

EXERCISE 11.1

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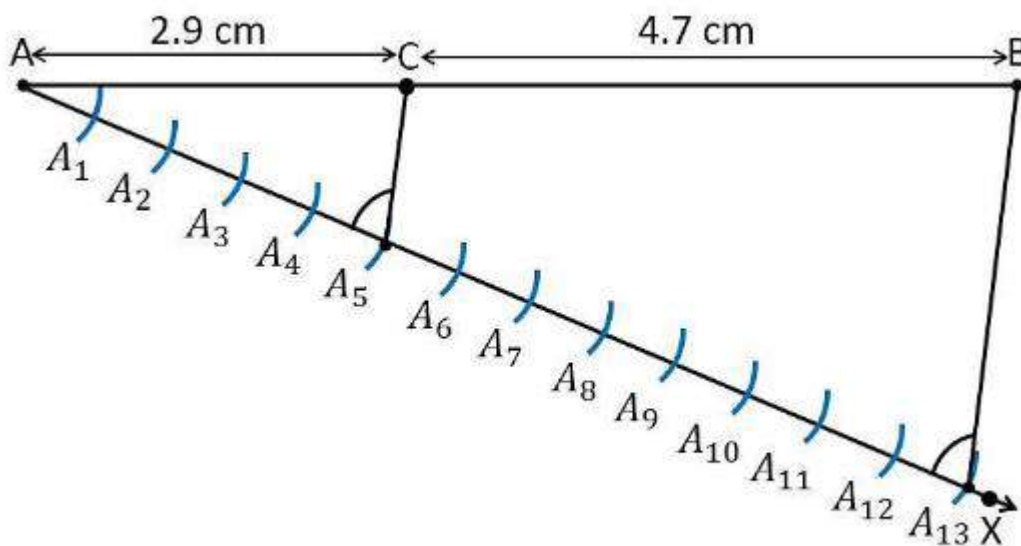
In each of the following, give the justification for the construction also.

1. Draw a line segment of length 7.6 cm and divide it in the ratio 5:8. Measure the two parts.

Construction Procedure

A line segment with a measure of 7.6 cm length is divided in the ratio of 5:8 as follows.

1. Draw line segment AB with a length measure of 7.6 cm.
2. Draw a ray AX that makes an acute angle with line segment AB.
3. Locate the points, i.e., 13 (= 5+8) points, such as A₁, A₂, A₃, A₄ A₁₃, on the ray AX, such that it becomes AA₁ = A₁A₂ = A₂A₃ and so on.
4. Join the line segment and the ray, BA₁₃.
5. Through the point A₅, draw a line parallel to BA₁₃ which makes an angle equal to ∠AA₁₃B.
6. Point A₅, which intersects line AB at point C.
7. C is the point that divides line segment AB of 7.6 cm in the required ratio of 5:8.
8. Now, measure the lengths of the line AC and CB. It becomes the measure of 2.9 cm and 4.7 cm, respectively.



Justification:

The construction of the given problem can be justified by proving that

$$AC/CB = 5/8$$

By construction, we have A₅C || A₁₃B. From the Basic proportionality theorem for the triangle AA₁₃B, we get

$$AC/CB = AA_5/A_5A_{13} \dots (1)$$

From the figure constructed, it is observed that AA_5 and A_5A_{13} contain 5 and 8 equal divisions of line segments, respectively.

Therefore, it becomes

$$AA_5/A_5A_{13} = 5/8 \dots (2)$$

Compare the equations (1) and (2), we obtain

$$AC/CB = 5/8$$

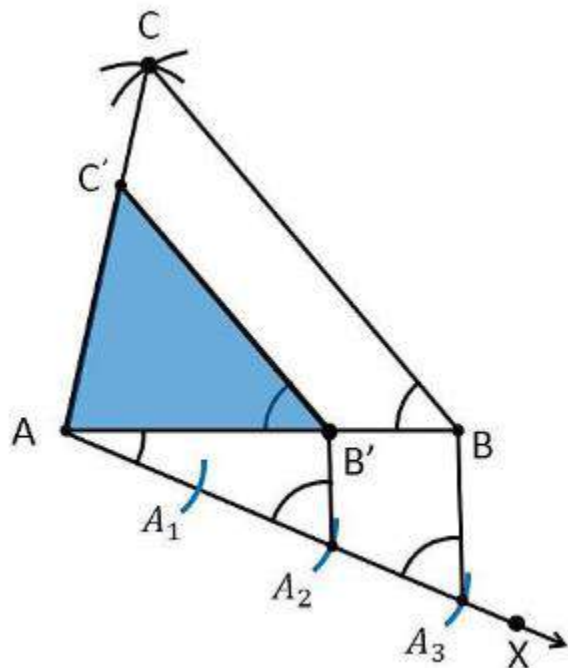
Hence, justified.

