

EXERCISE 3.6 PAGE: 67

1. Solve the following pairs of equations by reducing them to a pair of linear equations:

(i)
$$1/2x + 1/3y = 2$$

$$1/3x + 1/2y = 13/6$$

Solution:

Let us assume 1/x = m and 1/y = n, then the equation will change as follows.

$$m/2 + n/3 = 2$$

$$\Rightarrow$$
 3m+2n-12 = 0....(1)

$$m/3 + n/2 = 13/6$$

$$\Rightarrow$$
 2m+3n-13 = 0....(2)

Now, using cross-multiplication method, we get,

$$m/(-26-(-36)) = n/(-24-(-39)) = 1/(9-4)$$

$$m/10 = n/15 = 1/5$$

$$m/10 = 1/5$$
 and $n/15 = 1/5$

So,
$$m = 2$$
 and $n = 3$

$$1/x = 2$$
 and $1/y = 3$

$$x = 1/2$$
 and $y = 1/3$

(ii)
$$2/\sqrt{x} + 3/\sqrt{y} = 2$$

$$4/\sqrt{x} + 9/\sqrt{y} = -1$$

Solution:

Substituting $1/\sqrt{x} = m$ and $1/\sqrt{y} = n$ in the given equations, we get

$$2m + 3n = 2$$
(i)

$$4m - 9n = -1$$
(ii)

Multiplying equation (i) by 3, we get

$$6m + 9n = 6$$
(iii)

Adding equation (ii) and (iii), we get

$$10m = 5$$

$$m = 1/2....(iv)$$

Now by putting the value of 'm' in equation (i), we get

$$2 \times 1/2 + 3n = 2$$

$$3n = 1$$

$$n = 1/3$$





$$\frac{1}{2} = \frac{1}{\sqrt{X}}$$

$$x = 4$$

$$n = 1/\sqrt{y}$$

$$1/3 = 1/\sqrt{y}$$

$$y = 9$$

Hence,
$$x = 4$$
 and $y = 9$

(iii)
$$4/x + 3y = 14$$

$$3/x - 4y = 23$$

Solution:

Putting in the given equation we get,

So,
$$4m + 3y = 14 = > 4m + 3y - 14 = 0$$
(1)

$$3m - 4y = 23$$
 => $3m - 4y - 23 = 0$ (2)

By cross-multiplication, we get,

$$m/(-69-56) = y/(-42-(-92)) = 1/(-16-9)$$

$$-m/125 = y/50 = -1/25$$

$$-m/125 = -1/25$$
 and $y/50 = -1/25$

$$m = 5$$
 and $b = -2$

$$m = 1/x = 5$$

So,
$$x = 1/5$$

$$y = -2$$

(iv)
$$5/(x-1) + 1/(y-2) = 2$$

$$6/(x-1) - 3/(y-2) = 1$$

Solution:

Substituting 1/(x-1) = m and 1/(y-2) = n in the given equations, we get,

$$5m + n = 2$$
(i)

$$6m - 3n = 1$$
(ii)

Multiplying equation (i) by 3, we get

$$15m + 3n = 6$$
(iii)

Adding (ii) and (iii) we get

$$21m = 7$$

$$m = 1/3$$

Putting this value in equation (i), we get



$$5 \times 1/3 + n = 2$$

$$n = 2 - 5/3 = 1/3$$

$$m = 1/(x-1)$$

$$\Rightarrow 1/3 = 1/(x-1)$$

$$\Rightarrow x = 4$$

$$n = 1/(y-2)$$

$$\Rightarrow 1/3 = 1/(y-2)$$

$$\Rightarrow$$
 y = 5

Hence,
$$x = 4$$
 and $y = 5$

$$(v) (7x-2y)/xy = 5$$

$$(8x + 7y)/xy = 15$$

Solution:

$$(7x-2y)/xy = 5$$

$$7/y - 2/x = 5$$
....(i)

$$(8x + 7y)/xy = 15$$

$$8/y + 7/x = 15...$$
 (ii)

Substituting 1/x = m in the given equation we get,

$$-2m + 7n = 5$$
 => $-2 + 7n - 5 = 0$ (iii)

$$7m + 8n = 15$$
 => $7m + 8n - 15 = 0$ (iv)

By cross-multiplication method, we get,

$$m/(-105-(-40)) = n/(-35-30) = 1/(-16-49)$$

$$m/(-65) = n/(-65) = 1/(-65)$$

$$m/-65 = 1/-65$$

$$m = 1$$

$$n/(-65) = 1/(-65)$$

$$n = 1$$

$$m = 1$$
 and $n = 1$

$$m = 1/x = 1$$
 $n = 1/x = 1$

Therefore,
$$x = 1$$
 and $y = 1$

$$(vi) 6x + 3y = 6xy$$

$$2x + 4y = 5xy$$

Solution:

$$6x + 3y = 6xy$$



$$6/y + 3/x = 6$$

Let
$$1/x = m$$
 and $1/y = n$

$$=>6n +3m = 6$$

$$=>3m + 6n-6 = 0....(i)$$

2x + 4y = 5xy

$$=> 2/y + 4/x = 5$$

$$=> 2n + 4m = 5$$

$$=> 4m+2n-5 = 0...$$
(ii)

$$3m + 6n - 6 = 0$$

$$4m + 2n - 5 = 0$$

By cross-multiplication method, we get

$$m/(-30 - (-12)) = n/(-24 - (-15)) = 1/(6-24)$$

$$m/-18 = n/-9 = 1/-18$$

$$m/-18 = 1/-18$$

$$m = 1$$

$$n/-9 = 1/-18$$

$$n = 1/2$$

$$m = 1$$
 and $n = 1/2$

$$m = 1/x = 1$$
 and $n = 1/y = 1/2$

$$x = 1$$
 and $y = 2$

Hence,
$$x = 1$$
 and $y = 2$

(vii)
$$10/(x+y) + 2/(x-y) = 4$$

$$15/(x+y) - 5/(x-y) = -2$$

Solution:

Substituting 1/x+y = m and 1/x-y = n in the given equations, we get,

$$10m + 2n = 4$$
 => $10m + 2n - 4 = 0$ (i)

$$15m - 5n = -2$$
 => $15m - 5n + 2 = 0$ (ii)

Using cross-multiplication method, we get,

$$m/(4-20) = n/(-60-(20)) = 1/(-50-30)$$

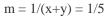
$$m/-16 = n/-80 = 1/-80$$

$$m/-16 = 1/-80$$
 and $n/-80 = 1/-80$

$$m = 1/5$$
 and $n = 1$



NCERT Solutions for Class 10 Chapter 3 – Linear Equations in Two Variables



$$x+y=5$$
(iii)

$$n = 1/(x-y) = 1$$

$$x-y = 1$$
....(iv)

Adding equation (iii) and (iv), we get

$$2x = 6 = x = 3 \dots (v)$$

Putting the value of x = 3 in equation (3), we get

$$y = 2$$

Hence, x = 3 and y = 2

(viii)
$$1/(3x+y) + 1/(3x-y) = 3/4$$

$$1/2(3x+y) - 1/2(3x-y) = -1/8$$

Solution:

Substituting 1/(3x+y) = m and 1/(3x-y) = n in the given equations, we get,

$$m + n = 3/4$$
(1)

$$m/2 - n/2 = -1/8$$

$$m - n = -1/4$$
(2)

Adding (1) and (2), we get

$$2m = 3/4 - 1/4$$

$$2m = 1/2$$

Putting in (2), we get

$$1/4 - n = -1/4$$

$$n = 1/4 + 1/4 = 1/2$$

$$m = 1/(3x+y) = 1/4$$

$$3x + y = 4$$
(3)

$$n = 1/(3x-y) = 1/2$$

$$3x - y = 2$$
(4)

Adding equations (3) and (4), we get

$$6x = 6$$

$$x = 1$$
(5)

Putting in (3), we get

$$3(1) + y = 4$$

$$y = 1$$

Hence,
$$x = 1$$
 and $y = 1$

NCERT Solutions for Class 10 Chapter 3 – Linear Equations in Two Variables

- 2. Formulate the following problems as a pair of equations, and hence find their solutions:
- (i) Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hours. Find her speed of rowing in still water and the speed of the current.
- (ii) 2 women and 5 men can together finish an embroidery work in 4 days, while 3 women and 6 men can finish it in 3 days. Find the time taken by 1 woman alone to finish the work, and also that taken by 1 man alone.
- (iii) Roohi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and the remaining by bus, she takes 10 minutes longer. Find the speed of the train and the bus separately.

Solutions:

bolutions.
(i) Let us consider,
Speed of Ritu in still water = $x \text{ km/hr}$
Speed of Stream = y km/hr
Now, speed of Ritu during,
Downstream = x + y km/h
Upstream = x - y km/h
As per the question given,
2(x+y) = 20
Or $x + y = 10$ (1)
And, $2(x-y) = 4$
Or $x - y = 2$ (2)
Adding both the eq.1 and 2, we get,
2x = 12
x = 6
Putting the value of x in eq.1, we get,
y = 4
Therefore,
Speed of Ritu rowing in still water = 6 km/hr
Speed of Stream = 4 km/hr
(ii) Let us consider,
Number of days taken by women to finish the work $= x$
Number of days taken by men to finish the work = y
Work done by women in one day = $1/x$
Work done by women in one day = $1/y$
As per the question given,

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$$4(2/x + 5/y) = 1$$

$$(2/x + 5/y) = 1/4$$

And,
$$3(3/x + 6/y) = 1$$

$$(3/x + 6/y) = 1/3$$

Now, put 1/x=m and 1/y=n, we get,

$$2m + 5n = 1/4 \implies 8m + 20n = 1$$
....(1)

$$3m + 6n = 1/3 = 9m + 18n = 1....(2)$$

Now, by cross multiplication method, we get here,

$$m/(20-18) = n/(9-8) = 1/(180-144)$$

$$m/2 = n/1 = 1/36$$

$$m/2 = 1/36$$

$$m = 1/18$$

$$m = 1/x = 1/18$$

or
$$x = 18$$

$$n = 1/y = 1/36$$

$$y = 36$$

Therefore,

Number of days taken by women to finish the work = 18

Number of days taken by men to finish the work = 36.

(iii) Let us consider,

Speed of the train = x km/h

Speed of the bus = y km/h

According to the given question,

$$60/x + 240/y = 4$$
(1)

$$100/x + 200/y = 25/6$$
(2)

Put 1/x=m and 1/y=n, in the above two equations;

$$60m + 240n = 4....(3)$$

$$100m + 200n = 25/6$$

$$600m + 1200n = 25$$
(4)

Multiply eq.3 by 10, to get,

$$600m + 2400n = 40$$
(5)

Now, subtract eq.4 from 5, to get,

$$1200n = 15$$



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n = 15/1200 = 1/80

Substitute the value of n in eq. 3, to get,

60m + 3 = 4

m = 1/60

m = 1/x = 1/60

x = 60

And y = 1/n

y = 80

Therefore,

Speed of the train = 60 km/h

Speed of the bus = 80 km/h