12/04/2023
Morning

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# Memory Based Answers \& Solutions 

Time : 3 hrs.

## JEE (Main)-2023 (Online) Phase-2

(Physics, Chemistry and Mathematics)

## IMPORTANT INSTRUCTIONS:

(1) The test is of $\mathbf{3}$ hours duration.
(2) The Test Booklet consists of 90 questions. The maximum marks are 300 .
(3) There are three parts in the question paper consisting of Physics, Chemistry and Mathematics having 30 questions in each part of equal weightage. Each part (subject) has two sections.
(i) Section-A: This section contains 20 multiple choice questions which have only one correct answer. Each question carries $\mathbf{4}$ marks for correct answer and -1 mark for wrong answer.
(ii) Section-B: This section contains 10 questions. In Section-B, attempt any five questions out of 10. The answer to each of the questions is a numerical value. Each question carries 4 marks for correct answer and $\mathbf{- 1}$ mark for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

## PHYSICS

## SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

## Choose the correct answer:

1. If a planet has mass equal to 16 times the mass of earth, and radius equal to 4 times that of earth. The ratio of escape speed of planet to that of earth is
(1) $2: 1$
(2) $1: 2$
(3) $\sqrt{2}: 1$
(4) $4: 1$

Answer (1)
Sol. $\frac{V_{P}}{V_{e}}=\sqrt{\frac{2 G M_{P}}{R_{P}}} \times \sqrt{\frac{R_{e}}{2 G M_{e}}}$
$=\sqrt{\frac{16}{4}}=2$
2. Find ratio of de-Broglie wavelength of a proton and an $\alpha$-particle, when accelerated through a potential difference of 2 V and 4 V respectively.
(1) $4: 1$
(2) $2: 1$
(3) $1: 8$
(4) $16: 1$

## Answer (1)

Sol. $\frac{\lambda_{p}}{\lambda_{\alpha}}=\frac{\sqrt{2 q_{\alpha} V_{\alpha} m_{\alpha}}}{\sqrt{2 q_{p} V_{p} m_{p}}}=\sqrt{\frac{2 \times 4 \times 4}{1 \times 2 \times 1}}=\frac{4}{1}$
3. If a body of mass 5 kg is in equilibrium due to forces $F_{1}, F_{2}$ and $F_{3} . F_{2}$ and $F_{3}$ are perpendicular to each other. If $F_{1}$ is removed then find the acceleration of body. Given : $F_{2}=6 \mathrm{~N}$ and $F_{3}=8 \mathrm{~N}$
(1) $2 \mathrm{~m} / \mathrm{s}^{2}$
(2) $3 \mathrm{~m} / \mathrm{s}^{2}$
(3) $4 \mathrm{~m} / \mathrm{s}^{2}$
(4) $5 \mathrm{~m} / \mathrm{s}^{2}$

Answer (1)
Sol. $F_{\text {net }}=\sqrt{6^{2}+8^{2}}=10 \mathrm{~N}$
$a=\frac{10}{5}=2 \mathrm{~m} / \mathrm{s}^{2}$
4. If an object cools down from $80^{\circ} \mathrm{C}$ to $60^{\circ} \mathrm{C}$ in 5 minutes in a surrounding of temperature $20^{\circ} \mathrm{C}$. The time taken to cool from $60^{\circ} \mathrm{C}$ to $40^{\circ} \mathrm{C}$ will be (assume Newton's law of cooling to be valid)
(1) $\frac{25}{3}$ minutes
(2) 5 minutes
(3) $\frac{25}{4}$ minutes
(4) 9 minutes

Answer (1)

Sol. $\frac{20}{5}=K(70-20)$
also $\frac{20}{t}=K(50-20)$
from (1) and (2)
$t=\frac{25}{3}$ minutes
5. Ratio between rms speed of Ar to the most probable speed of $\mathrm{O}_{2}$ at $27^{\circ} \mathrm{C}$ is
(1) $\sqrt{\frac{8}{\pi}}$
(2) $\sqrt{\frac{8}{3}}$
(3) $\sqrt{\frac{4}{\pi}}$
(4) $\sqrt{\frac{4}{3}}$

