_m$$



LC OSCILLATION

Oscillation period

$$q = q_m \cos(\omega_o t) \dots (5)$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$i_m = \omega_o q_m$$

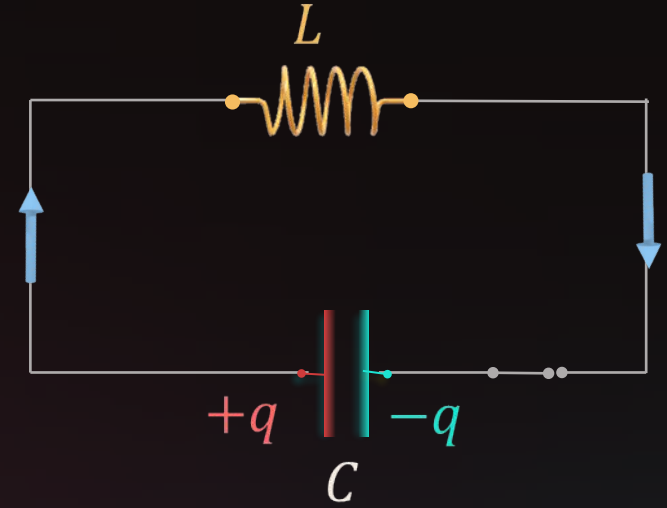
$$i = i_m \sin(\omega_o t) \dots (6)$$

$$U = \frac{q^2}{2C}, \quad U' = \frac{1}{2} L i^2$$

$$L = \frac{1}{\omega_o^2 C}$$

$$U_{Total} = U + U'$$

$$\sim U_{Total} = \frac{q^2}{2C} + \frac{1}{2} L i^2 \sim$$



LC OSCILLATION

period

$$q = q_m \cos(\omega_o t) \dots (5)$$

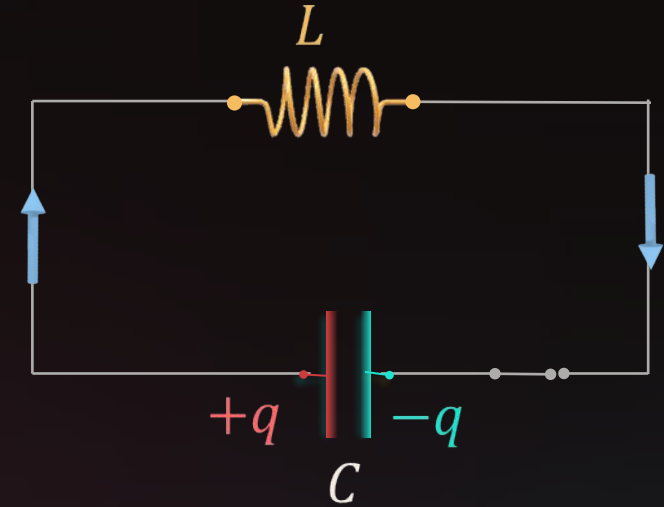
$$i = i_m \sin(\omega_o t) \dots (6)$$

$$U_{Total} = \frac{q^2}{2C} + \frac{1}{2}Li^2$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$i_m = \omega_o q_m$$

$$L = \frac{1}{\omega_o^2 C}$$



LC OSCILLATION

Oscillation period



$$q = q_m \cos(\omega_o t) \dots (5)$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$i_m = \omega_o q_m$$