2. Construct a triangle of sides 4 cm, 5 cm and 6 cm and then a triangle similar to it whose sides are $2/3$ of the corresponding sides of the first triangle.

Construction Procedure

1. Draw a line segment AB which measures 4 cm, i.e., $AB = 4$ cm.
2. Take point A as the centre, and draw an arc of radius 5 cm.
3. Similarly, take point B as its centre, and draw an arc of radius 6 cm.
4. The arcs drawn will intersect each other at point C.
5. Now, we have obtained $AC = 5$ cm and $BC = 6$ cm, and therefore, $\triangle ABC$ is the required triangle.
6. Draw a ray AX which makes an acute angle with the line segment AB on the opposite side of vertex C.
7. Locate 3 points such as A_1 , A_2 , and A_3 (as 3 is greater between 2 and 3) on line AX such that it becomes $AA_1 = A_1A_2 = A_2A_3$.
8. Join point BA_3 and draw a line through A_2 , which is parallel to the line BA_3 that intersects AB at point B' .
9. Through the point B' , draw a line parallel to line BC that intersects the line AC at C' .
10. Therefore, $\triangle AB'C'$ is the required triangle.





Justification

The construction of the given problem can be justified by proving that

$$AB' = \frac{2}{3}AB$$

$$B'C' = \frac{2}{3}BC$$

$$AC' = \frac{2}{3}AC$$

From the construction, we get $B'C' \parallel BC$

$$\therefore \angle AB'C' = \angle ABC \text{ (Corresponding angles)}$$

In $\triangle AB'C'$ and $\triangle ABC$,

$$\angle ABC = \angle AB'C' \text{ (Proved above)}$$

$$\angle BAC = \angle B'AC' \text{ (Common)}$$

$$\therefore \triangle AB'C' \sim \triangle ABC \text{ (From AA similarity criterion)}$$

$$\text{Therefore, } AB'/AB = B'C'/BC = AC'/AC \dots (1)$$

In $\triangle AA_2B'$ and $\triangle AA_3B$,

$$\angle A_2AB' = \angle A_3AB \text{ (Common)}$$

From the corresponding angles, we get

$$\angle AA_2B' = \angle AA_3B$$

Therefore, from the AA similarity criterion, we obtain

$$\triangle AA_2B' \text{ and } \triangle AA_3B$$

$$\text{So, } AB'/AB = AA_2/AA_3$$

Therefore, $AB'/AB = 2/3 \dots\dots (2)$

From equations (1) and (2), we get

$$AB'/AB = B'C'/BC = AC'/AC = 2/3$$

This can be written as

$$AB' = (2/3)AB$$

$$B'C' = (2/3)BC$$

$$AC' = (2/3)AC$$

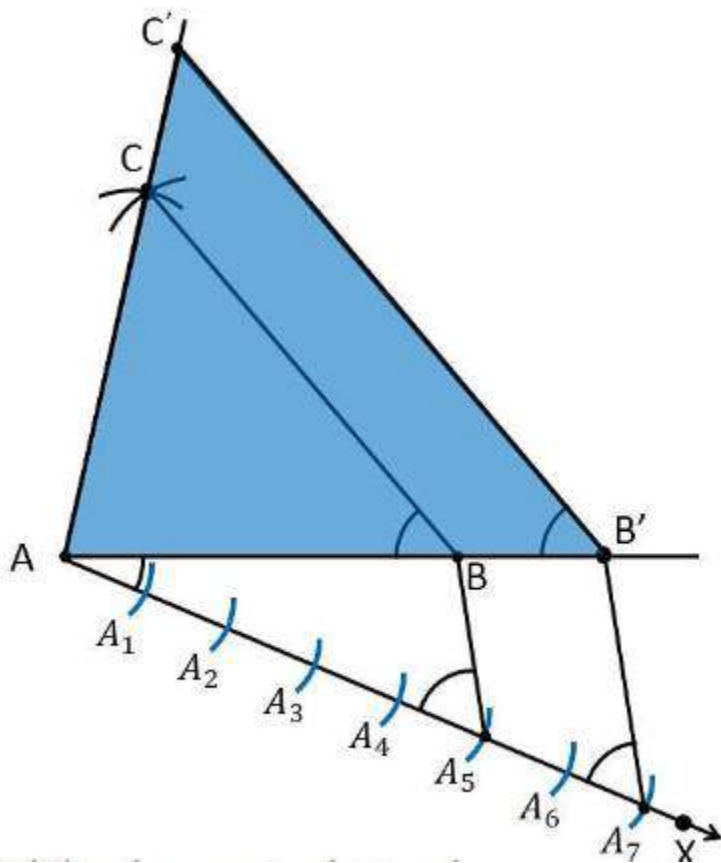
Hence, justified.