## Answer (2)

Sol. $v_{\text {rms Ar }}=\sqrt{\frac{3 R T}{M}}=\sqrt{\frac{3 R T}{40}}$
$v_{\text {mp } o_{2}}=\sqrt{\frac{2 R T}{M}}=\sqrt{\frac{2 R T}{32}}$
$\frac{v_{\mathrm{rms}}}{v_{\mathrm{mp}} o_{2}}=\sqrt{\frac{3}{40} \times \frac{32}{2}}=\sqrt{\frac{6}{5}}$
6. A dipole having dipole moment $\vec{M}$ is placed in two magnetic field of strength $B_{1}$ and $B_{2}$ respectively. If dipole oscillates 60 time in 20 seconds in $B_{1}$ magnetic field and 60 oscillations in 30 seconds in $B_{2}$ magnetic field. Then find the $\left(\frac{B_{1}}{B_{2}}\right)$.
(1) $\frac{3}{2}$
(2) $\frac{2}{3}$
(3) $\frac{4}{9}$
(4) $\frac{9}{4}$

Answer (4)
Sol. $\tau=\vec{M} \times \vec{B}$
$l \alpha=-M B \theta$
$\alpha=-\left(\frac{M B}{I}\right) \theta$
$T=2 \pi \sqrt{\frac{1}{M B}}$
$\frac{T_{1}}{T_{2}}=\sqrt{\frac{B_{2}}{B_{1}}}$
$\Rightarrow \quad \frac{20}{30}=\sqrt{\frac{B_{2}}{B_{1}}}$
$\Rightarrow \quad \frac{B_{1}}{B_{2}}=\frac{9}{4}$
7. Mass of body $=500 \mathrm{~kg}, \mu=0.7$. Find work required to move a distance of 4 Km if the body moves with velocity $10 \mathrm{~m} / \mathrm{s}$.
(1) $3.5 \times 10^{6} \mathrm{~J}$
(2) $28 \times 10^{6} \mathrm{~J}$
(3) $7 \times 10^{6} \mathrm{~J}$
(4) $14 \times 10^{6} \mathrm{~J}$

## Answer (4)

Sol. Since $v=$ const. $\Rightarrow F=\mu m g=0.7 \times 500 \times 10$
$=3500 \mathrm{~N}$
$W=F S=3.5 \times 10^{3} \times 4 \times 10^{3}=14 \times 10^{6} \mathrm{~J}$
8. Suppose a situation in which two planet orbits around the sun in same orbit. If the mass of planet 1 is twice the mass of planet 2 , then what do they have same?
(1) Potential energy
(2) Kinetic energy
(3) Total energy
(4) Velocity

Answer (4)
Sol. $v=\sqrt{\frac{G M}{r}} ; M=$ mass of sun
P.E. $=-\frac{G M m}{r} \quad m$, different so different P.E.
K.E. $=\frac{1}{2} m v^{2} \quad m$, different so different K.E.
T.E. will be different.
9. In a ice cube of thickness 24 cm , has bubble trapped in it as shown in figure. If apparent side are 12 cm and 4 cm from side (1) and side (2) respectively then refractive index of ice cube is

(1) $\frac{4}{3}$
(2) $\frac{3}{2}$
(3) 2
(4) 2.4

Answer (2)
Sol. $\frac{I}{\mu}=12+4=16 \mathrm{~cm}$
$\frac{24}{16}=\mu$
$\Rightarrow \mu=\frac{3}{2}$
10. Statement (1): A truck and a car moving with equal kinetic energy are stopped by equal retarding force. Both will cover equal distance to stop.

Statement (2): A car moving towards east suddenly changes its direction towards north with same speed. Its acceleration is zero.
(1) Both (1) and (2) are true
(2) Both (1) and (2) are false
(3) (1) is true, (2) is false
(4) (1) is false, (2) is true

## Answer (3)

Sol. For (1) $v \propto \frac{1}{\sqrt{m}}, a \propto \frac{1}{m}$
$\because s=\frac{v^{2}}{2 a} \rightarrow$ independent of mass
For (2) direction is changed, $\therefore a \neq 0$
11. Match the physical quantity in column-I with the respective dimension in column-II and choose the correct option

|  | Column-I |  | Column-II |
| :--- | :--- | :--- | :--- |
| I. | Spring constant | (P) | $\left[\mathrm{ML}^{2} \mathrm{~T}^{0}\right]$ |
| II. | Moment of inertia | (Q) | $\left[\mathrm{M}^{0} \mathrm{~L}^{0} \mathrm{~T}^{-1}\right]$ |
| III. | Angular momentum | (R) | $\left[\mathrm{ML}^{0} \mathrm{~T}^{-2}\right]$ |
| IV. | Angular speed | (S) | $\left[\mathrm{ML}^{2} \mathrm{~T}^{-1}\right]$ |

