

11/04/2023

Evening



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Answers & Solutions

Time : 3 hrs.

for

M.M. : 300

JEE (Main)-2023 (Online) Phase-2

(Mathematics, Physics and Chemistry)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are **three** parts in the question paper consisting of **Mathematics, Physics** and **Chemistry** having 30 questions in each part of equal weightage. Each part (subject) has two sections.
 - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
 - (ii) **Section-B:** This section contains 10 questions. In Section-B, attempt any **five questions out of 10**. The answer to each of the questions is a numerical value. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. The domain of the function

$$f(x) = \frac{1}{\sqrt{[x]^2 - 3[x] - 10}}$$
 is (where $[x]$ denotes the

greatest integer less than or equal to x)

- (1) $(-\infty, -3] \cup (5, \infty)$ (2) $(-\infty, -2) \cup [6, \infty)$
(3) $(-\infty, -2) \cup (5, \infty)$ (4) $(-\infty, -3] \cup [6, \infty)$

Answer (2)

Sol. $f(x) = \frac{1}{\sqrt{[x]^2 - 3[x] - 10}}$

For Domain $[x]^2 - 3[x] - 10 > 0$

$$\Rightarrow ([x] - 5)([x] + 2) > 0$$

$$\Rightarrow [x] \in (-\infty, -2) \cup (5, \infty)$$

$$\therefore x \in (-\infty, -2) \cup [6, \infty)$$

2. If the system of linear equations

$$7x + 11y + \alpha z = 13$$

$$5x + 4y + 7z = \beta$$

$$175x + 194y + 57z = 361$$

has infinitely many solutions, then $\alpha + \beta + 2$ is equal to

- (1) 4 (2) 3
(3) 5 (4) 6

Answer (1)

Sol. $7x + 11y + \alpha z = 13$

$$5x + 4y + 7z = \beta$$

$$175x + 194y + 57z = 361$$

For infinite solution, $\begin{vmatrix} 7 & 11 & \alpha \\ 5 & 4 & 7 \\ 175 & 194 & 57 \end{vmatrix} = 0$

$$\Rightarrow \begin{vmatrix} 7 & 11 & \alpha \\ 5 & 4 & 7 \\ 0 & -81 & 57 - 25\alpha \end{vmatrix} = 0$$

$$\Rightarrow 81(49 - 5\alpha) + (57 - 25\alpha)(-27) = 0$$

$$\Rightarrow 270\alpha = -2430 \Rightarrow \boxed{\alpha = -9}$$

$$\text{and } \Delta_1 = 0$$

$$\begin{vmatrix} 13 & 11 & -9 \\ \beta & 4 & 7 \\ 361 & 194 & 57 \end{vmatrix} = 0$$

$$\Rightarrow \boxed{\beta = 11}$$

$$\therefore \alpha + \beta + 2 = 4$$

3. Let $A = \{1, 3, 4, 6, 9\}$ and $B = \{2, 4, 5, 8, 10\}$. Let R be a relation defined on $A \times B$ such that $R = \{((a_1, b_1), (a_2, b_2)) : a_1 \leq b_2 \text{ and } b_1 \leq a_2\}$. Then the number of elements in the set R is

- (1) 160 (2) 52
(3) 26 (4) 180

Answer (1)

Sol. $A = \{1, 3, 4, 6, 9\}$ $B = \{2, 4, 5, 8, 10\}$

$$R = \{((a_1, b_1), (a_2, b_2)) : a_1 \leq b_2 \text{ and } b_1 \leq a_2\}$$

For

Similarly for (b_1, a_2) we will have

$$a_1 = 1 \quad b_2 \rightarrow 5 \quad b_1 \rightarrow 2 \quad a_2 = 4$$

$$a_1 = 3 \quad b_2 \rightarrow 4 \quad b_1 \rightarrow 4 \quad a_2 = 3$$

$$a_1 = 4 \quad b_2 \rightarrow 4 \quad b_1 \rightarrow 5 \quad a_2 = 2$$

$$a_1 = 6 \quad b_2 \rightarrow 2 \quad b_1 \rightarrow 8 \quad a_2 = 1$$

$$a_1 = 9 \quad b_2 \rightarrow 1 \quad b_1 \rightarrow 10 \quad a_2 = 0$$

16 cases

10 cases

$$\therefore \text{Total elements in relation} = 16 \times 10 = 160$$

4. Let the mean of 6 observations 1, 2, 4, 5, x and y be 5 and their variance be 10. Then their mean deviation about the mean is equal to

- (1) $\frac{7}{3}$ (2) 3
(3) $\frac{8}{3}$ (4) $\frac{10}{3}$

Answer (3)

Sol. $12 + x + y = 30$

$$\Rightarrow x + y = 18$$

$$\text{and } \frac{x^2 + y^2 + 46}{6} - 25 = 10$$

$$\therefore x = 10, y = 8$$

Now, mean deviation about mean

$$= \frac{4+3+1+0+5+3}{6} = \frac{8}{3}$$

5. If four distinct points with position vectors \vec{a} , \vec{b} , \vec{c} and \vec{d} are coplanar, then $[\vec{a} \vec{b} \vec{c}]$ is equal to

$$(1) [\vec{d} \vec{b} \vec{a}] + [\vec{a} \vec{c} \vec{d}] + [\vec{d} \vec{b} \vec{c}]$$

$$(2) [\vec{a} \vec{d} \vec{b}] + [\vec{d} \vec{c} \vec{a}] + [\vec{d} \vec{b} \vec{c}]$$

$$(3) [\vec{d} \vec{c} \vec{a}] + [\vec{b} \vec{d} \vec{a}] + [\vec{c} \vec{d} \vec{b}]$$

$$(4) [\vec{b} \vec{c} \vec{d}] + [\vec{d} \vec{a} \vec{c}] + [\vec{d} \vec{b} \vec{a}]$$

Answer (3)

Sol. $[\vec{b} - \vec{a} \vec{c} - \vec{a} \vec{d} - \vec{a}] = 0$

$$(\vec{b} - \vec{a}) \cdot [(\vec{c} - \vec{a}) \times (\vec{d} - \vec{a})] = 0$$

$$(\vec{b} - \vec{a}) \cdot (\vec{c} \times \vec{d} - \vec{c} \times \vec{a} - \vec{a} \times \vec{d}) = 0$$

$$[\vec{b} \vec{c} \vec{d}] - [\vec{b} \vec{c} \vec{a}] - [\vec{b} \vec{a} \vec{d}] - [\vec{a} \vec{c} \vec{d}] = 0$$

$$\therefore [\vec{a} \vec{b} \vec{c}] = [\vec{b} \vec{c} \vec{d}] + [\vec{a} \vec{b} \vec{d}] + [\vec{a} \vec{d} \vec{c}]$$

$$= [\vec{d} \vec{c} \vec{a}] + [\vec{b} \vec{d} \vec{a}] + [\vec{c} \vec{d} \vec{b}]$$

6. Let $y = y(x)$ be the solution of the differential equation

$$\frac{dy}{dx} + \frac{5}{x(x^5 + 1)} y = \frac{(x^5 + 1)^2}{x^7}, x > 0. \text{ If } y(1) = 2, \text{ then}$$

$y(2)$ is equal to

$$(1) \frac{637}{128} \quad (2) \frac{679}{128}$$

$$(3) \frac{693}{128} \quad (4) \frac{697}{128}$$

Answer (3)

Sol. I.F. = $e^{\int \frac{5}{x(1+x^5)} dx}$

$$= e^{\int \frac{5}{x^6 \left(\frac{1}{x^5} + 1 \right)} dx}$$

$$\text{Put } \frac{1}{x^5} + 1 = t$$

$$\frac{-5}{x^6} dx = dt$$

$$e^{\int -\frac{dt}{t}} = e^{-\ln t} = \frac{1}{t} = \frac{x^5}{1+x^5}$$

$$y \left(\frac{x^5}{1+x^5} \right) = \int \frac{x^5}{1+x^5} \cdot \frac{(1+x^5)^2}{x^7} dx + c$$

$$y \left(\frac{x^5}{1+x^5} \right) = \frac{-1}{x} + \frac{x^4}{4} + c$$

$$\text{Now } y(1) = 2, \text{ then } c = \frac{7}{4}$$

$$\therefore y(2) = \frac{693}{128}$$

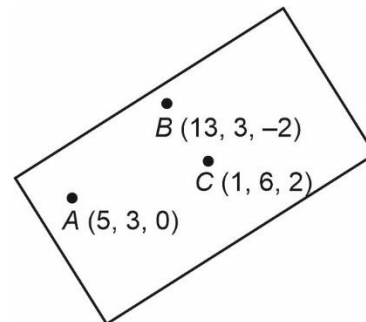
7. Let P be the plane passing through the points $(5, 3, 0)$, $(13, 3, -2)$ and $(1, 6, 2)$. For $\alpha \in \mathbb{N}$, if the distances of the points $A(3, 4, \alpha)$ and $B(2, \alpha, a)$ from the plane P are 2 and 3 respectively, then the positive value of a is

$$(1) 6 \quad (2) 3$$

$$(3) 5 \quad (4) 4$$

Answer (4)

Sol.



$$\vec{AB} = 8\hat{i} - 2\hat{k}$$

$$\vec{AC} = -4\hat{i} + 3\hat{j} + 2\hat{k}$$

$$\vec{AB} \times \vec{AC} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 8 & 0 & -2 \\ -4 & 3 & 2 \end{vmatrix}$$

$$= 6\hat{i} - 8\hat{j} + 24\hat{k}$$

Equation of plane : $6x - 8y + 24z = d$ passes through $(5, 3, 0)$

$$6 \times 5 - 8 \times 3 + 24 \times 0 = d$$

$$d = 6$$

$$6x - 8y + 24z = 6 \Rightarrow 3x - 4y + 12z = 3$$

Distance of point $(3, 4, \alpha)$

$$\frac{9 - 16 + 12\alpha - 3}{\sqrt{9 + 16 + 144}} = 2 \Rightarrow \alpha = 3$$

Distance of point $(2, \alpha, a)$

$$\frac{3 \times 2 - 4 \times 3 + 12 \times a - 3}{13} = 3$$

$$12a - 9 = 39$$

$$12a = 48$$

$$a = 4$$

8. The converse of $((\sim p) \wedge q) \Rightarrow r$ is

$$(1) ((\sim p) \vee q) \Rightarrow r \quad (2) (\sim r) \Rightarrow p \wedge q$$

$$(3) (\sim r) \Rightarrow ((\sim p) \wedge q) \quad (4) (p \vee (\sim q)) \Rightarrow (\sim r)$$

Answer (4)

