

RBSE Class 10th Maths Question Paper With Solution 2017

QUESTION PAPER CODE S-09-Mathematics

PART - A

Question 1: HCF and LCM of two integers are 12 and 336 respectively. If one integer is 48, then find another integer.

Solution:

HCF and LCM of two integers are 12 and 336.

First number \times Second number = HCF \times LCM

Let another integer be a

$$\Rightarrow 48 \times a = 12 \times 336$$

$$\Rightarrow a = [12 \times 336] / [48]$$

$$a = 84$$

Hence, the second integer is 84.

Question 2: Find the sum of the first 20 terms of the AP: 13, 8, 3,

Solution:

$$a = 13$$

$$d = 8 - 13 = -5$$

$$n = 20$$

$$S_n = [n / 2] [2a + [n - 1] d]$$

$$= [20 / 2] [2 * 13 + [20 - 1] * (-5)]$$

$$= [10] [26 - 95]$$

$$= 10 * [-69]$$

$$= -690$$

Question 3: If cosec A = 17 / 8, then calculate tan A.

Solution:

$$\operatorname{cosec} A = 17 / 8$$

$$h = 17$$

$$p = 8$$

$$b = ?$$

$$p^2 + b^2 = h^2$$

$$8^2 + b^2 = 17^2$$

$$b^2 = 17^2 - 8^2$$

$$b^2 = 289 - 64$$

$$b^2 = 225$$

$$b = 15$$

$$\tan A = p / b$$

$$= 8 / 15$$

Question 4: Write the trigonometric ratio of $\sin A$ in terms of $\cot A$.

Solution:

$$\sin A = 1 / \operatorname{cosec} A$$

$$= 1 / \sqrt{(1 + \cot^2 A)}$$

$$\cot^2 A + 1 = \operatorname{cosec}^2 A$$

$$\operatorname{cosec} A = \sqrt{(1 + \cot^2 A)}$$

Question 5: If the ratio of corresponding medians of two similar triangles is 9:16, then find the ratio of their areas.

Solution:

The theorem states that "the ratio of the areas of two triangles is equal to the square of the ratio of their corresponding medians".

Thus, we have,

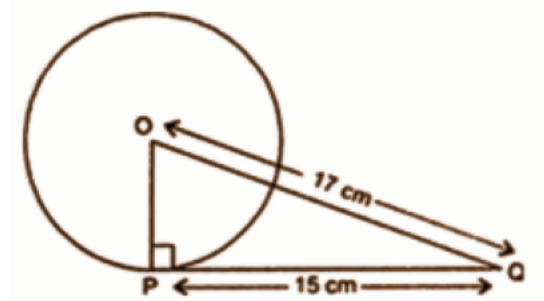
$$\text{Ratio of medians} = 9:16 = 9 / 16$$

$$\text{Ratios of their areas} = [9 / 16]^2$$

$$= 81 / 256$$

Question 6: From a point Q, the length of the tangent to a circle is 15 cm and the distance of Q from the centre of the circle is 17 cm, then find the radius of the circle.

Solution:



$$PQ = 15\text{cm}$$

$$OQ = 17\text{cm}$$

To find the radius OP

$$OQ^2 = OP^2 + PQ^2$$

$$17^2 = OP^2 + 15^2$$

$$17^2 - 15^2 = OP^2$$

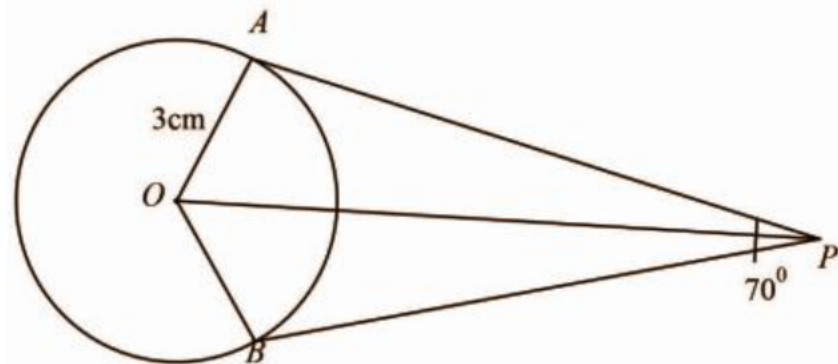
$$289 - 225 = OP^2$$

$$64 = OP^2$$

$$OP = 8\text{cm}$$

Question 7: Draw a pair of tangents to a circle of radius 5 cm which is inclined to each other at an angle of 70° .

