

EXERCISE 12.1

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1. Evaluate:

Solution:

(i)
$$3^{-2} = (1/3)^2$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/9$$

(ii)
$$(-4)^{-2} = (1/-4)^2$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/16$$

(iii)
$$(1/2)^{-5} = (2/1)^5$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

$$= 2^{5}$$

$$= 32$$

${\bf 2. \ Simplify \ and \ express \ the \ result \ in \ power \ notation \ with \ a \ positive \ exponent:}$

(i)
$$(-4)^4 \div (-4)^8$$

(ii)
$$(1/2^3)^2$$

(iii)
$$-(3)^4 \times (5/3)^4$$

(iv)
$$(3^{-7} \div 3^{-10}) \times 3^{-5}$$

(v)
$$2^{-3} \times (-7)^{-3}$$

Solution:

$$(1)$$

$$(-4)^5 \div (-4)^8$$

$$= (-4)^5/(-4)^8$$

$$\left[\because a^m \div a^n = a^{m-n} \right]$$

$$= (-4)^{5-8}$$

$$= 1/(-4)^3$$

$$= 1^2/(2^3)^2$$

$$\left[\because \left(\frac{a}{b} \right)^m = \frac{a^m}{a^n} \right]$$

$$= 1/2^{3\times 2} = 1/2^6$$

$$\left[\because \left(a^m \right)^n = a^{m \times n} \right]$$

$$(-3)^4 \times \left(\frac{5}{3}\right)^4 = (-3)^4 \times \frac{5^4}{3^4}$$

$$\left[\because \left(\frac{a}{b} \right)^m = \frac{a^m}{a^n} \right]$$

$$= (-1)^4 \times 3^4 \times (5^4/3^4)$$

$$\left[\because (ab)^m = a^m b^m \right]$$

$$=3^{(4-4)}\times5^4$$

$$\left[\because a^m \div a^n = a^{m-n} \right]$$

$$= 3^{0} \times 5^{4} = 5^{4}$$

$$\begin{bmatrix} \because & a^0 = 1 \end{bmatrix}$$

(iv)
$$(3^{-7} \div 3^{-10}) \times 3^{-5}$$

$$= (3^{-7}/3^{-10}) \times 3^{-5}$$

$$= 3^{-7-(-10)} \times 3^{-5}$$

$$\left[\begin{array}{cc} \cdots & a^m \div a^n = a^{m-n} \end{array} \right]$$

$$=3^{(-7+10)}\times3^{-5}$$

$$= 3^3 \times 3^{-5}$$

$$=3^{(3+-5)}$$

$$\left[: a^m \times a^n = a^{m+n} \right]$$

$$= 3^{-2}$$

$$=1/3^{2}$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

(v)
$$2^{-3} \times (-7)^{-3}$$

$$=(2\times -7)^{-3}$$

(Because
$$a^m \times b^m = (ab)^m$$
)

$$= 1/(2 \times -7)^3$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/(-14)^3$$

3. Find the value of:

(i)
$$(3^0+4^{-1})\times 2^2$$

(ii)
$$(2^{-1} \times 4^{-1}) \div 2^{-2}$$

(iii)
$$(1/2)^{-2}+(1/3)^{-2}+(1/4)^{-2}$$

(iv)
$$(3^{-1}+4^{-1}+5^{-1})^0$$

(v)
$$\{(-2/3)^{-2}\}^2$$

Solution:

$$(i)(3^0+4^{-1})\times 2^2 = (1+(1/4))\times 2^2$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

 $=((4+1)/4)\times 2^2$

 $= (5/4) \times 2^2$

 $=(5/2^2)\times 2^2$

 $=5\times2^{(2-2)}$

 $\left[\because a^m \div a^n = a^{m-n} \right]$

 $= 5 \times 2^{\circ}$

 $= 5 \times 1 = 5$

 $\left[\because a^{-m} = \frac{1}{a^m} \right]$

 $(ii)(2^{-1}\times 4^{-1})\div 2^{-2}$

 $= [(1/2) \times (1/4)] \div (1/4)$

 $\left[\because a^{-m} = \frac{1}{a^m} \right]$

 $= (1/2 \times 1/2^2) \div 1/4$

 $= 1/2^3 \div 1/4$

 $= (1/8) \times (4)$

= 1/2

(iii) (1/2)-2+(1/3)-2+(1/4)-2

 $= (2^{-1})^{-2} + (3^{-1})^{-2} + (4^{-1})^{-2}$

 $\left[\because a^{-m} = \frac{1}{a^m} \right]$

 $= 2^{(-1\times-2)} + 3^{(-1\times-2)} + 4^{(-1\times-2)}$

 $\left[\begin{array}{cc} \ddots & \left(a^m \right)^n = a^{m \times n} \end{array} \right]$

 $= 2^2 + 3^2 + 4^2$

=4+9+16

=29

(iv)
$$(3^{-1}+4^{-1}+5^{-1})^0$$

= 1

$$\begin{bmatrix} \because a^0 = 1 \end{bmatrix}$$

(v)
$$\{(-2/3)^{-2}\}^2 = (-2/3)^{-2\times 2}$$

$$\left[\because \left(a^m \right)^n = a^{m \times n} \right]$$

$$=(-2/3)^{-4}$$

$$=(-3/2)^4$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

$$= 81/16$$

4. Evaluate:

(i)
$$(8^{-1} \times 5^3)/2^{-4}$$

(ii)
$$(5^{-1}\times 2^{-2})\times 6^{-1}$$

Solution:

(i)
$$(8^{-1} \times 5^3)/2^{-4}$$

$$\frac{8^{-1} \times 5^{3}}{2^{-4}} = \frac{\left(2^{3}\right)^{-1} \times 5^{3}}{2^{-4}} = \frac{2^{-3} \times 5^{3}}{2^{-4}}$$

$$\left[\because \left(a^{m}\right)^{n} = a^{m \times n} \right]$$

=

$$2^{-3-(-4)} \times 5^{3} = 2^{-3+4} \times 5^{3}$$

$$[\because a^{m} \div a^{n} = a^{m-n}]$$

$$= 2 \times 125 = 250$$

(ii)
$$(5^{-1} \times 2^{-2}) \times 6^{-1}$$

$$(5^{-1} \times 2^{-1}) \times 6^{-1} = (\frac{1}{5} \times \frac{1}{2}) \times \frac{1}{6}$$

$$\left[\begin{array}{cc} \cdots & a^{-m} = \frac{1}{a^m} \end{array} \right]$$

$$=(1/10)\times1/6$$

$$= 1/60$$

5. Find the value of m for which $5^m \div 5^{-3} = 5^5$

Solution:

$$5^m \div 5^{-3} = 5^5$$

$$5^{\text{(m-(-3))}} = 5^5$$

$$\left[\because a^m \div a^n = a^{m-n} \right]$$

$$5^{m+3} = 5^5$$

Comparing exponents on both sides, we get

$$m+3 = 5$$

$$m = 5-3$$

$$m = 2$$

6. Evaluate:

(i)

$$\left\{ \left(\frac{1}{3}\right)^{-1} - \left(\frac{1}{4}\right)^{-1} \right\}^{-1}$$

(ii)

$$\left(\frac{5}{8}\right)^{-7} \times \left(\frac{8}{5}\right)^{-4}$$

Solution:

(i)



$$\left\{ \left(\frac{1}{3}\right)^{-1} - \left(\frac{1}{4}\right)^{-1} \right\} = \left\{ \left(\frac{3}{1}\right)^{1} - \left(\frac{4}{1}\right)^{1} \right\}$$

$$\left[\because a^{-m} = \frac{1}{a^{m}} \right]$$

$$\left(\frac{5}{8}\right)^{-7} \times \left(\frac{8}{5}\right)^{-4} = \frac{5^{-7}}{8^{-7}} \times \frac{8^{-4}}{5^{-4}}$$

$$\left[\because \left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}\right]$$

$$5^{-7-(-4)} \times 8^{-4-(-7)}$$

$$\left[\because \ a^m \div a^n = a^{m-n} \right]$$

$$=$$
 $5^{-7+4} \times 8^{-4+7}$

$$=5^{-3}\times8^3$$

$$\frac{8^3}{5^3}$$

$$\left[\because a^{-m} = \frac{1}{a^m} \right]$$

7. Simplify the following:

(i)

$$\frac{25 \times t^{-4}}{5^{-3} \times 10 \times t^{-8}} \quad (t \neq 0)$$

(ii)

$$\frac{3^{-5} \times 10^{-5} \times 125}{5^{-7} \times 6^{-5}}$$

Solution:

(i)

$$\frac{25 \times t^{-4}}{5^{-3} \times 10 \times t^{-8}}$$

$$=\frac{5^2 \times t^{-4}}{5^{-3} \times 5 \times 2 \times t^{-8}}$$

$$=\frac{5^{2-(-3)-1}\times t^{-4-(-8)}}{2}$$

$$\left[\because a^m \div a^n = a^{m-n} \right]$$

$$\frac{5^{2+3-1} \times t^{-4+8}}{2} = \frac{5^4 \times t^4}{2} = 625_{4}$$

$$\frac{625}{2}t^4$$

(ii)

$$\frac{3^{-5} \times 10^{-5} \times 125}{5^{-7} \times 6^{-5}}$$

$$=\frac{3^{-5}\times (2\times 5)^{-5}\times 5^{3}}{5^{-7}\times (2\times 3)^{-5}}$$

$$=\frac{3^{-5}\times 2^{-5}\times 5^{-5}\times 5^{3}}{5^{-7}\times 2^{-5}\times 3^{-5}}$$

$$\left[\because (ab)^m = a^m b^m \right]$$

$$\frac{2^{-5} \times 2^{-5} \times 5^{-5+3}}{5^{-7} \times 2^{-5} \times 3^{-5}} = \frac{3^{-5} \times 2^{-5} \times 5^{-2}}{5^{-7} \times 2^{-5} \times 3^{-5}}$$

$$\left[\because a^m \times a^n = a^{m+n} \right]$$

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=

$$3^{-5-(-5)} \times 2^{-5-(-5)} \times 5^{-2-(-7)}$$

$$[:: a^m \div a^n = a^{m-n}]$$

=

$$\begin{array}{l} -\\ 3^{-5+5} \times 2^{-5+5} \times 5^{-2+7} = \\ 3^{0} \times 2^{0} \times 5^{5} \end{array}$$

$$= 1 \times 1 \times 3125$$

$$\begin{bmatrix} \because & a^0 = 1 \end{bmatrix}$$