3. Construct a triangle with sides 5 cm, 6 cm and 7 cm and then another triangle whose sides are $7/5$ of the corresponding sides of the first triangle

Construction Procedure

1. Draw a line segment $AB = 5$ cm.
2. Take A and B as the centre, and draw the arcs of radius 6 cm and 7 cm, respectively.
3. These arcs will intersect each other at point C, and therefore, $\triangle ABC$ is the required triangle with the length of sides as 5 cm, 6 cm, and 7 cm, respectively.
4. Draw a ray AX which makes an acute angle with the line segment AB on the opposite side of vertex C.
5. Locate the 7 points, such as $A_1, A_2, A_3, A_4, A_5, A_6, A_7$ (as 7 is greater between 5 and 7), on line AX such that it becomes $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_6A_7$
6. Join the points BA_5 and draw a line from A_7 to BA_5 , which is parallel to the line BA_5 where it intersects the extended line segment AB at point B'.
7. Now, draw a line from B' to the extended line segment AC at C', which is parallel to the line BC, and it intersects to make a triangle.
8. Therefore, $\triangle AB'C'$ is the required triangle.





Justification

The construction of the given problem can be justified by proving that

$$AB' = (7/5)AB$$

$$B'C' = (7/5)BC$$

$$AC' = (7/5)AC$$

From the construction, we get $B'C' \parallel BC$

$$\therefore \angle AB'C' = \angle ABC \text{ (Corresponding angles)}$$

In $\triangle AB'C'$ and $\triangle ABC$,

$$\angle ABC = \angle AB'C' \text{ (Proved above)}$$

$$\angle BAC = \angle B'AC' \text{ (Common)}$$

$$\therefore \triangle AB'C' \sim \triangle ABC \text{ (From AA similarity criterion)}$$