(1) $\mathrm{I}(\mathrm{P}), \mathrm{II}(\mathrm{Q}), \mathrm{III}(\mathrm{R}), \mathrm{IV}(\mathrm{S})$
(2) $I(R), I I(P), I I I(Q), I V(S)$
(3) $I(R), I I(S), I I(Q), I V(P)$
(4) $I(R), I I(P), I I I(S), I V(Q)$

## Answer (4)

Sol. Theoretical
12. The length of a conductor having resistance $160 \Omega$, is compressed to $25 \%$ of its initial value. The new resistance will be
(1) $10 \Omega$
(2) $20 \Omega$
(3) $15 \Omega$
(4) $17 \Omega$

## Answer (1)

Sol. At constant volume, $R \propto \ell^{2}$

$$
\begin{array}{r}
\therefore \quad \frac{160}{R^{\prime}}=\frac{l^{2}}{\frac{l^{2}}{16}} \\
\\
R^{\prime}=10 \Omega
\end{array}
$$

13. Statement I : In LCR circuit, by increasing frequency current increases first then decreases Statement II : Power factor of LCR circuit is one. Choose the correct option
(1) Statement I is correct and statement II is incorrect
(2) Statement I is incorrect and statement I is correct
(3) Both Statement I and statement II are correct
(4) Both Statement I and statement II are incorrect

## Answer (1)

Sol. $I=\frac{V}{Z}$
As $\omega$ increases, $Z$ decreases first then increases

$$
\cos \phi=\left(\frac{R}{Z}\right)
$$

14. Assertion (A): An electrical dipole is enclosed in a closed gaussian surface. The total flux through the enclosed surface is zero.
Reason (R): Net charge inside the enclosed surface is zero.
(1) Both (A) and (R) are correct and (R) is correct explanation of $(A)$
(2) Both (A) and (R) are correct and (R) is not the correct explanation of $(A)$
(3) (A) is true, but (R) is false
(4) (A) and (R) both are false

Answer (1)
Sol. $\phi=\frac{q_{\text {in }}}{\epsilon_{0}}$ and $q_{\text {in }}=0$ inside surface
15. A circular ring is placed in magnetic field of 0.4 T . Suddenly its radius starts shrinking at the rate of $1 \mathrm{~mm} / \mathrm{s}$. Find the induced emf in the ring at $r=2 \mathrm{~cm}$.
(1) $16 \pi \mu \mathrm{~V}$
(2) $8 \pi \mu \mathrm{~V}$
(3) $16 \pi \mathrm{mV}$
(4) $8 \pi \mathrm{mV}$

## Answer (1)

Sol. $\phi=B A$
$\varepsilon=\frac{d \phi}{d t}=\frac{B d A}{d t}=\frac{2 \pi r B d r}{d t}$
at $r=2 \mathrm{~cm}$
$\varepsilon_{\text {induced }}=\frac{2 \pi \times 2}{100} \times 0.4 \times \frac{.1}{1000}$
$=\frac{16 \pi}{10^{6}}=16 \pi \times 10^{-6} \mathrm{~V}$
16. A body is doing SHM with amplitude $A$. When it is at $x=+\frac{A}{2}$, find ratio of kinetic energy to potential energy
(1) $1: 1$
(2) $3: 1$
(3) $2: 1$
(4) $4: 1$

## Answer (2)

Sol. $\frac{K}{U}=\frac{\frac{1}{2} m \omega^{2}\left(A^{2}-x^{2}\right)}{\frac{1}{2} m \omega^{2} x^{2}}$
$=\frac{A^{2}-x^{2}}{x^{2}}=\frac{\frac{3 A^{2}}{4}}{\frac{A^{2}}{4}}=\frac{3}{1}$
17. Current flowing in a conductor at $0^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$ is 2 A and 1.2 A respectively. The current at $80^{\circ} \mathrm{C}$ is
(1) 1.3 A
(2) 1.5 A
(3) 1.6 A
(4) 1.8 A