Sol. Converse of $(\sim p \wedge q) \Rightarrow r$ is

$$r \Rightarrow (\sim p \wedge q)$$

$$(p \vee (\sim q)) \Rightarrow (\sim r)$$

9. Let the function $f : [0, 2] \rightarrow \mathbb{R}$ be defined as

$$f(x) = \begin{cases} e^{\min\{x^2, x - [x]\}}, & x \in [0, 1) \\ e^{\lceil x - \log_e x \rceil}, & x \in [1, 2] \end{cases}$$

where $[t]$ denotes the greatest integer less than or

equal to t . Then the value of the integral $\int_0^2 xf(x) dx$

is

$$(1) 1 + \frac{3e}{2} \quad (2) (e - 1) \left(e^2 + \frac{1}{2} \right)$$

$$(3) 2e - 1 \quad (4) 2e - \frac{1}{2}$$

Answer (4)

$$\text{Sol. } f(x) = \begin{cases} e^{\min\{x^2, x\}} & x \in [0, 1) \\ e & x \in [1, 2] \end{cases}$$

$$= \begin{cases} e^{x^2} & x \in [0, 1) \\ e & x \in [1, 2] \end{cases}$$

$$\because x - \ln x \in [1, 2] \text{ for } x \in [1, 2]$$

$$\therefore [x - \ln x] = 1$$

$$\int_0^2 xf(x) dx = \int_0^1 x \cdot e^{x^2} dx + \int_1^2 x \cdot e dx$$

$$x^2 = t \Rightarrow 2x dx = dt$$

$$= \frac{1}{2} \int_0^1 e^t dt + e \left[\frac{x^2}{2} \right]_1^2$$

$$\Rightarrow \left(\frac{e-1}{2} \right) + \frac{3e}{2} \Rightarrow 2e - \frac{1}{2}$$

Option (4) is correct.

10. If $f : \mathbb{R} \rightarrow \mathbb{R}$ be a continuous function satisfying

$$\int_0^{\frac{\pi}{2}} f(\sin 2x) \sin x dx + \alpha \int_0^{\frac{\pi}{4}} f(\cos 2x) \cos x dx = 0, \text{ then}$$

the value of α is

$$(1) \sqrt{2} \quad (2) -\sqrt{3}$$

$$(3) \sqrt{3} \quad (4) -\sqrt{2}$$

Answer (4)

$$\text{Sol. } \int_0^{\frac{\pi}{2}} f(\sin 2x) \sin x dx + \alpha \int_0^{\frac{\pi}{4}} f(\cos 2x) \cos x dx = 0$$

$$\text{Let } I = \int_0^{\frac{\pi}{2}} f(\sin 2x) \sin x dx$$

$$= \int_0^{\frac{\pi}{4}} f(\sin 2x) \sin x dx + \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} f(\sin 2x) \sin x dx$$

$$= \int_0^{\frac{\pi}{4}} f(\cos 2x) \sin \left(\frac{\pi}{4} - x \right) dx$$

$$+ \int_0^{\frac{\pi}{4}} f \left(\sin 2 \left(\frac{\pi}{4} + x \right) \right) \sin \left(\frac{\pi}{4} + x \right) dx$$

$$= \int_0^{\frac{\pi}{4}} f(\cos 2x) \left(\frac{1}{\sqrt{2}} \cos x - \frac{1}{\sqrt{2}} \sin x \right) dx$$

$$+ \int_0^{\frac{\pi}{4}} f(\cos 2x) \left(\frac{1}{\sqrt{2}} \cos x + \frac{1}{\sqrt{2}} \sin x \right) dx$$

$$= \int_0^{\frac{\pi}{4}} f(\cos 2x) (\sqrt{2} \cos x) dx$$

$$\therefore \alpha = -\sqrt{2}$$

Option (4) is correct.

11. If the radius of the largest circle with centre (2, 0) inscribed in the ellipse $x^2 + 4y^2 = 36$ is r , then $12r^2$ is equal to

- (1) 115 (2) 92
(3) 69 (4) 72

Answer (2)

Sol. Equation of normal at $P(6\cos\theta, 3\sin\theta)$ is

$$6\sec\theta x - 3\operatorname{cosec}\theta y = 27$$

If passes through (2, 0)

$$\therefore 12\sec\theta = 27$$

$$\therefore \cos\theta = \frac{4}{9}, \sin\theta = \frac{\sqrt{65}}{9}$$

$$P\left(\frac{8}{3}, \frac{\sqrt{65}}{3}\right)$$

$$r = OP \quad (O = (2, 0))$$

$$= \sqrt{\left(\frac{8}{3} - 2\right)^2 + \left(\frac{\sqrt{65}}{3}\right)^2}$$

$$= \frac{\sqrt{69}}{3}$$

$$\therefore 12r^2 = 12 \times \frac{69}{9} = 92$$

\therefore Option (2) is correct.

12. Let the line passing through the points $P(2, -1, 2)$ and $Q(5, 3, 4)$ meet the plane $x - y + z = 4$ at the point R . Then the distance of the point R from the plane $x + 2y + 3z + 2 = 0$ measured parallel to the

$$\text{line } \frac{x-7}{2} = \frac{y+3}{2} = \frac{z-2}{1} \text{ is}$$

- (1) $\sqrt{61}$ (2) $\sqrt{189}$
(3) $\sqrt{31}$ (4) 3

Answer (4)

Sol. Equation of line PQ .

$$\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{2} = \lambda$$

Let R be $(3\lambda + 2, 4\lambda - 1, 2\lambda + 2)$

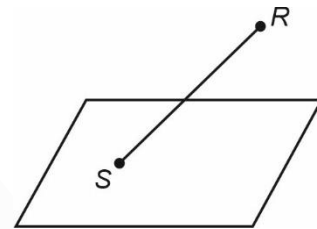
R lies on plane $x - y + z = 4$

$$\therefore 3\lambda + 2 - 4\lambda + 1 + 2\lambda + 2 = 4$$

$$\Rightarrow \lambda = -1$$

$$\therefore R(-1, -5, 0)$$

$$\text{Let } SR \text{ be : } \frac{x+1}{2} = \frac{y+5}{2} = \frac{z}{1} = k$$



$$S: (2k - 1, 2k - 5, k)$$

S lies on plane : $x + 2y + 3z + 2 = 0$

$$\Rightarrow (2k - 1) + (4k - 10) + 3k + 2 = 0$$

$$\Rightarrow 9k - 9 = 0 \Rightarrow k = 1$$

$$S(1, -3, 1) \quad \therefore SR = \sqrt{4 + 4 + 1} = 3$$

\therefore Option (4) is correct.

$$13. \text{ If } \begin{vmatrix} x+1 & x & x \\ x & x+\lambda & x \\ x & x & x+\lambda^2 \end{vmatrix} = \frac{9}{8}(103x+81), \text{ then } \lambda, \frac{\lambda}{3}$$

are the roots of the equation

$$(1) 4x^2 + 24x - 27 = 0 \quad (2) 4x^2 - 24x - 27 = 0$$

$$(3) 4x^2 + 24x + 27 = 0 \quad (4) 4x^2 - 24x + 27 = 0$$

Answer (4)

$$\text{Sol. } \begin{vmatrix} x+1 & x & x \\ x & x+\lambda & x \\ x & x & x+\lambda^2 \end{vmatrix} = \frac{9}{8}(103x+81)$$

Put $x = 0$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & \lambda & 0 \\ 0 & 0 & \lambda^2 \end{vmatrix} = \frac{9}{8} \times 81$$

$$\lambda^3 = \frac{3^6}{2^3}$$

$$\lambda = \frac{9}{2}$$

$$\frac{\lambda}{3} = \frac{3}{2}$$

$$\text{Equation : } x^2 - \left(\frac{9}{2} + \frac{3}{2}\right)x + \frac{9}{2} \times \frac{3}{2} = 0$$

$$4x^2 - 24x + 27 = 0$$

14. If the letters of the word MATHS are permuted and all possible words so formed are arranged as in a dictionary with serial numbers, then the serial number of the word THAMS is

- (1) 103 (2) 102
(3) 101 (4) 104

Answer (1)

Sol.
$$\begin{array}{ccccc} 5 & 2 & 1 & 3 & 4 \\ T & H & A & M & S \\ 4! & 3! & 2! & 1! & 0! \end{array}$$

$$\begin{aligned} \text{Rank} &= 4 \times 4! + 1 \times 3! + 1 \\ &= 96 + 6 + 1 \\ &= 103 \end{aligned}$$

15. Let f and g be two functions defined by

$$f(x) = \begin{cases} x+1, & x < 0 \\ |x-1|, & x \geq 0 \end{cases} \text{ and } g(x) = \begin{cases} x+1, & x < 0 \\ 1, & x \geq 0 \end{cases}$$

Then $(g \circ f)(x)$ is

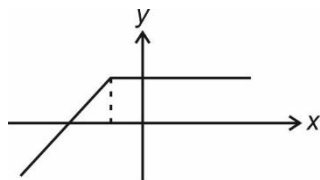
- (1) Continuous everywhere but not differentiable exactly at one point
(2) Continuous everywhere but not differentiable at $x = 1$
(3) Differentiable everywhere
(4) Not continuous at $x = -1$

Answer (1)

Sol.
$$f(x) = \begin{cases} x+1 & x < 0 \\ 1-x & 0 \leq x < 1 \\ x-1 & x > 1 \end{cases} \quad g(x) = \begin{cases} 1+x & x < 0 \\ 1 & x \geq 0 \end{cases}$$

For $g \circ f(x)$

$$g \circ f(x) = \begin{cases} x+2 & x < -1 \\ 1 & x \geq -1 \end{cases}$$



∴ Continuous but not differentiable at $x = -1$

16. Let a, b, c and d be positive real numbers such that $a + b + c + d = 11$. If the maximum value of $a^5 b^3 c^2 d$ is 3750β , then the value of β is

- (1) 90 (2) 110
(3) 55 (4) 108

Answer (1)

Sol. $a + b + c + d = 11$

$$a^5 b^3 c^2 d \Big|_{\min} = 3750\beta$$

$$\text{Assume numbers be } \frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{a}{5}, \frac{b}{3}, \frac{b}{3}, \frac{b}{3}, \frac{c}{2}, \frac{c}{2}, d$$

Apply AM ≥ GM

$$\frac{\frac{a}{5} + \frac{a}{5} + \frac{a}{5} + \frac{a}{5} + \frac{a}{5} + \frac{b}{3} + \frac{b}{3} + \frac{b}{3} + \frac{c}{2} + \frac{c}{2} + d}{11}$$

$$\geq \left(\frac{a^5 b^3 c^2 d}{5^5 3^3 2^2 1} \right)^{\frac{1}{11}}$$

$$\therefore a^5 b^3 c^2 d \leq 90 \times 3750$$

$$\therefore \beta = 90$$

17. For $a \in \mathbb{C}$, let $A = \{z \in \mathbb{C} : \operatorname{Re}(a + \bar{z}) > \operatorname{Im}(\bar{a} + z)\}$

and $B = \{z \in \mathbb{C} : \operatorname{Re}(a + \bar{z}) < \operatorname{Im}(\bar{a} + z)\}$. Then

among the two statements:

- (S1) : If $\operatorname{Re}(a), \operatorname{Im}(a) > 0$, then the set A contains all the real numbers
(S2) : If $\operatorname{Re}(a), \operatorname{Im}(a) < 0$, then the set B contains all the real numbers,

- (1) Only (S2) is true
(2) Only (S1) is true
(3) Both are true
(4) Both are false

Answer (4)

Sol. Let $a = x_1 + iy_1$, $\bar{a} = x_1 - iy_1$

$$z = x_2 + iy_2, \quad \bar{z} = x_2 - iy_2$$

$$A = \{z : x_1 + x_2 > y_2 - y_1\} = \{z : x_1 + y_1 + x_2 > y_2\}$$

$$B = \{z : x_1 + x_2 < y_2 - y_1\} = \{z : x_1 + y_1 + x_2 < y_2\}$$

If $y_2 = 0$ and $x_1, y_1 > 0$, then

$$A = \{z : x_2 > -(x_1 + y_1)\}$$

A covers a part of negative real axis and therefore, does not contain whole real axis

Similarly if $y_2 = 0$, and $x_1, y_1 < 0$, then

$$B = \{z : x_2 < -(x_1 + y_1)\}$$

$\therefore B$ covers part of positive real axis and therefore does not cover whole real axis.