$$i = i_m \sin(\omega_o t) \dots (6)$$

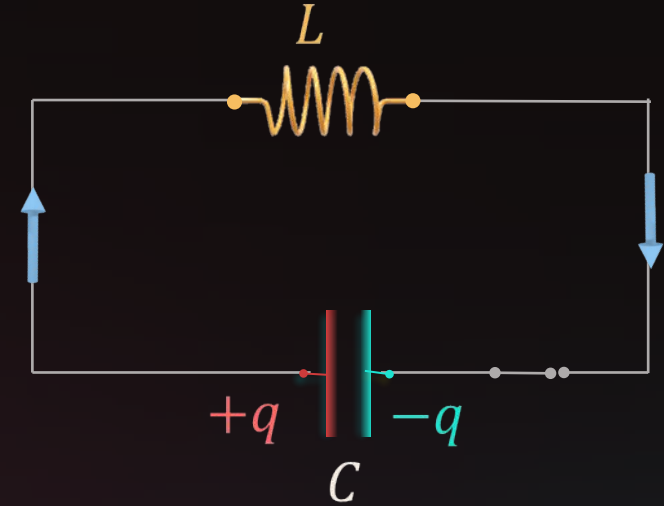
$$L = \frac{1}{\omega_o^2 C}$$

$$U_{Total} = \frac{q^2}{2C} + \frac{1}{2} L i^2$$

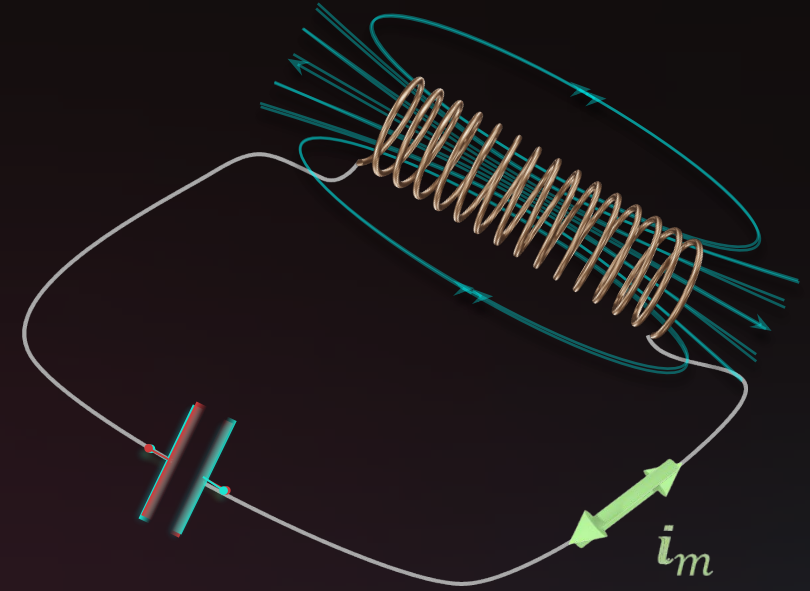
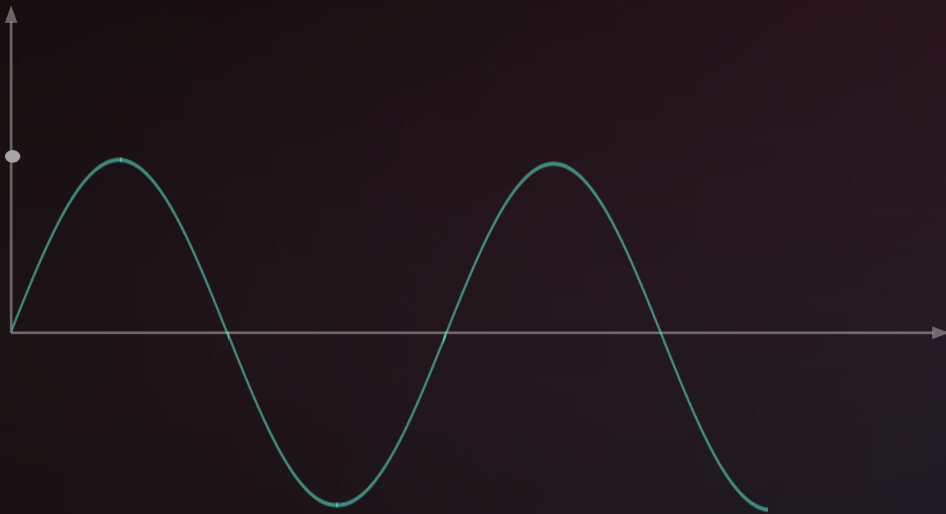
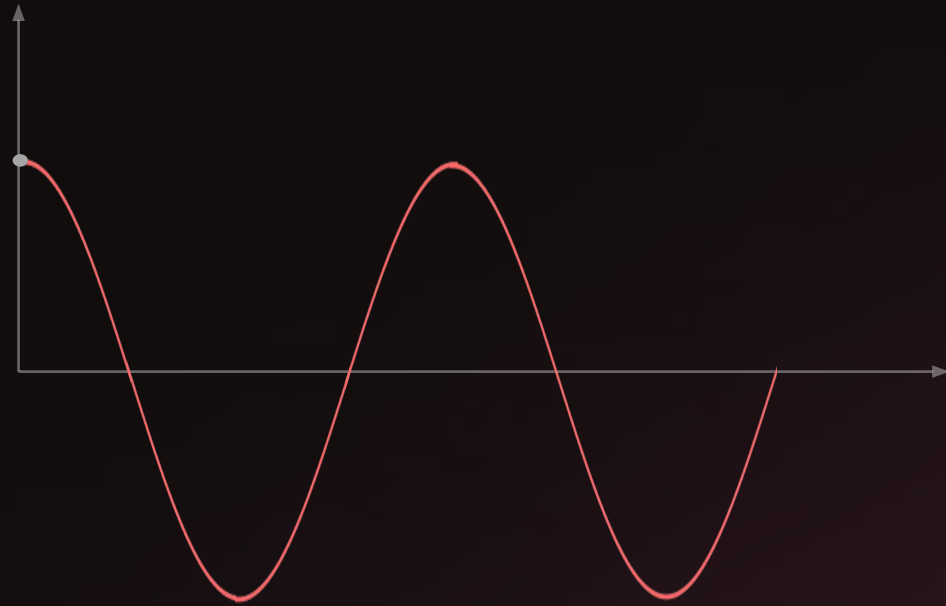
$$U_{Total} = \frac{[q_m \cos(\omega_o t)]^2}{2C} + \frac{1}{2} \frac{1}{\omega_o^2 C} [i_m \sin(\omega_o t)]^2$$

$$U_{Total} = \frac{(q_m)^2}{2C} [(\cos^2 \omega_o t) + (\sin^2 \omega_o t)]$$

$$\sim U_{Total} = \frac{q_m^2}{2C} \sim$$



LC OSCILLATION GRAPHS



LC OSCILLATION

Energy

