

EXERCISE 6.2

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1. Find the square of the following numbers.

i. 32

ii. 35

iii. 86

iv. 93

v. 71

vi. 46

Solution:

i. $(32)^2$

$$= (30 + 2)^2$$

$$= (30)^2 + (2)^2 + 2 \times 30 \times 2 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab \text{]}$$

$$= 900 + 4 + 120$$

$$= 1024$$

ii. $(35)^2$

$$= (30 + 5)^2$$

$$= (30)^2 + (5)^2 + 2 \times 30 \times 5 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab \text{]}$$

$$= 900 + 25 + 300$$

$$= 1225$$

iii. $(86)^2$

$$= (90 - 4)^2$$

$$= (90)^2 + (4)^2 - 2 \times 90 \times 4 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab \text{]}$$

$$= 8100 + 16 - 720$$

$$= 8116 - 720$$

$$= 7396$$

iv. $(93)^2$

$$= (90 + 3)^2$$

$$= (90)^2 + (3)^2 + 2 \times 90 \times 3 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab \text{]}$$

$$= 8100 + 9 + 540$$

$$= 8649$$

v. $(71)^2$

$$\begin{aligned} &= (70+1)^2 \\ &= (70)^2 + (1)^2 + 2 \times 70 \times 1 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab\text{]} \\ &= 4900 + 1 + 140 \\ &= 5041 \\ \text{vi. } &(46)^2 \\ &= (50-4)^2 \\ &= (50)^2 + (4)^2 - 2 \times 50 \times 4 \text{ [Since, } (a+b)^2 = a^2 + b^2 + 2ab\text{]} \\ &= 2500 + 16 - 400 \\ &= 2116 \end{aligned}$$

2. Write a Pythagorean triplet whose one member is.

i. 6

ii. 14

iii. 16

iv. 18

Solution:

For any natural number m , we know that $2m, m^2-1, m^2+1$ is a Pythagorean triplet.

i. $2m = 6$

$$\Rightarrow m = 6/2 = 3$$

$$m^2-1 = 3^2-1 = 9-1 = 8$$

$$m^2+1 = 3^2+1 = 9+1 = 10$$

$\therefore (6, 8, 10)$ is a Pythagorean triplet.

ii. $2m = 14$

$$\Rightarrow m = 14/2 = 7$$

$$m^2-1 = 7^2-1 = 49-1 = 48$$

$$m^2+1 = 7^2+1 = 49+1 = 50$$

$\therefore (14, 48, 50)$ is not a Pythagorean triplet.

iii. $2m = 16$

$$\Rightarrow m = 16/2 = 8$$

$$m^2-1 = 8^2-1 = 64-1 = 63$$

$$m^2+1 = 8^2+1 = 64+1 = 65$$

$\therefore (16, 63, 65)$ is a Pythagorean triplet.

iv. $2m = 18$

$$\Rightarrow m = 18/2 = 9$$

$$m^2 - 1 = 9^2 - 1 = 81 - 1 = 80$$

$$m^2 + 1 = 9^2 + 1 = 81 + 1 = 82$$

$\therefore (18, 80, 82)$ is a Pythagorean triplet.