18. If the 1011th term from the end in the binomial expansion of $\left(\frac{4x}{5} - \frac{5}{2x}\right)^{2022}$ is 1024 times 1011th term from the beginning, then $|x|$ is equal to

- (1) 15 (2) 10
(3) 12 (4) 8

Answer (*)

Sol. 1011th term from end = $a_{1013} = 1013^{\text{th}}$ term from beginning

$$\frac{a_{1013}}{a_{1011}} = 1024$$

$$\frac{{}^{2022}C_{1012} \left(\frac{4x}{5}\right)^{1010} \cdot \left(\frac{-5}{2x}\right)^{1012}}{{}^{2022}C_{1010} \left(\frac{4x}{5}\right)^{1012} \left(\frac{-5}{2x}\right)^{1010}} = 1024$$

$$\frac{\left(\frac{-5}{2x}\right)^2}{\left(\frac{4x}{5}\right)^2} = 1024$$

$$\frac{5^4}{2^6 x^4} = 2^{10}$$

$$\left(\frac{5}{x}\right)^4 = 2^{16}$$

$$|x| = \frac{5}{16}$$

Note : If the binomial expansion of $(x + a)^n$ is written in increasing power of x (and decreasing power of a), then answer matches to one of the option.

19. The sum of the coefficients of three consecutive terms in the binomial expansion of $(1 + x)^{n+2}$, which are in the ratio 1 : 3 : 5, is equal to

- (1) 92
(2) 63
(3) 41
(4) 25

Answer (2)

Sol. Let the three terms be T_r, T_{r+1}, T_{r+2}

$$\frac{T_{r+1}}{T_r} = \frac{{}^{n+2}C_r}{{}^{n+2}C_{r-1}} = \frac{n+2-r+1}{r} = \frac{n+3-r}{r} = 3$$

$$n - 4r + 3 = 0 \quad \dots(1)$$

$$\frac{T_{r+2}}{T_{r+1}} = \frac{{}^{n+2}C_{r+1}}{{}^{n+2}C_r} = \frac{(n+2)-(r+1)+1}{r+1} = \frac{n-r+2}{r+1} = \frac{5}{3}$$

$$3n - 8r + 1 = 0 \quad \dots(2)$$

$$(1) \text{ and } (2) \Rightarrow n = 5, r = 2$$

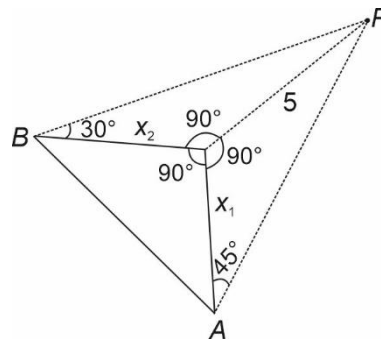
$$T_r + T_{r+1} + T_{r+2} = {}^7C_1 + {}^7C_2 + {}^7C_3 \\ = 7 + 21 + 35 = 63$$

20. The angle of elevation of the top P of a tower from the feet of one person standing due south of the tower is 45° and from the feet of another person standing due west of the tower is 30° . If the height of the tower is 5 meters, then the distance (in meters) between the two persons is equal to

- (1) $\frac{5}{2}\sqrt{5}$
(2) 10
(3) 5
(4) $5\sqrt{5}$

Answer (2)

Sol.



$$\tan 45^\circ = \frac{5}{x_1}, \tan 30^\circ = \frac{5}{x_2}$$

$$x_1 = 5, x_2 = 5\sqrt{3}, AB = 10$$

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. The number of points, where the curve $f(x) = e^{8x} - e^{6x} - 3e^{4x} - e^{2x} + 1$, $x \in \mathbb{R}$ cuts x -axis, is equal to _____

Answer (2)

Sol. $f(x) = e^{8x} - e^{6x} - 3e^{4x} - e^{2x} + 1$, $x \in \mathbb{R}$

$$\lim_{x \rightarrow -\infty} f(x) = 1, \quad f(0) = -3, \quad \lim_{x \rightarrow \infty} f(x) \rightarrow \infty$$

One root of $f(x) = 0$ is negative and other root of $f(x) = 0$ is positive

Curve $y = f(x)$ cuts x -axis at two points

22. Let $S = \left\{ z \in \mathbb{C} - \{i, 2i\} : \frac{z^2 + 8iz - 15}{z^2 - 3iz - 2} \in \mathbb{R} \right\}$. If $\alpha - \frac{13}{11}i \in S$, $\alpha \in \mathbb{R} - \{0\}$, then $242\alpha^2$ is equal to _____.

Answer (1680)

Sol. Put $z = x + iy$

$$\operatorname{Im} \left(\frac{z^2 + 8iz - 15}{z^2 - 3iz - 2} \right) = 0$$

$$\Rightarrow -(x^2 - y^2 - 8y - 15)(2xy - 3x) + (2xy + 8x)(x^2 - y^2 + 3y - 2) = 0$$

$$\Rightarrow (x^2 - y^2)(2xy + 8x - 2xy + 3x) + (8y + 15)(2xy - 3x) + (2xy + 8x)(3y - 2) = 0$$

$$\Rightarrow 11x^3 - 11xy^2 + 16xy^2 - 24xy + 30xy - 45x + 6xy^2 - 4xy + 24xy - 16x = 0$$

$$\Rightarrow 11x^3 + 11xy^2 + 26xy - 61x = 0$$

$$\Rightarrow (11x^2 + 11y^2 + 26y - 61) = 0$$

$$\therefore \alpha \neq 0, \Rightarrow x = 0 \text{ (neglected)}$$

$$\text{Put } y = -\frac{13}{11}, \quad x = \alpha$$

$$11\alpha^2 + 11 \cdot \frac{13^2}{11^2} - 26 \cdot \frac{13}{11} - 61 = 0$$

$$\Rightarrow 121\alpha^2 = 840$$

$$\Rightarrow 242\alpha^2 = 1680$$

23. Let the probability of getting head for a biased coin be $\frac{1}{4}$. It is tossed repeatedly until a head appears.

Let N be the number of tosses required. If the probability that the equation $64x^2 + 5Nx + 1 = 0$ has

no real root is $\frac{p}{q}$, where p and q are co-prime, then $q - p$ is equal to _____.

Answer (27)

Sol. $64x^2 + 5Nx + 1 = 0$ has no real root

$$\Rightarrow 25N^2 - 4 \times 64 < 0$$

$$\Rightarrow N < \frac{16}{5} \Rightarrow N = 1, 2, 3$$

$$\Rightarrow \frac{1}{4} + \frac{3}{4} \times \frac{1}{4} + \frac{3}{4} \cdot \frac{3}{4} \cdot \frac{1}{4} = \frac{p}{q}$$

$$\Rightarrow \frac{p}{q} = \frac{37}{64} \Rightarrow q - p = 64 - 37 = 27$$

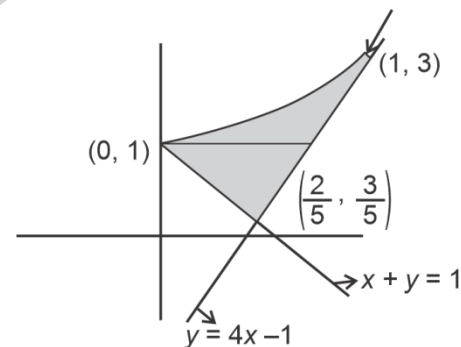
24. If A is the area in the first quadrant enclosed by the curve $C: 2x^2 - y + 1 = 0$, the tangent to C at the point $(1, 3)$ and the line $x + y = 1$, then the value of $60A$ is _____.

Answer (16.00)

Sol. $y = 2x^2 + 1$

$$\text{Tangent : } y - 3 = 4(x - 1)$$

$$y = 4x - 1$$



Required area

$$= \frac{1}{2} \times \frac{1}{2} \times \frac{2}{5} + \int_1^3 \left(\frac{y+1}{4} - \left(\frac{y-1}{2} \right)^{\frac{1}{2}} \right) dy$$

$$= \frac{4}{15}$$

$$60A = 16$$

25. Let the tangent to the parabola $y^2 = 12x$ at the point $(3, \alpha)$ be perpendicular to the line $2x + 2y = 3$. Then the square of distance of the point $(6, -4)$ from the normal to the hyperbola $\alpha^2 x^2 - 9y^2 = 9\alpha^2$ at its point $(\alpha - 1, \alpha + 2)$ is equal to _____.

Answer (116.00)

Sol. Slope of tangent $= 1 = \frac{6}{\alpha} \Rightarrow \boxed{\alpha = 6}$

$$36x^2 - 9y^2 = 324$$

$$\frac{x^2}{9} - \frac{y^2}{36} = 1$$

Tangent at $(5, 8)$

$$\frac{5x}{9} - \frac{8y}{36} = 1$$

$$\boxed{5x - 2y = 9}$$

$$\text{Slope of normal} = \frac{-2}{5}$$

Equation of normal

$$y - 8 = \frac{-2}{5}(x - 5)$$

$$5y - 40 = -2x + 10$$

$$5y + 2x = 50$$

Distance from $(6, -4)$

$$= \left| \frac{12 - 20 - 50}{\sqrt{29}} \right| = \frac{58}{\sqrt{29}}$$

$$= 2\sqrt{29}$$

26. Let $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} - \hat{k}$. If \vec{c} is a vector such that $\vec{a} \cdot \vec{c} = 11$, $\vec{b} \cdot (\vec{a} \times \vec{c}) = 27$ and $\vec{b} \cdot \vec{c} = -\sqrt{3}|\vec{b}|$, then $|\vec{a} \times \vec{c}|^2$ is equal to _____.