$$\text{Therefore, } AB'/AB = B'C'/BC = AC'/AC \dots (1)$$

In $\triangle AA_7B'$ and $\triangle AA_5B$,

$$\angle A_7AB' = \angle A_5AB \text{ (Common)}$$

From the corresponding angles, we get

$$\angle A A_7 B' = \angle A A_5 B$$

Therefore, from the AA similarity criterion, we obtain

$$\Delta A A_2 B' \text{ and } \Delta A A_3 B$$

$$\text{So, } AB'/AB = AA_5/AA_7$$

$$\text{Therefore, } AB/AB' = 5/7 \dots\dots (2)$$

From equations (1) and (2), we get

$$AB'/AB = B'C'/BC = AC'/AC = 7/5$$

This can be written as

$$AB' = (7/5)AB$$

$$B'C' = (7/5)BC$$

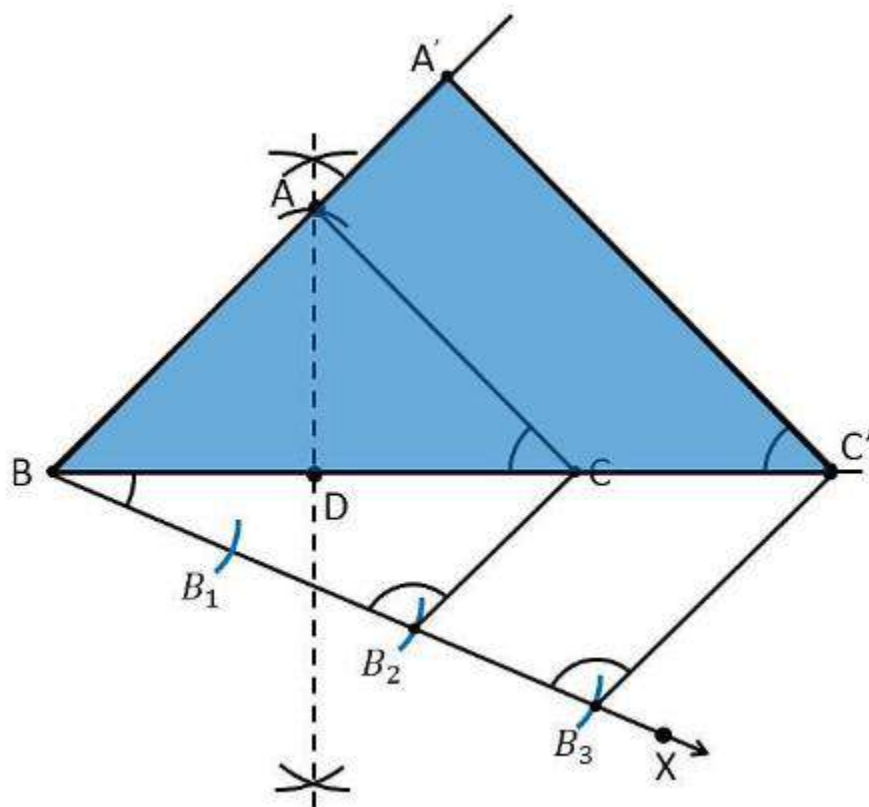
$$AC' = (7/5)AC$$

Hence, justified.

4. Construct an isosceles triangle whose base is 8 cm and altitude 4 cm and then another triangle whose sides are $1\frac{1}{2}$ times the corresponding sides of the isosceles triangle

Construction Procedure:

1. Draw a line segment BC with a measure of 8 cm.
2. Now, draw the perpendicular bisector of the line segment BC and intersect at point D.
3. Take the point D as the centre and draw an arc with a radius of 4 cm, which intersects the perpendicular bisector at the point A.
4. Now, join the lines AB and AC, and the triangle is the required triangle.
5. Draw a ray BX which makes an acute angle with the line BC on the side opposite to the vertex A.
6. Locate the 3 points B₁, B₂ and B₃ on the ray BX such that BB₁ = B₁B₂ = B₂B₃
7. Join the points B₂C and draw a line from B₃, which is parallel to the line B₂C where it intersects the extended line segment BC at point C'.
8. Now, draw a line from C' to the extended line segment AC at A', which is parallel to the line AC, and it intersects to make a triangle.
9. Therefore, $\Delta A'BC'$ is the required triangle.



Justification

The construction of the given problem can be justified by proving that

$$A'B = (3/2)AB$$

$$BC' = (3/2)BC$$

$$A'C' = (3/2)AC$$

From the construction, we get $A'C' \parallel AC$

$$\therefore \angle A'C'B = \angle ACB \text{ (Corresponding angles)}$$

In $\triangle A'BC'$ and $\triangle ABC$,

$$\angle B = \angle B \text{ (Common)}$$

$$\angle A'BC' = \angle ACB$$

$$\therefore \triangle A'BC' \sim \triangle ABC \text{ (From AA similarity criterion)}$$

$$\text{Therefore, } A'B/AB = BC'/BC = A'C'/AC$$

Since the corresponding sides of the similar triangle are in the same ratio, it becomes