Solution:



Question 8: If the circumference and the area of a circle are numerically equal, then find the radius of the circle.

Solution:

Area of circle = circumference of the circle

$$\Rightarrow \pi r^2 = 2\pi r$$

\Rightarrow Dividing by πr on both the sides

$$\Rightarrow r = 2$$

\Rightarrow So the radius of the circle is 2 units.

Question 9: Find the area of a quadrant of a circle whose circumference is 44 cm.

Solution:

Let radius be r cm.

Circumference, $2\pi r = 44$

$$\pi r = 22$$

$$[22 / 7] * r = 22$$

$$r = 7 \text{ cm}$$

Area of Quadrant = $[1 / 4] * \pi r^2$

$$= [1 / 4] * [22 / 7] * 7 * 7$$

$$= [22 * 7] / 4$$

$$= 154 / 4$$

$$= 38.5 \text{ cm}^2$$

Question 10: If the probability of “not E” = 0.95, then find P(E).

Solution:

$$P(\text{not E}) = 0.95$$

$$\text{Thus } P(E) = 1 - P(\text{not E})$$

$$\Rightarrow P(E) = 1 - 0.95$$

$$\Rightarrow P(E) = 0.05$$

PART - B

Question 11: Name the type of quadrilateral formed by the points (4, 5), (7, 6), (4, 3), (1, 2).

Solution:

Let the points (4, 5), (7, 6), (4, 3), and (1, 2) be representing the vertices A, B, C, and D of the given quadrilateral respectively.

$$AB = \sqrt{(4 - 7)^2 + (5 - 6)^2} = \sqrt{(-3)^2 + (-1)^2} = \sqrt{9 + 1} = \sqrt{10}$$

$$BC = \sqrt{(7 - 4)^2 + (6 - 3)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9 + 9} = \sqrt{18}$$

$$CD = \sqrt{(4 - 1)^2 + (3 - 2)^2} = \sqrt{(3)^2 + (1)^2} = \sqrt{9 + 1} = \sqrt{10}$$

$$AD = \sqrt{(4 - 1)^2 + (5 - 2)^2} = \sqrt{(3)^2 + (3)^2} = \sqrt{9 + 9} = \sqrt{18}$$

$$\text{Diagonal AC} = \sqrt{(4 - 4)^2 + (5 - 3)^2} = \sqrt{(0)^2 + (2)^2} = \sqrt{0 + 4} = 2$$

$$\text{Diagonal BD} = \sqrt{(7 - 1)^2 + (6 - 2)^2} = \sqrt{(6)^2 + (4)^2} = \sqrt{36 + 16} = \sqrt{52}$$

The opposite sides of this quadrilateral are of the same length. However, the diagonals are of different lengths.

Therefore, the given points are the vertices of a parallelogram.

Question 12: A vessel is in the form of a hollow hemisphere. The diameter of the hemisphere is 14 cm. Find the inner surface area of the vessel.

Solution:

$$D = 14\text{cm (given)}$$

$$R = 14 / 2 = 7\text{cm}$$

$$\text{CSA of hemisphere} = 2\pi r^2$$

$$= 2 \times [22 / 7] \times 7 \times 7$$

$$= 44 \times 7$$

$$= 308 \text{ cm}^2$$

Question 13: The following distribution shows the daily pocket allowance of children of a locality.

Daily pocket	10 - 20	20 - 30	30 - 40	40 - 50	50 - 60
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allowance					
Number of children	3	5	4	7	6

Find the mean daily pocket allowance by using the appropriate method.