Answer (285)

Sol. $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$

$$\vec{b} = \hat{i} + \hat{j} - \hat{k}$$

$$\vec{a} \cdot \vec{c} = 11$$

$$\vec{b} \cdot (\vec{a} \times \vec{c}) = 27$$

$$\vec{b} \cdot \vec{c} = -\sqrt{3}|\vec{b}|$$

$$(\vec{b} \times \vec{a}) \cdot \vec{c} = 27$$

$$\text{Let } \vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$$

$$c_1 + 2c_2 + 3c_3 = 11 \quad \dots(i)$$

$$c_1 + c_2 - c_3 = -\sqrt{3}\sqrt{3}$$

$$c_1 + c_2 - c_3 = -3 \quad \dots(ii)$$

$$5c_1 - 4c_2 + c_3 = 27 \quad \dots(iii)$$

From (i), (ii) & (iii)

$$\vec{c} = 3\hat{i} - 2\hat{j} + 4\hat{k}$$

$$|\vec{a} \times \vec{c}|^2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 3 & -2 & 4 \end{vmatrix}^2$$

$$= |14\hat{i} + 5\hat{j} - 8\hat{k}|^2$$

$$= 14^2 + 5^2 + 8^2 = 285$$

27. Let $A = \{1, 2, 3, 4, 5\}$ and $B = \{1, 2, 3, 4, 5, 6\}$. Then the number of functions $f : A \rightarrow B$ satisfying $f(1) + f(2) = f(4) - 1$ is equal to

Answer (360.00)

Sol. $f(1) + f(2) + 1 = f(4)$

$$\Rightarrow f(1) + f(2) \leq 5$$

Let $f(4) = 6$, then $f(1) + f(2) = 5$

So (f_1, f_2) may be $(1, 4), (4, 1), (2, 3), (3, 2)$

$$\text{Total ways} = 4 \cdot 1 \cdot 6 \cdot 6 = 144$$

Let $f(4) = 5$, $f(1) + f(2) = 4$

so (f_1, f_2) may be $(1, 3), (3, 1), (2, 2)$

$$\text{Total ways} = 3 \cdot 1 \cdot 6 \cdot 6 = 108$$

Let $f(4) = 4$, $f(1) + f(2) = 3$

so (f_1, f_2) may be $(1, 2), (2, 1)$

$$\text{Total ways} = 2 \cdot 1 \cdot 6 \cdot 6 = 72$$

Let $f(4) = 3$, $f(1) + f(2) = 2$

Only way $(1, 1)$

$$\text{Total ways} = 1 \cdot 1 \cdot 36 = 36$$

28. For $k \in \mathbb{N}$, if the sum of the series $1 + \frac{4}{k} + \frac{8}{k^2} + \frac{13}{k^3} + \frac{19}{k^4} + \dots$ is 10, then the value of k is _____.

Answer (2)

Sol. $S = 1 + \frac{4}{k} + \frac{8}{k^2} + \frac{13}{k^3} + \frac{19}{k^4} + \dots$... (i)

$$\frac{1}{k}S = \frac{1}{k} + \frac{4}{k^2} + \frac{8}{k^3} + \dots$$
 ... (ii)

$$(i) - (ii) \Rightarrow \left(1 - \frac{1}{k}\right)S = 1 + \frac{3}{k} + \frac{4}{k^2} + \frac{5}{k^3} + \dots$$
 ... (iii)

Let $S' = \frac{3}{k} + \frac{4}{k^2} + \frac{5}{k^3} + \dots$... (iv)

$$\frac{S'}{k} = \frac{3}{k^2} + \frac{4}{k^3} + \dots$$
 ... (v)

$$(iv) - (v) \Rightarrow \left(1 - \frac{1}{k}\right)S' = \frac{3}{k} + \frac{1}{k^2} + \frac{1}{k^3} + \frac{1}{k^4} + \dots$$

$$= \frac{3}{k} + \frac{\frac{1}{k^2}}{1 - \frac{1}{k}}$$

$$\Rightarrow S' = \frac{3}{k-1} + \frac{1}{(k-1)^2}$$
 ... (vi)

From (iii) and (vi)

$$\frac{k-1}{k}S = 1 + \frac{3}{k-1} + \frac{1}{(k-1)^2}$$

$$S = 10 \Rightarrow 9k^3 - 31k^2 + 31k - 10 = 0$$

$$\Rightarrow k = 2$$

29. Let the line $l: x = \frac{1-y}{-2} = \frac{z-3}{\lambda}$, $\lambda \in \mathbb{R}$ meet the plane $P: x + 2y + 3z = 4$ at the point (α, β, γ) . If the angle between the line l and the plane P is $\cos^{-1}\left(\frac{\sqrt{5}}{\sqrt{14}}\right)$, then $\alpha + 2\beta + 6\gamma$ is equal to _____.

Answer (11)

Sol. $L: \frac{x-0}{1} = \frac{y-1}{2} = \frac{z-3}{\lambda}$ & $P: x + 2y + 3z = 4$

Vector parallel to line : $\langle 1, 2, \lambda \rangle = \vec{b}$

Normal vector to plane P : $\langle 1, 2, 3 \rangle = \vec{n}$

Angle between plane & line is θ

$$\text{Then, } \sin \theta = \frac{|\langle 1, 2, \lambda \rangle \cdot \langle 1, 2, 3 \rangle|}{\sqrt{1^2 + 2^2 + \lambda^2} \cdot \sqrt{1^2 + 2^2 + 3^2}}$$

$$\Rightarrow \frac{3}{\sqrt{14}} = \frac{1 + 4 + 3\lambda}{\sqrt{\lambda^2 + 5} \sqrt{14}} \Rightarrow \lambda = \frac{2}{3}$$

$$L_1 \equiv \frac{x-0}{3} = \frac{y-1}{6} = \frac{z-3}{2} = \mu$$

Any point on line : $(3\mu, 6\mu + 1, 2\mu + 3)$

It lies on $P \Rightarrow 3\mu + 12\mu + 2 + 6\mu + 9 = 4$

$$\Rightarrow \mu = \frac{-1}{3}$$

Hence, $\alpha = 3\mu = -1$, $\beta = 6\mu + 1 = -1$, $\gamma = 2\mu + 3 = \frac{7}{3}$

Now, $\alpha + 2\beta + 6\gamma = 11$

30. If the line $l_1: 3y - 2x = 3$ is the angular bisector of the lines $l_2: x - y + 1 = 0$ and $l_3: \alpha x + \beta y + 17 = 0$, then $\alpha^2 + \beta^2 - \alpha - \beta$ is equal to _____.

Answer (348)

Sol. $L_1: 3y - 2x = 3$

$$L_2: x - y + 1 = 0$$

$$L_3: \alpha x + \beta y + 17 = 0$$

Point of intersection of L_1 & L_2 is $(0, 1)$, should lie

on $L_3 \Rightarrow \beta = -17$

Any point, say $\left(\frac{-3}{2}, 0\right)$ on L_1 should be equidistant from the lines L_2 & L_3

$$\Rightarrow \left| \frac{\frac{-3}{2} - 0 + 1}{\sqrt{1^2 + 1^2}} \right| = \left| \frac{\frac{-3\alpha}{2} + 0 + 17}{\sqrt{\alpha^2 + (-17)^2}} \right|$$

$$\Rightarrow (\alpha - 7)(\alpha - 17) = 0$$

For $\alpha = 17$, L_2 & L_3 coincides $\Rightarrow \alpha = 7$

$$\alpha^2 + \beta^2 - \alpha - \beta = (-17)^2 + 7^2 - 7 + 17 = 348$$

PHYSICS

SECTION - A

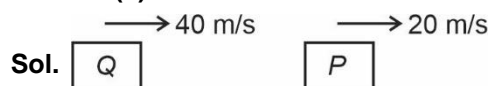
Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

31. A car P travelling at 20 ms^{-1} sounds its horn at a frequency of 400 Hz. Another car Q is travelling behind the first car in the same direction with a velocity 40 ms^{-1} . The frequency heard by the passenger of the car Q is approximately [Take, velocity of sound = 360 ms^{-1}]

- (1) 421 Hz (2) 471 Hz
(3) 485 Hz (4) 514 Hz

Answer (2)



$$f = f_0 \left(\frac{C + 40}{C - 20} \right)$$

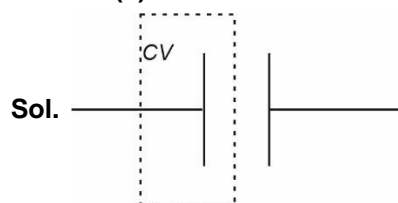
$$= 400 \left(\frac{360 + 40}{360 - 20} \right)$$

$$\approx 471 \text{ Hz}$$

32. A capacitor of capacitance C is charged to a potential V . The flux of the electric field through a closed surface enclosing the positive plate of the capacitor is:

- (1) $\frac{CV}{\epsilon_0}$
(2) Zero
(3) $\frac{2CV}{\epsilon_0}$
(4) $\frac{CV}{2\epsilon_0}$

Answer (1)



$$\phi = \frac{q_{\text{enc}}}{\epsilon_0} = \left(\frac{CV}{\epsilon_0} \right)$$

33. Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**

Assertion A: A bar magnet dropped through a metallic cylindrical pipe takes more time to come down compared to a non-magnetic bar with same geometry and mass.

Reason R: For the magnetic bar, Eddy currents are produced in the metallic pipe which oppose the motion of the magnetic bar.

In the light of the above statements, choose the correct answer from the options given below

- (1) **A** is false but **R** is true
(2) Both **A** and **R** are true and **R** is the correct explanation of **A**
(3) **A** is true but **R** is false
(4) Both **A** and **R** are true but **R** is **NOT** the correct explanation of **A**

Answer (2)

Sol. Due to change in flux, eddy current is produced which opposes the motion.

