

# **EXERCISE 12.1**

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# 1. Evaluate:

# **Solution:**

(i) 
$$3^{-2} = (1/3)^2$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/9$$

(ii) 
$$(-4)^{-2} = (1/-4)^2$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/16$$

(iii) 
$$(1/2)^{-5} = (2/1)^5$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 2^{5}$$

$$= 32$$

# $\ensuremath{\textbf{2.}}\ \mbox{Simplify and express the result in power notation with a positive exponent:}$

(i) 
$$(-4)^4 \div (-4)^8$$

(ii) 
$$(1/2^3)^2$$

(iii) 
$$-(3)^4 \times (5/3)^4$$

(iv) 
$$(3^{-7} \div 3^{-10}) \times 3^{-5}$$

(v) 
$$2^{-3} \times (-7)^{-3}$$

# **Solution:**

$$(i) (-4)^5 \div (-4)^8$$

 $= (-4)^5/(-4)^8$ 

$$\left[ \because \ a^m \div a^n = a^{m-n} \right]$$

$$=(-4)^{5-8}$$

$$= 1/(-4)^3$$

$$= 1^2/(2^3)^2$$

$$\left[ \because \left( \frac{a}{b} \right)^m = \frac{a^m}{a^n} \right]$$

$$= 1/2^{3\times 2} = 1/2^6$$

$$\left[ \because \left( a^m \right)^n = a^{m \times n} \right]$$

(iii) -(3)4×(5/3)4

$$(-3)^4 \times \left(\frac{5}{3}\right)^4 = (-3)^4 \times \frac{5^4}{3^4}$$

$$\left[ \because \left( \frac{a}{b} \right)^m = \frac{a^m}{a^n} \right]$$

$$= (-1)^4 \times 3^4 \times (5^4/3^4)$$

$$\left[ \because \left( ab \right)^m = a^m b^m \right]$$

$$=3^{(4-4)}\times5^4$$

$$\left[ \because a^m \div a^n = a^{m-n} \right]$$

$$=3^{0}\times5^{4}=5^{4}$$

$$\left[ \because a^0 = 1 \right]$$

(iv) 
$$(3^{-7} \div 3^{-10}) \times 3^{-5}$$

$$= (3^{-7}/3^{-10}) \times 3^{-5}$$

$$=3^{-7-(-10)}\times3^{-5}$$

$$\left[ \because a^m \div a^n = a^{m-n} \right]$$

$$=3^{(-7+10)}\times3^{-5}$$

$$= 3^3 \times 3^{-5}$$

$$=3^{(3+-5)}$$

$$\left[ : a^m \times a^n = a^{m+n} \right]$$

$$= 3^{-2}$$

$$=1/3^{2}$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

(v) 
$$2^{-3} \times (-7)^{-3}$$

$$=(2\times -7)^{-3}$$

(Because 
$$a^m \times b^m = (ab)^m$$
)

$$= 1/(2 \times -7)^3$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 1/(-14)^3$$

# 3. Find the value of:

(i) 
$$(3^0+4^{-1})\times 2^2$$

(ii) 
$$(2^{-1} \times 4^{-1}) \div 2^{-2}$$

(iii) 
$$(1/2)^{-2}+(1/3)^{-2}+(1/4)^{-2}$$

(iv) 
$$(3^{-1}+4^{-1}+5^{-1})^0$$

(v) 
$$\{(-2/3)^{-2}\}^2$$

# **Solution:**

$$(i)(3^0+4^{-1})\times 2^2 = (1+(1/4))\times 2^2$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