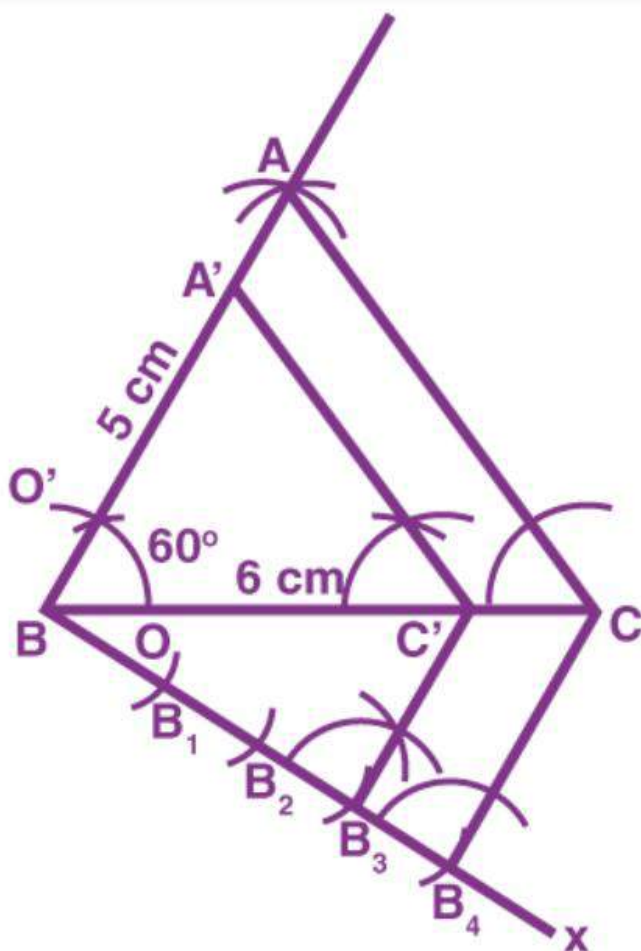
$$A'B/AB = BC'/BC = A'C'/AC = 3/2$$

Hence, justified.

5. Draw a triangle ABC with side BC = 6 cm, AB = 5 cm and $\angle ABC = 60^\circ$. Then construct a triangle whose sides are $3/4$ of the corresponding sides of the triangle ABC.

Construction Procedure

1. Draw a $\triangle ABC$ with base side $BC = 6$ cm, and $AB = 5$ cm and $\angle ABC = 60^\circ$.
2. Draw a ray BX which makes an acute angle with BC on the opposite side of vertex A .
3. Locate 4 points (as 4 is greater in 3 and 4), such as B_1, B_2, B_3, B_4 , on line segment BX .
4. Join the points B_4C and also draw a line through B_3 , parallel to B_4C intersecting the line segment BC at C' .
5. Draw a line through C' parallel to the line AC , which intersects the line AB at A' .
6. Therefore, $\triangle A'BC'$ is the required triangle.



Justification

The construction of the given problem can be justified by proving that

Since the scale factor is $\frac{3}{4}$, we need to prove

$$A'B = \left(\frac{3}{4}\right)AB$$

$$BC' = \left(\frac{3}{4}\right)BC$$

$$A'C' = \left(\frac{3}{4}\right)AC$$

From the construction, we get $A'C' \parallel AC$

In $\Delta A'BC'$ and ΔABC ,

$\therefore \angle A'C'B = \angle ACB$ (Corresponding angles)

$\angle B = \angle B$ (Common)

$\therefore \Delta A'BC' \sim \Delta ABC$ (From AA similarity criterion)

Since the corresponding sides of the similar triangle are in the same ratio, it becomes

Therefore, $A'B/AB = BC'/BC = A'C'/AC$

So, it becomes $A'B/AB = BC'/BC = A'C'/AC = 3/4$

Hence, justified.

6. Draw a triangle ABC with side BC = 7 cm, $\angle B = 45^\circ$, $\angle A = 105^\circ$. Then, construct a triangle whose sides are $4/3$ times the corresponding sides of ΔABC .

To find $\angle C$:

Given:

$\angle B = 45^\circ$, $\angle A = 105^\circ$

We know that,

The sum of all interior angles in a triangle is 180° .