34. When one light ray is reflected from a plane mirror with 30° angle of reflection, the angle of deviation of the ray after reflection is:

- (1) 120° (2) 110°
(3) 140° (4) 130°

Answer (1)

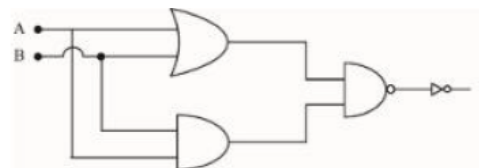
Sol. As $i = 30^\circ$

$$\delta = 180^\circ - 2i$$

$$= 180^\circ - 60^\circ$$

$$= 120^\circ$$

35. The logic operations performed by the given digital circuit is equivalent to:



- (1) NOR
(2) AND
(3) OR
(4) NAND

Answer (2)

Sol. $(A + B) \cdot (A \cdot B) = A \cdot (AB) + B \cdot (AB)$

$$= AB + AB$$

$$= (AB)$$

36. If V is the gravitational potential due to sphere of uniform density on its surface, then its value at the centre of sphere will be:

- (1) $\frac{4}{3}V$ (2) $\frac{V}{2}$
(3) V (4) $\frac{3V}{2}$

Answer (4)

Sol. $V = \frac{GM}{R}$

$$V_{\text{centre}} = -\frac{3}{2} \left(\frac{GM}{R} \right) = \left(\frac{3}{2} V \right)$$

37. In satellite communication, the uplink frequency band used is:

- (1) 420–890 MHz (2) 5.925–6.425 GHz
(3) 76–88 MHz (4) 3.7 – 4.2 GHz

Answer (2)

Sol. Uplink frequency band for satellite communication is 5.925 – 6.425 GHz.

38. When vector $\vec{A} = 2\hat{i} + 3\hat{j} + 2\hat{k}$ is subtracted from vector \vec{B} , it gives a vector equal to $2\hat{j}$. Then the magnitude of vector \vec{B} will be:

- (1) $\sqrt{5}$ (2) 3
(3) $\sqrt{6}$ (4) $\sqrt{13}$

Answer (*)

Sol. $\vec{B} - (2\hat{i} + 3\hat{j} + 2\hat{k}) = 2\hat{j}$

$$\vec{B} = 2\hat{i} + 5\hat{j} + 2\hat{k}$$

$$|\vec{B}| = \sqrt{4 + 25 + 4} = \sqrt{33}$$

39. A projectile is projected at 30° from horizontal with initial velocity 40 ms^{-1} . The velocity of the projectile at $t = 2 \text{ s}$ from the start will be:

(Given $g = 10 \text{ m/s}^2$)

- (1) $40\sqrt{3} \text{ ms}^{-1}$ (2) Zero
(3) 20 ms^{-1} (4) $20\sqrt{3} \text{ ms}^{-1}$

Answer (4)

Sol. $V_H = 40 \cos 30^\circ = 20\sqrt{3}$

$$V_V = 20 - 10 \times 2 = 0 \text{ m/s}$$

$$V = V_H = 20\sqrt{3} \text{ m/s}$$

40. A body of mass 500 g moves along x-axis such that its velocity varies with displacement x according to the relation $v = 10\sqrt{x} \text{ m/s}$ the force acting on the body is:

- (1) 125 N (2) 25 N
(3) 166 N (4) 5 N

Answer (2)

Sol. $v = 10\sqrt{x}$

$$\frac{dv}{dx} = \frac{10}{2\sqrt{x}} = \frac{5}{\sqrt{x}}$$

$$v \frac{dv}{dx} = a = 10\sqrt{x} \times \frac{5}{\sqrt{x}} = 50 \text{ m/s}^2$$

$$F = \frac{1}{2} \times 50 = 25 \text{ N}$$

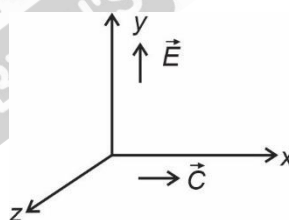
41. A plane electromagnetic wave of frequency 20 MHz propagates in free space along x-direction. At a particular space and time $\vec{E} = 6.6\hat{j} \text{ V/m}$. What is \vec{B} at this point?

- (1) $2.2 \times 10^{-8} \hat{k} \text{ T}$ (2) $-2.2 \times 10^{-8} \hat{i} \text{ T}$
(3) $-2.2 \times 10^{-8} \hat{k} \text{ T}$ (4) $2.2 \times 10^{-8} \hat{i} \text{ T}$

Answer (1)

Sol. $\vec{E} = 6.6\hat{j} \text{ (V/m)}$

$$\vec{E} \times \vec{B} = \vec{C}$$



$$\vec{B} = B_0(\hat{k})$$

$$CB_0 = E$$

$$B_0 = \left(\frac{E}{C} \right) = \frac{6.6}{3 \times 10^8} = 2.2 \times 10^{-8} \text{ T}$$

42. The root mean square speed of molecules of nitrogen gas at 27°C is approximately: (Given mass of a nitrogen molecule = $4.6 \times 10^{-26} \text{ kg}$ and take Boltzmann constant $k_B = 1.4 \times 10^{-23} \text{ JK}^{-1}$)

- (1) 27.4 m/s (2) 91 m/s
(3) 1260 m/s (4) 523 m/s

Answer (4)

Sol. $V_{\text{rms}} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3 \times 1.4 \times 10^{-23} \times 300}{4.6 \times 10^{-26}}}$
 $\approx 523 \text{ m/s}$

43. Eight equal drops of water are falling through air with a steady speed of 10 cm/s. If the drops coalesce, the new velocity is:-

- (1) 16 cm/s
(2) 40 cm/s
(3) 5 cm/s
(4) 10 cm/s

Answer (2)

Sol. $V_T \propto r^2$

$$\text{as, } 8r_1^3 = r_2^3$$

$$\left(\frac{V_T}{V_T}\right)_1 = \left(\frac{r_1}{r_2}\right)^2$$

$$\Rightarrow \frac{r_1}{r_2} = \left(\frac{1}{2}\right)$$

$$\frac{10}{V_T} = \frac{1}{4}$$

$$\Rightarrow \boxed{V_T = 40 \text{ cm/s}}$$

44. An electron is allowed to move with constant velocity along the axis of current carrying straight solenoid.

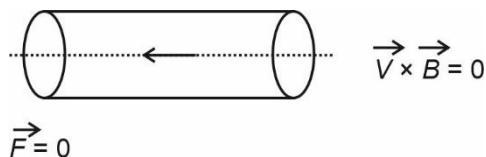
- (A) The electron will experience magnetic force along the axis of the solenoid.
(B) The electron will not experience magnetic force.
(C) The electron will continue to move along the axis of the solenoid.
(D) The electron will be accelerated along the axis of the solenoid.
(E) The electron will follow parabolic path-inside the solenoid.

Choose the correct answer from the option given below:

- (1) B, C and D only (2) A and D only
(3) B and C only (4) B and E only

Answer (3)

Sol.



45. A space ship of mass 2×10^4 kg is launched into a circular orbit close to the earth surface. The additional velocity to be imparted to the space ship in the orbit to overcome the gravitational pull will be (if $g = 10 \text{ m/s}^2$ and radius of earth = 6400 km):

- (1) $11.2(\sqrt{2}-1) \text{ km/s}$ (2) $8(\sqrt{2}-1) \text{ km/s}$
(3) $7.9(\sqrt{2}-1) \text{ km/s}$ (4) $7.4(\sqrt{2}-1) \text{ km/s}$

Answer (2)

$$\begin{aligned} \text{Sol. } \Delta V &= \sqrt{\frac{2GM}{R}} - \sqrt{\frac{GM}{R}} = (\sqrt{2}-1)\sqrt{\frac{GM}{R}} \\ &= (\sqrt{2}-1)\sqrt{gR} \\ &= (\sqrt{2}-1)\sqrt{10 \times 6400 \times 10^3} \\ &= 8(\sqrt{2}-1) \text{ km/s} \end{aligned}$$

46. The ratio of the de-Broglie wavelengths of proton and electron having same kinetic energy:

(Assume $m_p = m_e \times 1849$)

- (1) 1 : 43 (2) 1 : 30
(3) 1 : 62 (4) 2 : 43

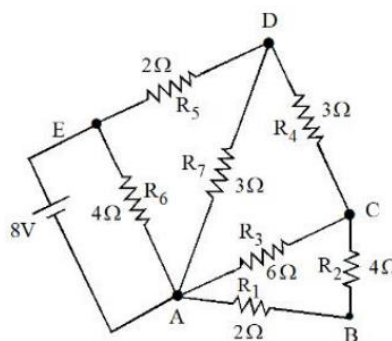
Answer (1)

Sol. $(K)_e = (K)_p$

$$\lambda = \frac{h}{\sqrt{2km}}$$

$$\frac{\lambda_p}{\lambda_e} = \frac{\sqrt{2k_e m_e}}{\sqrt{2k_e m_p}} = \sqrt{\frac{m_e}{m_p}} = \sqrt{\frac{1}{1849}} = \frac{1}{43}$$

- 47.



The current flowing through R_2 is :

- (1) $\frac{2}{3} \text{ A}$ (2) $\frac{1}{2} \text{ A}$
(3) $\frac{1}{3} \text{ A}$ (4) $\frac{1}{4} \text{ A}$

Answer (3)

Sol. I through battery $\frac{8}{2} = 4 \text{ A}$

$$I \text{ through } CD = \frac{3}{9} \times 2 = \frac{2}{3} \text{ A}$$

$$I \text{ through } R_2 = \frac{1}{2} \left(\frac{2}{3} \right) = \frac{1}{3} \text{ A}$$

48. The thermodynamic process, in which internal energy of the system remains constant is

- (1) Isochoric
- (2) Adiabatic
- (3) Isothermal
- (4) Isobaric

Answer (3)

Sol. $\Delta T = 0, \Delta U = 0$

49. If force (F), velocity (V) and time (T) are considered as fundamental physical quantity, then dimensional formula of density will be :

- (1) FV^4T^{-6}
- (2) $FV^{-4}T^{-2}$
- (3) $F^2V^{-2}T^6$
- (4) $FV^{-2}T^2$

Answer (2)

Sol. Density = $\frac{M}{L^3} = ML^{-3} = [MLT^{-2}]^x [LT^{-1}]^y [T]^z$

$$ML^{-3} = M^x L^{(x+y)} T^{-2x-y+z}$$

$$\begin{aligned} x = 1, \quad x + y = -3, \quad -2x - y + z = 0 \\ y = -4 \quad -2 + 4 + z = 0 \\ z = -2 \end{aligned}$$

$$\text{density} = FV^{-4}T^{-2}$$

50. The energy of He^+ ion in its first state is, (The ground state energy for the Hydrogen atom -13.6 eV):

- (1) -27.2 eV
- (2) -3.4 eV
- (3) -13.6 eV
- (4) -54.4 eV

Answer (3)

Sol. $E = -\frac{13.6 \times 2^2}{2^2} = -13.6 \text{ eV}$

SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33 , -00.30 , 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

51. A nucleus disintegrates into two nuclear parts, in such a way that ratio of their nuclear sizes is $1 : 2^{1/3}$. Their respective speed have a ratio of $n : 1$. The value of n is _____

Answer (2)

Sol. Momentum conservation

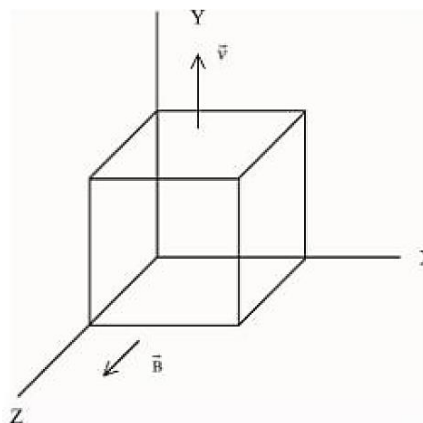
$$m_1 v_1 = m_2 v_2$$

$$\Rightarrow \left(\frac{m_1}{m_2} \right) = \left(\frac{v_2}{v_1} \right)$$

$$\Rightarrow \left(\frac{r_1^3}{r_2^3} \right) = \left(\frac{v_2}{v_1} \right) \Rightarrow \left(\frac{1}{2} \right) = \left(\frac{v_2}{v_1} \right)$$

$$\frac{v_1}{v_2} = \frac{2}{1}$$

52. A metallic cube of side 15 cm moving along y -axis at a uniform velocity of 2 ms^{-1} . In a region of uniform magnetic field of magnitude 0.5 T directed along z -axis. In equilibrium the potential difference between the faces of higher and lower potential developed because of the motion through the field will be _____ mV .