Solution:

Daily pocket allowance	10 - 20	20 - 30	30 - 40	40 - 50	50 - 60
Number of children (f_i)	3	5	4	7	6
Midpoint (x_i)	15	25	35	45	55
$f_i x_i$	45	125	140	315	330

$$\begin{aligned} \text{Mean} &= \frac{\sum f_i x_i}{\sum f_i} \\ &= 955 / 25 \\ &= 38.2 \end{aligned}$$

Question 14: A car travels 260 km distance from a place A to place B, at a uniform speed 65 km/hr passes through all thirteen green traffic signals, 4 minutes at the first signal, 7 minutes at the second signal, 10 minutes at a third signal and so on stops for 40 minutes at the thirteenth signal. How much total time does it take to reach place B? Solve by suitable Mathematical Method.

Solution:

Time sequence forms an A.P: 4, 7, 10.....

$$a = 4$$

$$d = 7 - 4 = 3$$

For the 13th station, time = 40

Total time is the sum of the first thirteen terms of the sequence

$$S = [n / 2] \{2a + (n - 1) d\}$$

$$S = [13 / 2] \{2(4) + (13 - 1) 3\}$$

$$S = [13 / 2] [8 + 36]$$

$$S = [13 / 2] \times 44$$

$$S = 286$$

$$S = [286 / 60] \text{ hour}$$

$$= 4 + [286 / 60]$$

$$= [240 + 286] / 60$$

$$= 526 / 60$$

$$= 8.76 \text{ hours}$$

Question 15: For traffic control, a CCTV camera is fixed on a straight and vertical pole. The camera can see 113 m distance straight from the top. If the area visible by the camera around the pole is 39424 m², then find the height of the pole.

Solution:

The height of the pole = 15m

As the area visible by the camera around the pole would form a circle.

Thus, the area visible by the camera around the pole = πr^2

Here, the correct area visible by the camera around the pole = 39424 m²

$$\Rightarrow 39424 \text{ m}^2 = (22 / 7) * r^2$$

$$\Rightarrow r^2 = 12544$$

$$\Rightarrow r = 112 \text{ m}$$

Thus, the radius of circle = 112 m

Also, the camera can see 113 m distance from the top.

So, A right triangle is formed whose base is 112 m and the hypotenuse is 113 m.

Thus, perpendicular = $\sqrt{\text{hypotenuse}^2 - \text{base}^2}$

$$= \sqrt{113^2 - 112^2}$$

$$= \sqrt{225}$$

$$= 15 \text{ m}$$

Thus, the height of the pole = 15 m.

PART - C

Question 16: Prove that $\sqrt{3}$ is an irrational number.

Solution:

Let us assume that $\sqrt{3}$ is a rational number.

A rational number should be in the form of p / q , where p and q are a coprime number.

$$\sqrt{3} = p / q \text{ \{ where } p \text{ and } q \text{ are co- prime\}}$$

$$\sqrt{3}q = p$$

Now, by squaring both the side we get,

$$(\sqrt{3}q)^2 = p^2$$

$$3q^2 = p^2 \text{ (i)}$$

So, if 3 is the factor of p^2 then, 3 is also a factor of p (ii)

\Rightarrow Let $p = 3m$ { where m is any integer }

Squaring both sides,

$$p^2 = (3m)^2$$

$$p^2 = 9m^2$$

Putting the value of p^2 in equation (i)

$$3q^2 = p^2$$

$$3q^2 = 9m^2$$

$$q^2 = 3m^2$$

So, if 3 is a factor of q^2 , then, 3 is also a factor of q .

Since 3 is the factor of p & q both, our assumption that p & q are coprime is wrong.

Hence $\sqrt{3}$ is an irrational number.

Question 17: Divide $x^3 - 6x^2 + 11x - 6$ by $x - 2$, and verify the division algorithm.

Solution:

$$\begin{array}{r}
 \overline{) x^3 - 6x^2 + 11x - 6} \\
 \underline{x^3 - 2x^2} \\
 -4x^2 + 11x - 6 \\
 \underline{-4x^2 + 8x - 6} \\
 3x - 6 \\
 \underline{3x - 6} \\
 0
 \end{array}$$

$$\begin{aligned}
 \text{Dividend} &= \text{Quotient} * \text{Divisor} + \text{Remainder} \\
 &= (x - 2)(x^2 - 4x + 3) + 0 \\
 &= x^3 - 4x^2 + 3x - 2x^2 + 8x - 6 \\
 &= x^3 - 6x^2 + 11x - 6
 \end{aligned}$$

Question 18: A manufacturer of TV sets produced 720 sets in the fourth year and 1080 sets in the sixth year. Assuming that the production increases uniformly by a fixed number every year, then find total production in the first 9 years.