$\angle A + \angle B + \angle C = 180^\circ$

$105^\circ + 45^\circ + \angle C = 180^\circ$

$\angle C = 180^\circ - 150^\circ$

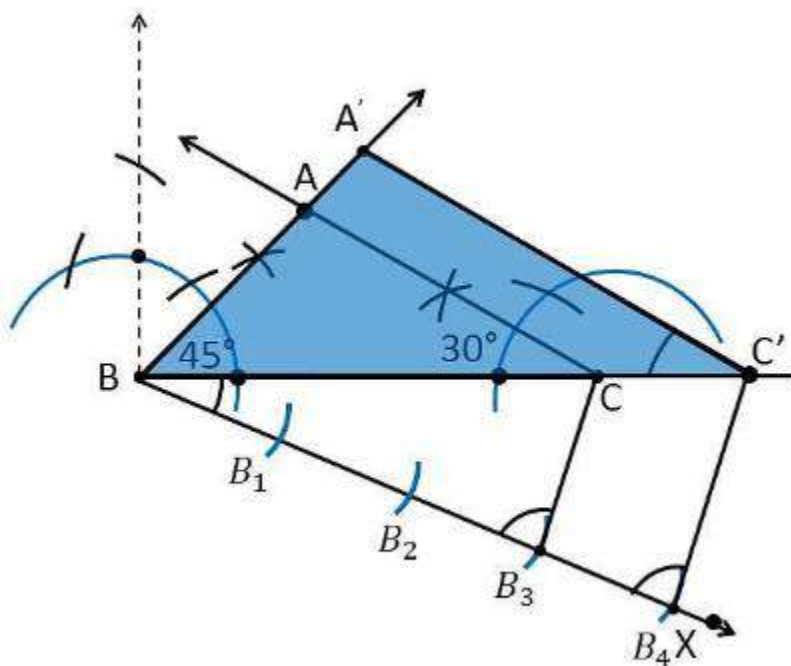
$\angle C = 30^\circ$

So, from the property of the triangle, we get $\angle C = 30^\circ$

Construction Procedure

The required triangle can be drawn as follows.

1. Draw a ΔABC with side measures of base $BC = 7$ cm, $\angle B = 45^\circ$, and $\angle C = 30^\circ$.
2. Draw a ray BX that makes an acute angle with BC on the opposite side of vertex A .
3. Locate 4 points (as 4 is greater in 4 and 3), such as B_1, B_2, B_3, B_4 , on the ray BX .
4. Join the points B_3C .
5. Draw a line through B_4 parallel to B_3C , which intersects the extended line BC at C' .
6. Through C' , draw a line parallel to the line AC that intersects the extended line segment at A' .
7. Therefore, $\Delta A'BC'$ is the required triangle.



Justification

The construction of the given problem can be justified by proving that

Since the scale factor is $\frac{4}{3}$, we need to prove

$$A'B = \left(\frac{4}{3}\right)AB$$

$$BC' = \left(\frac{4}{3}\right)BC$$

$$A'C' = \left(\frac{4}{3}\right)AC$$

From the construction, we get $A'C' \parallel AC$

In $\triangle A'BC'$ and $\triangle ABC$,

$$\therefore \angle A'C'B = \angle ACB \text{ (Corresponding angles)}$$

$$\angle B = \angle B \text{ (Common)}$$

$$\therefore \triangle A'BC' \sim \triangle ABC \text{ (From AA similarity criterion)}$$

Since the corresponding sides of the similar triangle are in the same ratio, it becomes

$$\text{Therefore, } \frac{A'B}{AB} = \frac{BC'}{BC} = \frac{A'C'}{AC}$$

$$\text{So, it becomes } \frac{A'B}{AB} = \frac{BC'}{BC} = \frac{A'C'}{AC} = \frac{4}{3}$$

Hence, justified.

7. Draw a right triangle in which the sides (other than hypotenuse) are of lengths 4 cm and 3 cm. Then construct another triangle whose sides are $\frac{5}{3}$ times the corresponding sides of the given triangle.

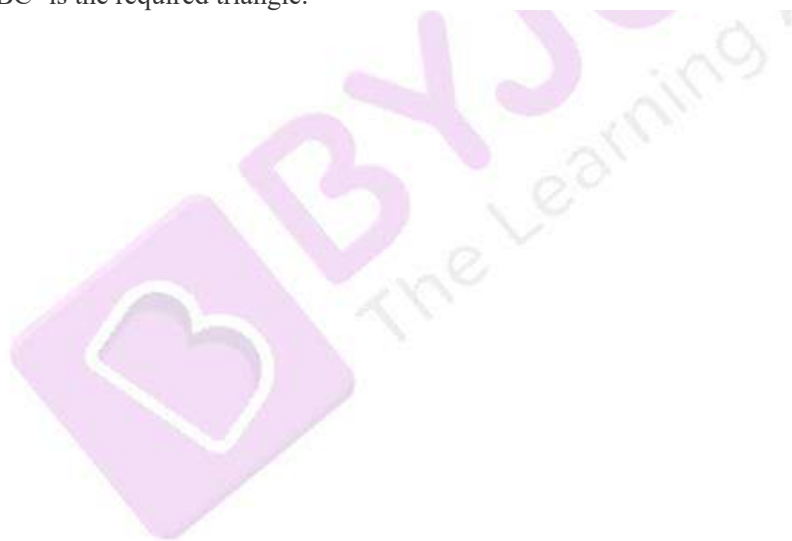
Given:

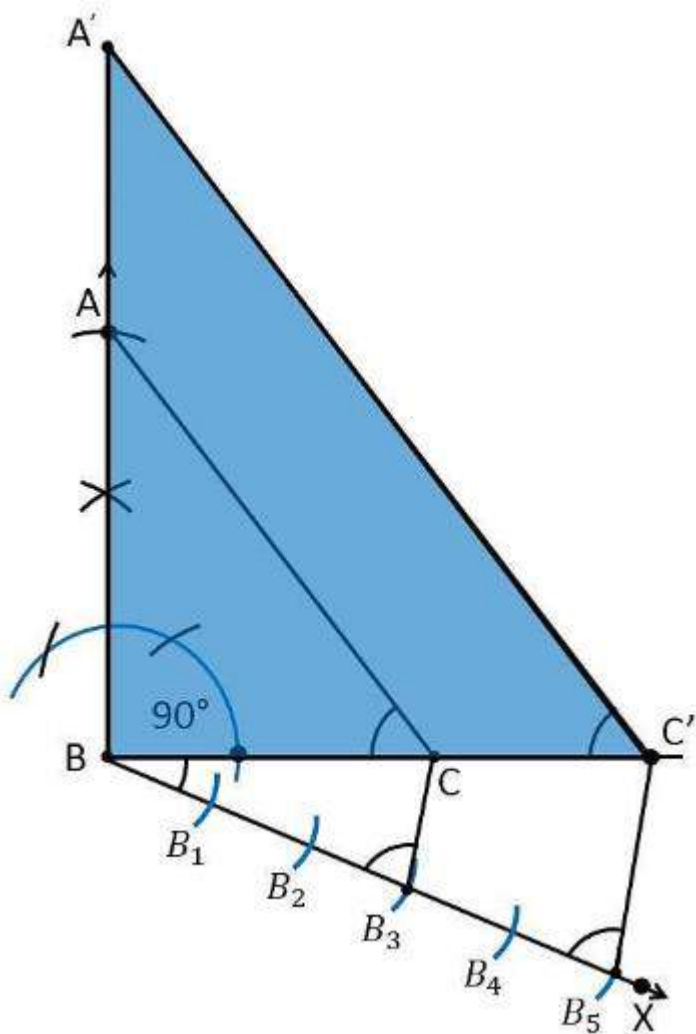
The sides other than the hypotenuse are of lengths 4cm and 3cm. It defines that the sides are perpendicular to each other

Construction Procedure

The required triangle can be drawn as follows.

1. Draw a line segment $BC = 3$ cm.
2. Now, measure and draw an angle 90°
3. Take B as the centre and draw an arc with a radius of 4 cm, and intersects the ray at point B.
4. Now, join the lines AC, and the triangle ABC is the required triangle.
5. Draw a ray BX that makes an acute angle with BC on the opposite side of vertex A.
6. Locate 5 such as B_1, B_2, B_3, B_4 , on the ray BX, such that $BB_1 = B_1B_2 = B_2B_3 = B_3B_4 = B_4B_5$
7. Join the points B_3C .
8. Draw a line through B_5 parallel to B_3C , which intersects the extended line BC at C' .
9. Through C' , draw a line parallel to the line AC that intersects the extended line AB at A' .
10. Therefore, $\triangle A'BC'$ is the required triangle.





Justification

The construction of the given problem can be justified by proving that

Since the scale factor is $\frac{5}{3}$, we need to prove

$$A'B = \left(\frac{5}{3}\right)AB$$

$$BC' = \left(\frac{5}{3}\right)BC$$

$$A'C' = \left(\frac{5}{3}\right)AC$$

From the construction, we get $A'C' \parallel AC$

In $\triangle A'BC'$ and $\triangle ABC$,

$$\therefore \angle A'C'B = \angle ACB \text{ (Corresponding angles)}$$

$$\angle B = \angle B \text{ (Common)}$$

$$\therefore \triangle A'BC' \sim \triangle ABC \text{ (From AA similarity criterion)}$$

Since the corresponding sides of the similar triangle are in the same ratio, it becomes

Therefore, $A'B/AB = BC'/BC = A'C'/AC$

So, it becomes $A'B/AB = BC'/BC = A'C'/AC = 5/3$

Hence, justified.