Answer (150)

Sol. $qE = eVB \Rightarrow \Delta V = (E.d)$

$$E = VB = (VB) \times 0.15$$

$$= 2 \times \frac{1}{2} \times 0.15 \text{ V}$$

$$= 0.15 \text{ V} = 150 \text{ mV}$$

53. A wire of density $8 \times 10^3 \text{ kg/m}^3$ is stretched between two clamps 0.5 m apart. The extension developed in the wire is $3.2 \times 10^{-4} \text{ m}$. If $Y = 8 \times 10^{10} \text{ N/m}^2$, the fundamental frequency of vibration in the wire will be _____ Hz.

Answer (80)

Sol. $\frac{T}{A} = Y \left(\frac{\Delta L}{L} \right) \quad \mu = \left(\frac{m}{L} \right)$

$$T = \left(\frac{Y \Delta L}{L} \times A \right)$$

$$\frac{T}{\mu} = \frac{Y \Delta L A}{L \left(\frac{m}{L} \right)} = \frac{Y(\Delta L) \times LA}{L(m)} = \left(\frac{Y \Delta L}{L} \right) \times \left(\frac{1}{\rho} \right)$$

$$\frac{T}{\mu} = \frac{8 \times 10^{10} \times 3.2 \times 10^{-4}}{0.5} \times \left(\frac{1}{8 \times 10^3} \right) = 6.4 \times 10^3$$

$$\frac{T}{\mu} = 64 \times 10^2$$

$$\sqrt{\frac{T}{\mu}} = 8 \times 10 = 80 \text{ m/s}$$

$$f = \left(\frac{V}{2L} \right) = \left(\frac{80}{1} \right) = 80 \text{ Hz}$$

54. A coil has an inductance of 2 H and resistance of 4Ω . A 10 V is applied across the coil. The energy stored in the magnetic field after the current has built up to its equilibrium value will be _____ $\times 10^{-2} \text{ J}$.

Answer (625)

Sol. $I = \frac{10}{4} = \frac{5}{2} \text{ A}$

$$E = \frac{1}{2} L I^2 = \frac{1}{2} \times 2 \times \left(\frac{25}{4} \right) = 625 \times 10^{-2} \text{ J}$$

55. A circular plate is rotating in horizontal plane, about an axis passing through its centre and perpendicular to the plate, with an angular velocity ω . A person sits at the centre having two dumbbells in his hands. When he stretched out his hands, the moment of inertia of the system becomes triple. If E be the initial Kinetic energy of the system, then final Kinetic energy will be $\frac{E}{x}$. The value of x is

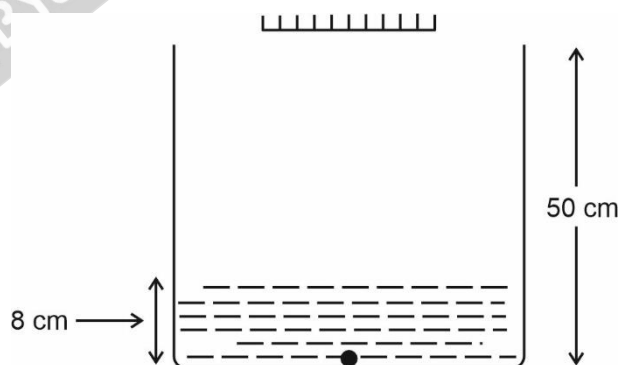
Answer (3)

Sol. $E = \frac{1}{2} I \omega^2 = \left(\frac{L^2}{2I} \right)$

as $I' = 3I$

$$E_f = \frac{L^2}{6I} \Rightarrow E_f = \left(\frac{E}{3} \right)$$

56. As shown in the figure, a plane mirror is fixed at a height of 50 cm from the bottom of tank containing water $\left(\mu = \frac{4}{3} \right)$. The height of water in the tank is 8 cm. A small bulb is placed at the bottom of the water tank. The distance of image of the bulb formed by mirror from the bottom of the tank is _____ cm.



Answer (98)

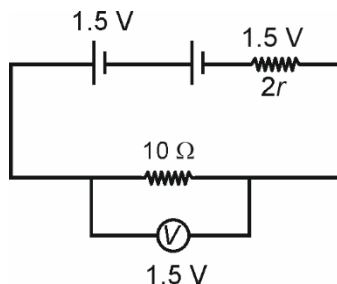
Sol. $h' = \frac{8}{\frac{4}{3}} = 6 \text{ cm}$

Distance of object from mirror = $42 + 6 = 48 \text{ m}$

Distance of image from bottom of tank = $48 + 50$
 $= 98 \text{ m}$

57. Two identical cells each of emf 1.5 V are connected in series across a $10\ \Omega$ resistance. An ideal voltmeter connected across $10\ \Omega$ resistance reads 1.5 V. The internal resistance of each cell is _____ Ω .

Answer (5)



Sol.

$$i = \left(\frac{3}{10 + 2r} \right)$$

$$10 \times \frac{3}{10 + 2r} = 1.5$$

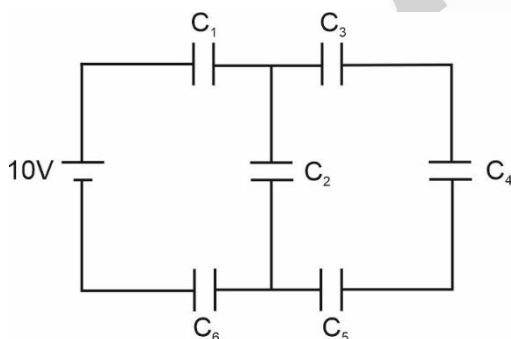
$$20 = 10 + 2r$$

$$\Rightarrow 2r = 10$$

$$\boxed{r = 5\Omega}$$

58. In the given circuit.

$C_1 = 2\ \mu\text{F}$, $C_2 = 0.2\ \mu\text{F}$, $C_3 = 2\ \mu\text{F}$, $C_4 = 4\ \mu\text{F}$, $C_5 = 2\ \mu\text{F}$, $C_6 = 2\ \mu\text{F}$. The charge stored on capacitor C_4 _____ μC .



Answer (4)

Sol. q through battery $= 10 \times \frac{1}{2} = 5\ \mu\text{C}$

$$\frac{q}{0.8\ \text{C}} = \frac{5 - q}{0.2}$$

$$\Rightarrow q = 20 - 4q$$

$$5q = 20$$

$$q = 4\ \mu\text{C}$$

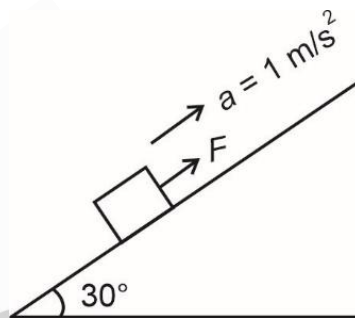
59. A block of mass 5 kg starting from rest pulled up on a smooth incline plane making an angle of 30° with horizontal with an effective acceleration of $1\ \text{ms}^{-2}$. The power delivered by the pulling force at $t = 10\ \text{s}$ from the start is _____ W

[Use $g = 10\ \text{ms}^{-2}$]

(Calculate the nearest integer value)

Answer (300)

Sol.



$$F - 50 \sin 30 = 5 \times 1$$

$$F = 5 + 25 = 30\ \text{N}$$

$$v \text{ at } t = 10\ \text{sec} = 0 + 1 \times 10 = 10\ \text{m/s}$$

$$\text{Power} = 30 \times 10 = 300\ \text{watt}$$

60. The surface tension of soap solution is $3.5 \times 10^{-2}\ \text{Nm}^{-1}$. The amount of work done required to increase the radius of soap bubble from 10 cm to 20 cm is _____ $\times 10^{-4}\ \text{J}$. (take $\pi = 22/7$)

Answer (264)

Sol. $\Delta U = \Delta w = (T \times \Delta A) \times 2$

$$= 3.5 \times 10^{-2} \times 4\pi[(0.2)^2 - (0.1)^2] \times 2$$

$$= 3.5 \times 10^{-2} \times 4 \times \frac{22}{7} \times 0.03 \times 2$$

$$= 2 \times 1.32 \times 10^{-2}$$

$$= 2 \times 132 \times 10^{-4}\ \text{J}$$

$$= 264 \times 10^{-4}\ \text{J}$$

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

61. For a chemical reaction $A + B \rightarrow \text{Product}$, the order is 1 with respect to A and B.

Rate $\text{mol L}^{-1} \text{S}^{-1}$	[A] mol L^{-1}	[B] mol L^{-1}
0.10	20	0.5
0.40	x	0.5
0.80	40	y

What is the value of x and y?

- (1) 160 and 4
- (2) 80 and 4
- (3) 80 and 2
- (4) 40 and 4

Answer (3)

Sol. Rate of Reaction $\propto (A)^x (B)^y$

From experiment II $x = 80$

from experiment III $y = 2$

62. Which of the following compounds is an example of Freon?

- (1) $\text{C}_2\text{H}_2\text{F}_2$
- (2) C_2F_4
- (3) C_2HF_3
- (4) $\text{C}_2\text{Cl}_2\text{F}_2$

Answer (4)

Sol. From is chlorofluoro carbons. Hence the correct answer is (4).