Solution:

Simplify the expression,

720 set in the fourth year

1080 set in the sixth year

2-year difference value of the sixth year - 4 year = 1080 - 720 = 360

2 difference = 360

1 year produced is = 360 / 2 = 180

Then, 1 year produced is 180

9-year total production are = 180 * 9 = 1620

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9 year total production are = 180 * 9 = 1620

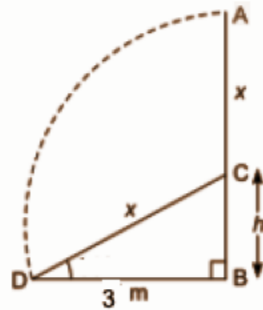
9 year total production are = 1620

Hence, the total production of 9 years is 1620.

Question 19: A tree breaks due to a storm and the broken part bends so that the top of the tree touches the ground making an angle 60° with it. The

distance between the foot of the tree to the point where the top touches the ground is 3 m. Find the height of the tree.

Solution:



Let the height of the tree before the storm is AB.

Due to the storm, it breaks from C such that its top touches the ground at D and makes an angle of 60° .

Let $AC = DC = x$ and $BC = h$, $BD = 3\text{m}$

Height of the tree = $BC = x + h$ ---- (1)

In triangle BCD,

$CD / BD = \sec 60^\circ$ and $BC / BD = \tan 60^\circ$

$x / 3 = 2$ and $h / 3 = \sqrt{3}$

$x = 6$ and $h = 3\sqrt{3}$

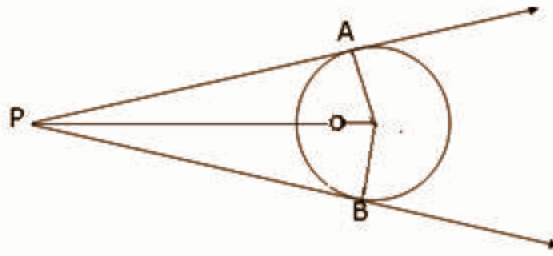
Substitute the value of x and h in (1)

$BC = 6 + 3\sqrt{3}$

$= 11.1\text{m}$

Question 20: Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.

Solution:



Consider a circle with centre O.

Let P be an external point from which two tangents PA and PB are drawn to the circle which are touching the circle at point A and B respectively and AB is the line segment, joining point of contacts A and B together such that it subtends $\angle AOB$ at centre O of the circle.

It can be observed that

$$OA \perp PA$$

$$\therefore \angle OAP = 90^\circ$$

Similarly, $OB \perp PB$

$$\therefore \angle OBP = 90^\circ$$

In quadrilateral OAPB,

Sum of all interior angles = 360°

$$\angle OAP + \angle APB + \angle PBO + \angle BOA = 360^\circ$$

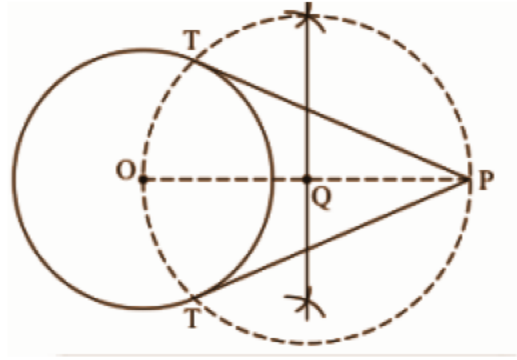
$$\Rightarrow 90^\circ + \angle APB + 90^\circ + \angle BOA = 360^\circ$$

$$\Rightarrow \angle APB + \angle BOA = 180^\circ$$

\therefore The angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.

Question 21: Draw a circle of radius 5 cm. From a point 13 cm away from its centre, construct the pair of tangents to the circle and measure their length. Also, verify the measurement by actual calculation.