Answer (1)
Sol. $\because \quad R \propto \frac{1}{i}$
Let $R=\frac{x}{i}$
also $\frac{\frac{x}{1.2}-\frac{x}{2}}{100-0}=\frac{\frac{x}{i}-\frac{x}{2}}{80-0}$
$i=\frac{30}{23} \approx 1.3 \mathrm{~A}$
18. Which of the following is more energetic between Infrared wave and microwave?
(1) IR wave
(2) Microwaves
(3) Both are same energetic
(4) Cannot predict

## Answer (1)

Sol. $\because \quad f_{\mathrm{R}}>f_{\text {micro }}$
$\therefore \quad E_{\mathrm{IR}}>E_{\text {micro }}$
IR waves are more energetic.
19. If carnot engines works between freezing point and boiling point of water then the efficiency of carnot engine is
(1) $35 \%$
(2) $27 \%$
(3) $22 \%$
(4) $17 \%$

Answer (2)
Sol. $\eta=1-\frac{T_{L}}{T_{H}}=1-\left(\frac{273}{373}\right)=\left(\frac{100}{373}\right) \approx 0.27$
20. In closed organ pipe, the resonance consecutive frequencies are in ratio $1: 3: 5 \ldots$ and $5^{\text {th }}$ harmonic frequency is 405 Hz . Velocity of sound $=345 \mathrm{~m} / \mathrm{s}$. Find length of organ pipe.
(1) $\frac{108}{115} \mathrm{~m}$
(2) $\frac{81}{115} \mathrm{~m}$
(3) $\frac{115}{108} \mathrm{~m}$
(4) $\frac{115}{81} \mathrm{~m}$

## Answer (3)

Sol. For $5^{\text {th }}$ harmonic, $f=5 f_{0}=405$

$$
\begin{aligned}
& \text { or } 5 \frac{v}{\lambda}=405 \Rightarrow 5\left(\frac{345}{4 l}\right)=405 \\
& \Rightarrow \quad I=\frac{5 \times 345}{4 \times 405}
\end{aligned}
$$

## SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a NUMERICAL VALUE. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, $-00.33,-00.30,30.27,-27.30$ ) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
21. A particle is thrown vertically upward with initial velocity of $150 \mathrm{~m} / \mathrm{s}$. Find the ratio of its speed at $t=3$ seconds and $t=5$ seconds. (take $g=10 \mathrm{~m} / \mathrm{s}^{2}$ )

## Answer (01.20)

Sol. $\frac{v_{3}}{v_{5}}=\left(\frac{u-g \times 3}{u-g \times 5}\right)=\left(\frac{150-30}{150-50}\right)=\frac{120}{100}=1.2$
22. 64 identical balls made of conducting material each having potential of 10 mV are joined to form a bigger ball. The potential of bigger ball is $\qquad$ V.

## Answer (00.16)

Sol. $64\left(\frac{4}{3} \pi r^{3}\right)=\frac{4}{3}=\pi R^{3} \Rightarrow R=4 r$
Also $Q^{\prime}=64 Q$
$\because \frac{K Q}{r}=10 \mathrm{mV}$ then $V^{\prime}=\frac{K(64 Q)}{4 r}=16 \times 10 \mathrm{mV}$
$=160 \mathrm{mV}$
23. An object placed at very large distance from lens $L$. The distance of final image formed from $L_{1}$ will be
$\qquad$ m.


Answer (01.00)
Sol. Is image is formed at focus of $L_{1}$ which is at $2 f_{2}$ from lens $L_{2}$.
24. A photon of energy 12.75 eV falls a H -atom. Find out no. of spectral lines observed?

## Answer (6)

Sol. $\because \Delta E=13.6\left[1-\frac{1}{n^{2}}\right] \mathrm{eV}$
For $n=4, \Delta E=12.75 \mathrm{eV}$
In 4 energy level,

no. of spectral lines $={ }^{4} \mathrm{C}_{2}=6$
25. A uniform solid sphere is rolling without slipping on a horizontal surface. The ratio of translational kinetic energy to the total kinetic energy is $5 / x$. Find the value of $x$.

## Answer (7)

Sol. $\frac{\mathrm{K} \cdot \mathrm{E}_{\text {Trans. }}}{\mathrm{K} \cdot \mathrm{E}_{\text {Total }}}=\frac{\frac{1}{2} m R^{2} \omega^{2}}{\frac{1}{2}\left(\frac{2}{5}+1\right) m R^{2} \omega^{2}}=\frac{5}{7}$
26.
27.
28.
29.
30.