63. Alkali metal from the following with least melting point is

- (1) Cs
- (2) Rb
- (3) Na
- (4) K

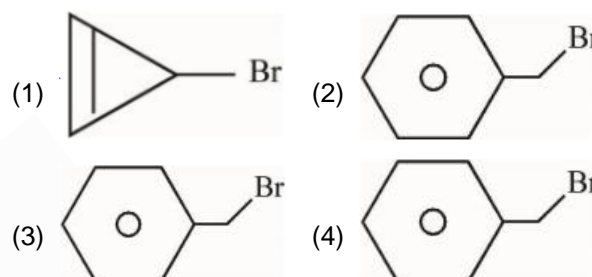
Answer (1)

Sol. Element

M.P. (K)

Na	371
K	336
Rb	312
Cl	302

64. Compound from the following that will not produce precipitate on reaction with AgNO_3 is



Answer (4)

Sol. Compounds which results in the formation of stable carbocation upon reacting with AgNO_3 will produce precipitate.

65. Which one of the following pairs is an example of polar molecular solids?

- (1) $\text{SO}_2(\text{s})$, $\text{CO}_2(\text{s})$
- (2) $\text{SO}_2(\text{s})$, $\text{NH}_3(\text{s})$
- (3) $\text{MgO}(\text{s})$, $\text{SO}_2(\text{s})$
- (4) $\text{HCl}(\text{s})$, $\text{AlN}(\text{s})$

Answer (2)

Sol. Solide

type

$\text{SO}_2(\text{s})$	Polar molecular
$\text{CO}_2(\text{s})$	Non polar molecular
$\text{NH}_3(\text{s})$	Polar molecular
MgO	Ionic Solid
HCl	Polar molecular solid
AlN	Covalent solid

66. Which hydride among the following is less stable?

- (1) BeH_2
- (2) HF
- (3) NH_3
- (4) LiH

Answer (1)

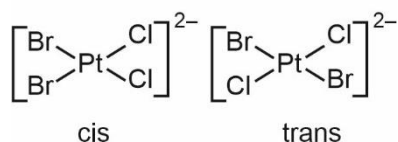
Sol. BeH_2 is the least stable among the given hydrides.

67. If Ni^{2+} is replaced by Pt^{2+} in the complex $[\text{NiCl}_2\text{Br}_2]^{2-}$, which of the following properties are expected to get changed?

- A. Geometry
B. Geometrical isomerism
C. Optical isomerism
D. Magnetic properties
- (1) A and D (2) A, B and C
(3) B and C (4) A, B and D

Answer (4)

Sol. $[\text{Pt} + \text{Cl}_2\text{Br}_2]^{2-}$ — Square planar



$[\text{PtCl}_2\text{Br}_2]^{2-}$ — Diamagnetic

68. Match List I with List II

LIST-I		LIST II	
Complex		Colour	
A.	$\text{Mg}(\text{NH}_4)\text{PO}_4$	I.	brown
B.	$\text{K}_3[\text{Co}(\text{NO}_2)_6]$	II.	white
C.	$\text{MnO}(\text{OH})_2$	III.	yellow
D.	$\text{Fe}_4[\text{Fe}(\text{CN})_6]_3$	IV.	Blue

Choose the correct answer from the options given below:

- (1) A-III, B-IV, C-II, D-I (2) A-II, B-III, C-I, D-IV
(3) A-II, B-IV, C-I, D-III (4) A-II, B-III, C-IV, D-I

Answer (2)

Sol.

Complex	Colour
$\text{Mg}(\text{NH}_4)\text{PO}_4$	White
$\text{K}_3[\text{Co}(\text{NO}_2)_6]$	Yellow
$\text{MnO}(\text{OH})_2$	Brown
$\text{Fe}_4[\text{Fe}(\text{CN})_6]_3$	Blue

69. Given below are two statements :

Statement I : In the metallurgy process, sulphide ore is converted to oxide before reduction.

Statement II : Oxide ores in general are easier to reduce.

In the light of the above statements, choose the most appropriate answer from the options given below :

- (1) Statement I is correct but Statement II is incorrect
(2) Both Statement I and Statement II are incorrect
(3) Statement I is incorrect but Statement II is correct
(4) Both Statement I and Statement II are correct

Answer (4)

Sol. Both Statements (I) and (II) are correct.

70. A solution is prepared by adding 2 g of "X" to 1 mole of water. Mass percent of "X" in the solution is

- (1) 5%
(2) 20%
(3) 2%
(4) 10%

Answer (4)

Sol. Mass percent of X = $\frac{2}{2+18} \times 100 = 10$

71. What weight of glucose must be dissolved in 100 g of water to lower the vapour pressure by 0.20 mm Hg?

(Assume dilute solution is being formed)

Given : Vapour pressure of pure water is 54.2 mm Hg at room temperature. Molar mass of glucose is 180 g mol^{-1}

- (1) 3.59 g (2) 3.69 g
(3) 4.69 g (4) 2.59 g

Answer (2)

Sol. Using the formula

$$\frac{P_0 - P}{P} = \frac{\text{Moles of solute}}{\text{Moles of solvent}}$$

$$\frac{54.2 - 54}{54} = \frac{w/180}{\frac{100}{18}}$$

$$w = 3.69 \text{ g}$$

72. Given below are two statements :

Statement I : Ethane at 333 to 343 K and 6-7 atm pressure in the presence of AlEt_3 and TiCl_4 undergoes addition polymerization to give LDP.

Statement II : Caprolactam at 533-543K in H_2O through step growth polymerizes to give Nylon 6.

In the light of the above statements, choose the correct answer from the options given below:

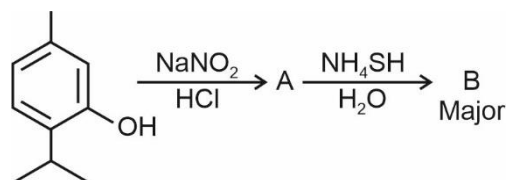
- (1) Statement I is false but Statement II is true
- (2) Statement I is true but Statement II is false
- (3) Both Statement I and Statement II are true
- (4) Both Statement I and Statement II are false

Answer (1)

Sol. Ethene at 333 to 343 K and 6-7 atm pressure in the presence of AlEt_3 and TiCl_4 undergo addition polymerization to give HDP.

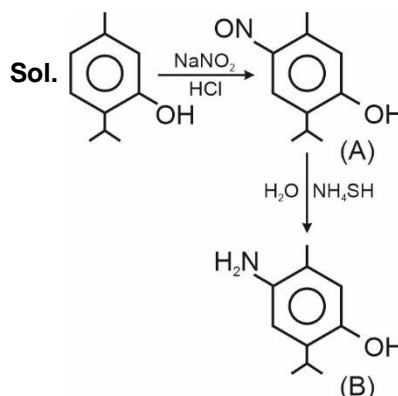
Caprolactam at 533-543 K in H_2O through step growth polymerization gives Nylon 6.

73. Compound 'B' is



- (1)
- (2)
- (3)
- (4)

Answer (1)



74. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

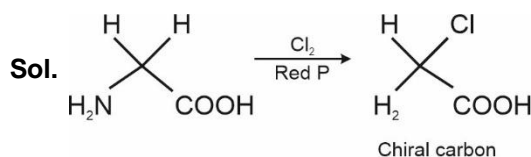
Assertion A : A solution of the product obtained by heating a mole of glycine with a mole of chlorine in presence of red phosphorous generates chiral carbon atom.

Reason R : A molecule with 2 chiral carbons is always optically active.

In the light of the above statements, choose the correct answer from the options given below :

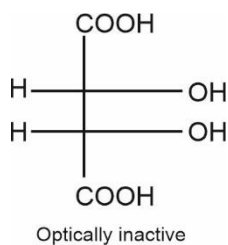
- (1) A is true but R is false
- (2) Both A and R are true but R is the correct explanation of A
- (3) A is false but R is true
- (4) Both A and R are true but R is NOT the correct explanation of A

Answer (1)

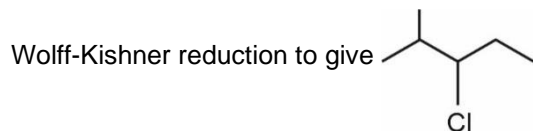
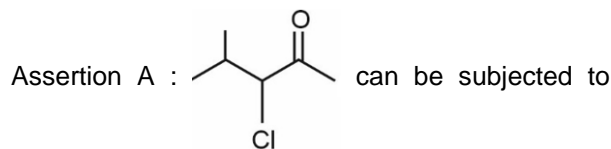


All molecules with 2 chiral carbons are not always optically active.

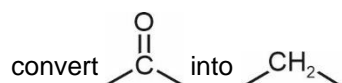
E.g.



75. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.



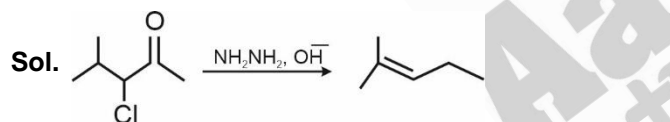
Reason R : Wolff-Kishner reduction is used to





In the light of the above statements, choose the correct answer from the options given below :

- (1) A is true but R is false
- (2) A is false but R is true
- (3) Both A and R are true and R is the correct explanation of A
- (4) Both A and R are true but R is NOT the correct explanation of A

Answer (2)



Wolff-Kishner reduction is used to convert  into .

76. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A : $[\text{CoCl}(\text{NH}_3)_5]^{2+}$ absorbs at lower wavelength of light with respect to $[\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+}$

Reason R : It is because the wavelength of the light absorbed depends on the oxidation state of the metal ion.

In the light of the above statements, choose the correct answer from the options given below :

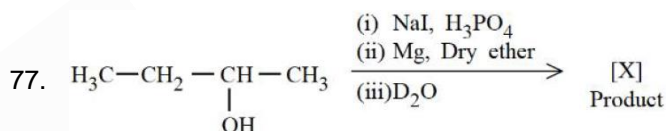
- (1) A is false but R is true
- (2) A is true but R is false
- (3) Both A and R are true and R is the correct explanation of A
- (4) Both A and R are true but R is NOT the correct explanation of A

Answer (1)

Sol. $[\text{CoCl}(\text{NH}_3)_5]^{2+}$ absorbs at higher wavelength of light with respect to $[\text{Co}(\text{NH}_3)_5(\text{H}_2\text{O})]^{3+}$ because Cl^- is weaker ligand than H_2O .

Wavelength of light absorbed depends upon the oxidation state of the metal ion.

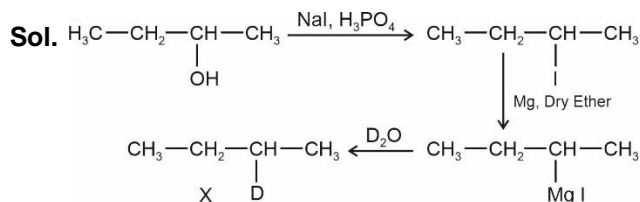
Hence, A is false but R is true.