Solution:



Steps of construction:

- Draw a circle of radius $OP = 13\text{cm}$.
- Make a point P at a distance of $OP = 13\text{cm}$.
- Join OP.
- Taking Q as centre and radius $OQ = PQ$, draw a circle to intersect the given circle at T and T'.
- Join PT and PT' to obtain the required tangents.
- Thus, PT and P'T' are the required tangents.

Finding the length of tangents.

We know that $OT \perp PT$ and in triangle OPT,

$$PT^2 = OP^2 - OT^2$$

$$= 13^2 - 5^2$$

$$= 169 - 25$$

$$= 144$$

$$= 12$$

The length of the tangents are 12cm each.

Question 22: If an arc of a circle subtends an angle of 60° at the centre and if the area of the minor sector is 231 cm^2 , then find the radius of the circle.

Solution:

$$\text{Area of the sector} = 231\text{cm}^2$$

$$\text{The angle subtended} = 60^\circ$$

$$A = \frac{\pi r^2 \theta}{360^\circ}$$

$$231 = \frac{(22/7) * r^2 * 60^\circ}{360^\circ}$$

$$231 = (22 / 7) r^2 * 0.1666$$

$$231 = 0.5236 r^2$$

$$r^2 = 441$$

$$r = 21\text{cm}$$

Question 23: A well of diameter 7 m is dug and earth from digging is evenly spread out to form a platform 22 m × 14 m × 2.5 m. Find the depth of the well.

Solution:

The diameter of the well = 7 m

The radius of the well = 7 / 2 m

$$L * B * H = \pi r^2 h$$

$$22 * 14 * 2.5 = 22 / 7 * 7 / 2 * 7 / 2 * h$$

$$770 / 38.485 = h$$

$$h = 20\text{cm}$$

Question 24: The following data gives information on the observed lifetimes (in hours) of 200 electrical components.

Lifetime (in hours)	40 - 60	60 - 80	80 - 100	100 - 120	120 - 140	140 - 160
Frequency	25	38	65	24	31	17

Determine the modal lifetimes of the components.

Solution:

As the lifetime (in hours) 80 -100 has a maximum frequency, so it is the modal lifetime in hours.

$$\text{Mode} = l + \frac{fm - f(m-1)}{2fm - f(m-1) - f(m+1)} \times h$$

Class size h = 20

$$l = 80$$

$$f_m = 65$$

$$f_{m-1} = 38$$

$$f_{m+1} = 24$$

$$\begin{aligned} \text{Mode} &= 80 + \{[65 - 38] / [2 * 65 - 38 - 24]\} * 20 \\ &= 80 + \{27 / 68\} * 20 \\ &= 87.94 \end{aligned}$$

Question 25: A box contains 7 red marbles, 10 white marbles and 5 green marbles. One marble is taken out of the box at random. What is the probability that the marble is taken out will be

- (i) not red?
- (ii) white?
- (iii) green?

Solution:

Number of red marbles = 7

Number of white marbles = 10

Number of green marbles = 5

Total marbles = $7 + 10 + 5 = 22$

Probability of getting not red marble = $15 / 22$

Probability of getting white marble = $10 / 22$

Probability of getting green marble = $5 / 22$

PART - D

Question 26: The cost of 7 erasers and 5 pencils is Rs. 58 and the cost of 5 erasers and 6 pencils are Rs. 56. Formulate this problem algebraically and solve it graphically.

Solution:

Let the cost of erasers be x and the cost of pencils be y .

Then,

$$7x + 5y = 58 \text{ ---- (1)}$$

$$5x + 6y = 56 \text{ ---- (2)}$$

Multiply equation (1) by 5

$$7x + 5y = 58 \text{ (6)}$$

$$5x + 6y = 56 \text{ (5)}$$

$$42x + 30y = 348$$

$$25x + 30y = 280$$

Subtract equation (1) of equation (2)

$$42x + 30y = 348$$

$$25x + 30y = 280$$

$$17x = 68$$

$$x = 68 / 17$$

$$x = 4$$

Putting the value of x in equation (1),

$$7 * 4 + 5y = 58$$

$$28 + 5y = 58$$

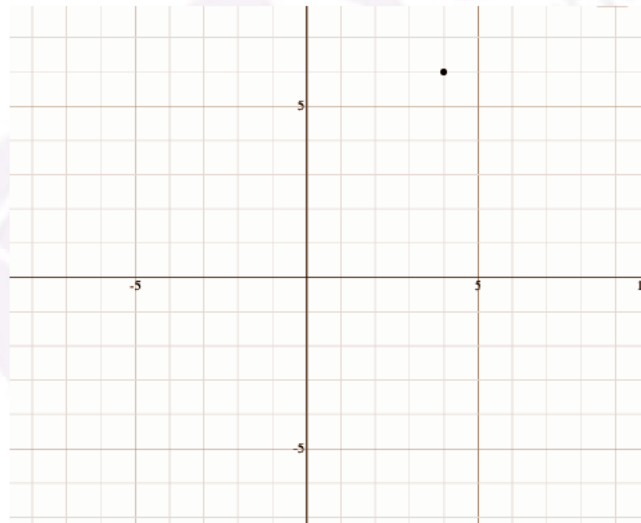
$$5y = 58 - 28$$

$$5y = 30$$

$$y = 30 / 5$$

$$y = 6$$

Hence, one cost of erasers is 4 and one cost of pencils is 6.



Question 27: [i] A train travels 300 km at a uniform speed. If the speed had been 10 km/h more, it would have taken 1 hour less for the same journey. Find the speed of the train.

OR

[ii] The diagonal of a rectangular field is 25 metres more than the shorter side. If the longer side is 23 metres more than the shorter side, find the sides of the field.

Solution:

[i] Let the constant speed of the train be x km / h.

Time is taken by train to cover = $300 / x$ hrs.

Increased speed = 10 km / h

Time taken to cover 300 km when speed is increased = $300 / (x + 10)$ hrs.

According to the question,

$$\Rightarrow 300 / x - 300 / (x + 10) = 1$$

$$\Rightarrow 300(x + 10) - 300x / x(x + 10) = 1$$

$$\Rightarrow 300x + 3000 - 300x / x^2 + 10x = 1$$

$$\Rightarrow x^2 + 10x = 3000$$

$$\Rightarrow x^2 + 10x - 3000 = 0$$

By using the factorization method, we get

$$\Rightarrow x^2 + 60x - 50x - 3000 = 0$$

$$\Rightarrow x(x + 60) - 50(x + 60) = 0$$

$$\Rightarrow (x + 60)(x - 50) = 0$$

$$\Rightarrow x + 60 = 0 \text{ or } x - 50 = 0$$

$$\Rightarrow x = -60, 50 \text{ (As } x \text{ can't be negative)}$$

$$\Rightarrow x = 50 \text{ km/h}$$

Hence, the original speed of the train is 50 km / h.

OR

[ii] Let the shorter side of the rectangular field be ' x ' meters.

Therefore the longer side will be $(x + 23)$ meters and the length of the diagonal will be $(x + 25)$ meters.

The diagonal divides the rectangular into two right-angled triangles and the diagonal is the common side of the two triangles and it is also the longest side of the triangles i.e. the hypotenuse.

By Pythagoras Theorem,

$$(\text{Diagonal})^2 = (\text{Smaller Side})^2 + (\text{Longer Side})^2$$

$$(x + 25)^2 = (x)^2 + (x + 23)^2$$

$$x^2 + 50x + 625 = x^2 + x^2 + 46x + 529$$

$$x^2 + 50x - 46x + 625 - 529 = 2x^2$$

$$x^2 + 4x + 96 = 2x^2$$

$$x^2 - 4x - 96 = 0$$

$$x^2 - 12x + 8x - 96 = 0$$

$$x(x - 12) + 8(x - 12) = 0$$

$$x = 12, -8$$

$x = 12$ m as length cannot be possible.

So the length of the shorter side is 12 meters and the length of the longer side is $12 + 23 = 35$ meters.

Question 28:

[i] Evaluate, $(1 + \tan \theta + \sec \theta) (1 + \cot \theta - \operatorname{cosec} \theta)$.