Product [X] formed in the above reaction is :

- (1) $\text{H}_3\text{C}-\text{CH}_2-\underset{\text{OH}}{\overset{\text{H}}{\text{C}}}-\text{CH}_3$
- (2) $\text{H}_3\text{C}-\text{CH}=\text{CH}-\text{CH}_3$
- (3) $\text{H}_3\text{C}-\text{CH}_2-\underset{\text{D}}{\text{CH}}-\text{CH}_3$
- (4) $\text{H}_3\text{C}-\text{CH}_2-\text{CH}=\text{CH}_2$

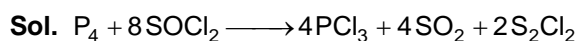
Answer (3)



78. One mole of P_4 reacts with 8 moles of SOCl_2 to give 4 moles of A, x mole of SO_2 and 2 moles of B. A, B and x respectively are

- (1) POCl_3 , S_2Cl_2 and 2
- (2) PCl_3 , S_2Cl_2 and 4
- (3) PCl_3 , S_2Cl_2 and 2
- (4) POCl_3 , S_2Cl_2 and 4

Answer (2)



Hence, A = PCl_3 , x = 4, B = S_2Cl_2

79. The magnetic moment is measured in Bohr Magneton (BM).

Spin only magnetic moment of Fe in $[\text{Fe}(\text{H}_2\text{O})_6]^{3+}$ and $[\text{Fe}(\text{CN})_6]^{3-}$ complexes respectively is:

- (1) 6.92 B.M. in both
- (2) 3.87 B.M. and 1.732 B.M.
- (3) 5.92 B.M. and 1.732 B.M.
- (4) 4.89 B.M. and 6.92 B.M.

Answer (3)

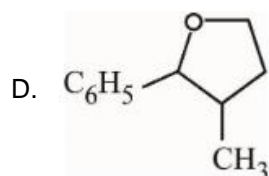
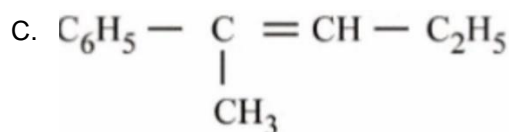
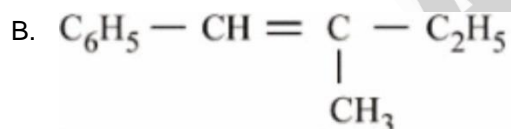
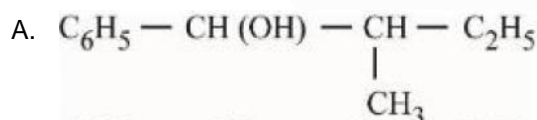
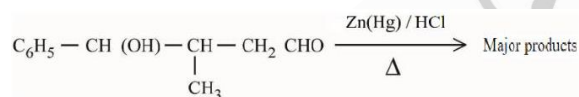
Sol. $[\text{Fe}(\text{H}_2\text{O})_6]^{3+} = d^5$ (H.S.) = 5 unpaired electrons

$$\mu = \sqrt{5 \times 7} = \sqrt{35} \\ = 5.92 \text{ B.M.}$$

$[\text{Fe}(\text{CN})_6]^{3-} = d^5$ (L.S.) = 1 unpaired electrons

$$\mu = \sqrt{1 \times 3} = \sqrt{3} \\ = 1.732 \text{ B.M.}$$

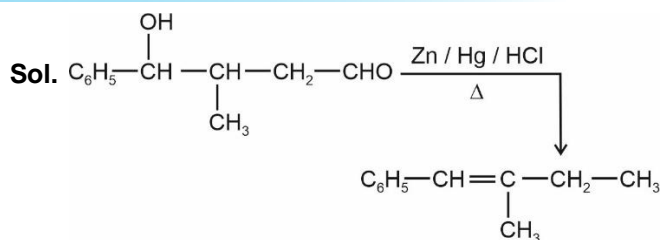
80. The major product formed in the following reaction is



Choose the correct answer from the options given below:

- (1) B only
- (2) A only
- (3) C only
- (4) D only

Answer (B)



SECTION - B

Numerical Value Type Questions: This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g., 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

81. Number of compounds from the following which will not produce orange red precipitate with Benedict solution is _____.

Glucose, maltose, sucrose, ribose, 2-deoxyribose, amylose, lactose

Answer (2)

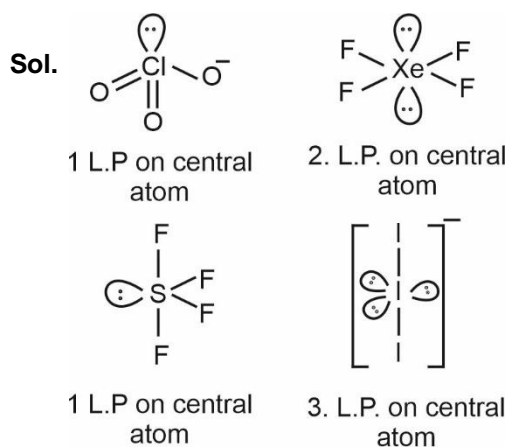
Sol. Except sucrose and amylose all other give orange red precipitate with Benedict solution.

Sucrose being non-reducing disaccharide and amylose being polysaccharides do not give positive Benedict's test.

82. The maximum number of lone pairs of electron on the central atom from the following species is _____.

ClO_3^- , XeF_4 , SF_4 and I_3^-

Answer (3)



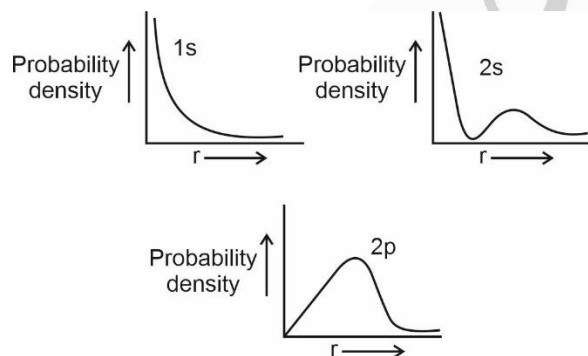
83. The number of correct statements from the following is _____.

- A. For 1s orbital, the probability density is maximum at the nucleus
- B. For 2s orbital, the probability density first increases to maximum and then decreases sharply to zero.
- C. Boundary surface diagrams of the orbitals encloses a region of 100% probability of finding the electron.
- D. p and d-orbitals have 1 and 2 angular nodes respectively
- E. probability density of p-orbital is zero at the nucleus

Answer (3)

Sol. Except B and C all statements are correct.

Probability density curves for 1s, 2s and 2p orbitals are given below.



84. The total number of intensive properties from the following is _____.

Volume, Molar heat capacity, molarity, E^\ominus cell, Gibbs free energy change, Molar mass, Mole

Answer (4)

Sol. Molar heat capacity, molarity, E^\ominus_{cell} and molar mass are intensive properties.

85. 4.5 moles each of hydrogen and iodine is heated in a sealed ten litre vessel. At equilibrium, 3 moles of HI were found. The equilibrium constant for $\text{H}_2(\text{g}) + \text{I}_2(\text{g}) \rightleftharpoons 2\text{HI}(\text{g})$ is _____.

Answer (1)

Sol. $\text{H}_2 + \text{I}_2 \rightleftharpoons 2\text{HI}$

at initial	4.5	4.5	0
at equilibrium	3	3	3

$$K_{\text{eq}} = \frac{[\text{HI}]^2}{[\text{H}_2][\text{I}_2]} = \frac{(3)^2}{3 \times 3} = 1$$

86. The volume of hydrogen liberated at STP by treating 2.4 g of magnesium with excess of hydrochloric acid is _____ $\times 10^{-2}$ L

Given: Molar volume of gas is 22.4 L at STP.

Molar mass of magnesium is 24 g mol^{-1}

Answer (224)

Sol. $\text{Mg} + 2\text{HCl} \longrightarrow \text{MgCl}_2 + \text{H}_2$
 $\frac{2.4\text{g}}{24} = 0.1 \text{ mole}$
 $\frac{2.4}{24} = 0.1 \text{ mole}$

Volume of 1 mole H_2 at STP = 22.4 Litre

\therefore 0.1 mole H_2 at STP will occupy = 2.24 Litre

87. The number of correct statements about modern adsorption theory of heterogeneous catalysis from the following is _____.

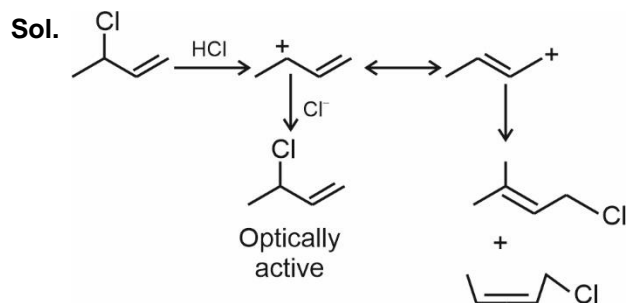
- A. The catalyst is diffused over the surface of reactants.
- B. Reactants are adsorbed on the surface of the catalyst.
- C. Occurrence of chemical reaction on the catalyst's surface through formation of an intermediate.
- D. It is a combination of intermediate compound formation theory and the old adsorption theory.
- E. It explains the action of the catalyst as well as those of catalytic promoters and poisons.

Answer (3)

Sol. Except (A) and (E) all statements are correct.

88. The number of possible isomeric products formed when 3-chloro-1-butene reacts with HCl through carbocation formation is _____.

Answer (4)



89. $\text{Mg}(\text{NO}_3)_2 \cdot x\text{H}_2\text{O}$ and $\text{Ba}(\text{NO}_3)_2 \cdot y\text{H}_2\text{O}$, represent formula of the crystalline forms of nitrate salts. Sum of X and Y is _____.

Answer (6)

Sol. Magnesium nitrate crystallises with six molecules of water, whereas barium nitrate crystallises as the anhydrous salt as $\text{Mg}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$

$\text{Ba}(\text{NO}_3)_2$ respectively

$\therefore x = 6, y = 0$

90. The number of correct statements from the following is _____.

- A. E_{cell} is an intensive parameter
- B. A negative E^\ominus means that the redox couple is a stronger reducing agent than the H^+/H_2 couple.
- C. The amount of electricity required for oxidation or reduction depends on the stoichiometry of the electrode reaction.
- D. The amount of chemical reaction which occurs at any electrode during electrolysis by a current is proportional to the quantity of electricity passed through the electrolyte.

Answer (4)

Sol. All statements are correct.

□ □ □