[ii] Prove that $[\tan A - \sin A] / [\tan A + \sin A] = [\sec A - 1] / [\sec A + 1]$.

Solution:

$$[i] (1 + \tan \theta + \sec \theta) (1 + \cot \theta - \operatorname{cosec} \theta)$$

$$= (1 + [\sin \theta / \cos \theta] + [1 / \cos \theta]) * (1 + [\cos \theta / \sin \theta] - [1 / \sin \theta])$$

$$= \{[\cos \theta + \sin \theta + 1] [\sin \theta + \cos \theta - 1]\} / [\cos \theta * \sin \theta]$$

$$= (\cos \theta + \sin \theta)^2 - 1 / [\cos \theta * \sin \theta]$$

$$= [\cos^2 \theta + \sin^2 \theta + 2 \cos \theta \sin \theta - 1] / \cos \theta \sin \theta$$

$$= [1 - 1 + 2 \sin \theta \cos \theta] / [\cos \theta \sin \theta]$$

$$= 2$$

$$[ii] \text{LHS} = [\tan A - \sin A] / [\tan A + \sin A]$$

$$= [\sin A / \cos A] - \sin A / [\sin A / \cos A] + \sin A$$

$$= \sin A [(1 / \cos A) - 1] / \sin A [(1 / \cos A) + 1]$$

$$= [\sec A - 1] / [\sec A + 1]$$

Question 29: Find the area of that triangle whose vertices are $(-3, -2)$, $(5, -2)$ and $(5, 4)$. Also, prove that it is a right-angle triangle.

Solution:

$$\begin{aligned}
 \text{Area of a triangle} &= [1 / 2] [x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)] \\
 &= [1 / 2] [-3 (-2 - 4) + 5 (4 + 2) + (-2 + 2)] \\
 &= [1 / 2] [18 + 30 + 0] \\
 &= [1 / 2] [48] \\
 &= 24
 \end{aligned}$$

The triangle ABC consists of vertices A (-3, -2), B (5, -2) and C (5, 4).

By distance formula,

$$AC^2 = (-3 - 5)^2 + (-2 - 2)^2$$

$$AC = 8$$

$$AB^2 = (-3 - 5)^2 + (-2 - 4)^2$$

$$AB = 10$$

$$BC^2 = (5 - 5)^2 + (4 + 2)^2$$

$$BC = 6$$

Since, the value of the right-angle triangle is (8, 6, and 10).

It is a right-angle triangle.

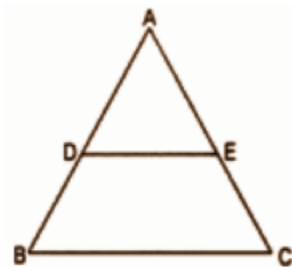
Question 30: [i] Prove that a line drawn through the midpoint of one side of a triangle parallel to the second side bisects the third side.

OR

[ii] PQRS is a trapezium in which PQ || RS and its diagonals intersect each at the point O. Prove that PO / QO = RO / SO.

Solution:

[i]



In $\triangle ABC$, D is the midpoint of AB and E is a point on AC such that $DE \parallel BC$.

Since, $DE \parallel BC$ [given]

Therefore, Using the Basic proportionality theorem,

$$AD / DB = AE / EC \dots(1)$$

But D is the midpoint of AB

Therefore, $AD = DB$

$$\Rightarrow AD / DB = 1 \dots(2)$$

From (1) and (2),

$$1 = AE / EC \Rightarrow EC = AE$$

\Rightarrow E is the midpoint of AC.

Hence, it is proved that a line through the midpoint of one side of a triangle parallel to another side bisects the third side.

OR

[ii] As $PQ \parallel RS$ and PR and QS are transversals,

$$\angle OSR = \angle OQP \text{ [alternate angles]}$$

$$\angle ORS = \angle OPQ \text{ [alternate angles]}$$

$$\triangle SOR \sim \triangle OPQ$$

$$SO / PO = RO / QO = SR / PQ$$

$$SO / PO = RO / QO$$

$$QO / PO = RO / SO$$