 $=((4+1)/4)\times 2^2$ 

 $= (5/4) \times 2^2$ 

 $=(5/2^2)\times 2^2$ 

 $=5\times2^{(2-2)}$ 

 $\left[ \because a^m \div a^n = a^{m-n} \right]$ 

 $= 5 \times 2^{\circ}$ 

 $= 5 \times 1 = 5$ 

 $\left[ \because a^{-m} = \frac{1}{a^m} \right]$ 

 $(ii)(2^{-1}\times 4^{-1})\div 2^{-2}$ 

 $= [(1/2) \times (1/4)] \div (1/4)$ 

 $\left[ \because a^{-m} = \frac{1}{a^m} \right]$ 

 $= (1/2 \times 1/2^2) \div 1/4$ 

 $= 1/2^3 \div 1/4$ 

 $= (1/8) \times (4)$ 

= 1/2

(iii) (1/2)-2+(1/3)-2+(1/4)-2

 $= (2^{-1})^{-2} + (3^{-1})^{-2} + (4^{-1})^{-2}$ 

 $\left[ \because a^{-m} = \frac{1}{a^m} \right]$ 

 $= 2^{(-1\times-2)} + 3^{(-1\times-2)} + 4^{(-1\times-2)}$ 

 $\left[ \because \left( a^m \right)^n = a^{m \times n} \right]$ 

 $= 2^2 + 3^2 + 4^2$ 

=4+9+16

=29

(iv) 
$$(3^{-1}+4^{-1}+5^{-1})^0$$

= 1

$$\left[ \because a^{0} = 1 \right]$$

(v) 
$$\{(-2/3)^{-2}\}^2 = (-2/3)^{-2\times 2}$$

$$\left[ \because \left( a^m \right)^n = a^{m \times n} \right]$$

$$=(-2/3)^{-4}$$

$$=(-3/2)^4$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 81/16$$

#### 4. Evaluate:

(i) 
$$(8^{-1} \times 5^3)/2^{-4}$$

(ii) 
$$(5^{-1}\times 2^{-2})\times 6^{-1}$$

# **Solution:**

(i)  $(8^{-1} \times 5^3)/2^{-4}$ 

$$\frac{8^{-1} \times 5^{3}}{2^{-4}} = \frac{\left(2^{3}\right)^{-1} \times 5^{3}}{2^{-4}} = \frac{2^{-3} \times 5^{3}}{2^{-4}}$$

$$\left[ \because \left(a^{m}\right)^{n} = a^{m \times n} \right]$$

=

$$2^{-3-(-4)} \times 5^{3} = 2^{-3+4} \times 5^{3}$$

$$[ : a^{m} \div a^{n} = a^{m-n} ]$$

$$= 2 \times 125 = 250$$

(ii) 
$$(5^{-1} \times 2^{-2}) \times 6^{-1}$$

# $(5^{-1} \times 2^{-1}) \times 6^{-1} = (\frac{1}{5} \times \frac{1}{2}) \times \frac{1}{6}$

$$\left[ \begin{array}{cc} \cdots & a^{-m} = \frac{1}{a^m} \end{array} \right]$$

$$=(1/10)\times1/6$$

$$= 1/60$$

# 5. Find the value of m for which $5^m \div 5^{-3} = 5^5$

**Solution:** 

$$5^m \div 5^{-3} = 5^5$$

$$5^{(m-(-3))} = 5^5$$

$$\left[ \because a^m \div a^n = a^{m-n} \right]$$

$$5^{m+3} = 5^5$$

Comparing exponents on both sides, we get

$$m+3 = 5$$

$$m = 5-3$$

$$m = 2$$

# 6. Evaluate:

(i)

$$\left\{ \left(\frac{1}{3}\right)^{-1} - \left(\frac{1}{4}\right)^{-1} \right\}^{-1}$$

(ii)

$$\left(\frac{5}{8}\right)^{-7} \times \left(\frac{8}{5}\right)^{-4}$$

# **Solution:**

(i)



$$\left\{ \left(\frac{1}{3}\right)^{-1} - \left(\frac{1}{4}\right)^{-1} \right\} = \left\{ \left(\frac{3}{1}\right)^{1} - \left(\frac{4}{1}\right)^{1} \right\}$$

$$\left[ \because a^{-m} = \frac{1}{a^{m}} \right]$$

$$\left(\frac{5}{8}\right)^{-7} \times \left(\frac{8}{5}\right)^{-4} = \frac{5^{-7}}{8^{-7}} \times \frac{8^{-4}}{5^{-4}}$$

$$\left[\because \left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}\right]$$

$$5^{-7-(-4)} \times 8^{-4-(-7)}$$

$$\left[ \because \ a^m \div a^n = a^{m-n} \right]$$

$$=$$
  $5^{-7+4} \times 8^{-4+7}$ 

$$=5^{-3}\times8^3$$

$$\frac{8^{3}}{2^{3}}$$

$$\frac{8^3}{5^3}$$

$$\left[ \because a^{-m} = \frac{1}{a^m} \right]$$

$$= 512/125$$

# 7. Simplify the following:

(i)

$$\frac{25 \times t^{-4}}{5^{-3} \times 10 \times t^{-8}} \quad (t \neq 0)$$

(ii)

$$\frac{3^{-5} \times 10^{-5} \times 125}{5^{-7} \times 6^{-5}}$$



Solution:

(i)

$$\frac{25 \times t^{-4}}{5^{-3} \times 10 \times t^{-8}}$$

$$=\frac{5^2 \times t^{-4}}{5^{-3} \times 5 \times 2 \times t^{-8}}$$

$$=\frac{5^{2-(-3)-1}\times t^{-4-(-8)}}{2}$$

$$\left[ : a^m \div a^n = a^{m-n} \right]$$

$$\frac{5^{2+3-1} \times t^{-4+8}}{2} = \frac{5^4 \times t^4}{2} = \frac{625}{2}$$

$$\frac{625}{2}t^4$$

(ii)

$$\frac{3^{-5} \times 10^{-5} \times 125}{5^{-7} \times 6^{-5}}$$

$$=\frac{3^{-5}\times (2\times 5)^{-5}\times 5^3}{5^{-7}\times (2\times 3)^{-5}}$$

$$=\frac{3^{-5}\times 2^{-5}\times 5^{-5}\times 5^{3}}{5^{-7}\times 2^{-5}\times 3^{-5}}$$

$$\left[ \because (ab)^m = a^m b^m \right]$$

$$\frac{2^{-5} \times 2^{-5} \times 5^{-5+3}}{5^{-7} \times 2^{-5} \times 3^{-5}} = \frac{3^{-5} \times 2^{-5} \times 5^{-2}}{5^{-7} \times 2^{-5} \times 3^{-5}}$$

$$\left[ \because a^m \times a^n = a^{m+n} \right]$$

$$3^{-5-(-5)} \times 2^{-5-(-5)} \times 5^{-2-(-7)}$$

$$\left[ \because \ a^m \div a^n = a^{m-n} \right]$$

$$= \\ 3^{\text{-5+5}} \times 2^{\text{-5+5}} \times 5^{\text{-2+7}} =$$

$$3^0\!\times\!2^0\!\times\!5^5$$

$$= 1 \times 1 \times 3125$$

$$\begin{bmatrix} \because a^0 = 1 \end{bmatrix}$$

$$= 3125$$



# EXERCISE 12.2 PAGE NO: 200

- 1. Express the following numbers in standard form.
- (i) 0.0000000000085
- (ii) 0.00000000000942
- (iii) 60200000000000000
- (iv) 0.00000000837
- (v) 31860000000

#### **Solution:**

- (i)  $0.0000000000085 = 0.000000000085 \times (10^{12}/10^{12}) = 8.5 \times 10^{-12}$
- (ii)  $0.00000000000942 = 0.00000000000942 \times (10^{12}/10^{12}) = 9.42 \times 10^{-12}$
- (iv)  $0.00000000837 = 0.00000000837 \times (10^9/10^9) = 8.37 \times 10^{-9}$
- (v)  $31860000000 = 31860000000 \times (10^{10}/10^{10}) = 3.186 \times 10^{10}$
- 2. Express the following numbers in the usual form.
- (i) 3.02×10-6
- (ii) 4.5×10<sup>4</sup>
- (iii) 3×10-8
- (iv) 1.0001×109
- (v)  $5.8 \times 10^{12}$
- (vi) 3.61492×106

#### **Solution:**

- (i)  $3.02 \times 10^{-6} = 3.02/10^{6} = 0.00000302$
- (ii)  $4.5 \times 10^4 = 4.5 \times 10000 = 45000$
- (iii)  $3 \times 10^{-8} = 3/10^8 = 0.000000003$
- (iv)  $1.0001 \times 10^9 = 1000100000$
- (v)  $5.8 \times 10^{12} = 5.8 \times 1000000000000 = 58000000000000$

# NCERT Solutions for Class 8 Maths Chapter 12 – Exponents and Powers

(vi)  $3.61492 \times 10^6 = 3.61492 \times 1000000 = 3614920$ 

- 3. Express the number appearing in the following statements in standard form.
- (i) 1 micron is equal to 1/1000000 m.
- (ii) Charge of an electron is 0.000, 000, 000, 000, 000, 000, 16 coulomb.
- (iii) Size of bacteria is 0.0000005 m
- (iv) Size of a plant cell is 0.00001275 m
- (v) Thickness of a thick paper is 0.07 mm

#### **Solution:**

- (i) 1 micron = 1/1000000
- $= 1/10^6$
- $= 1 \times 10^{-6}$
- (ii) Charge of an electron is 0.0000000000000000016 coulombs
- $= 0.00000000000000000016 \times 10^{19} / 10^{19}$
- $= 1.6 \times 10^{-19}$  coulomb
- (iii) Size of bacteria = 0.0000005
- $= 5/100000000 = 5/10^7 = 5 \times 10^{-7} \text{ m}$
- (iv) Size of a plant cell is 0.00001275 m
- $= 0.00001275 \times 10^{5}/10^{5}$
- $= 1.275 \times 10^{-5} \text{m}$
- (v) Thickness of a thick paper = 0.07 mm

 $0.07 \text{ mm} = 7/100 \text{ mm} = 7/10^{2} = 7 \times 10^{-2} \text{ mm}$ 

4. In a stack, there are 5 books, each having a thickness of 20 mm and 5 paper sheets, each having a thickness of 0.016 mm. What is the total thickness of the stack?

Solution:

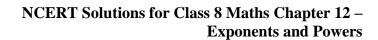
Thickness of one book = 20 mm

Thickness of 5 books =  $20 \times 5 = 100 \text{ mm}$ 

Thickness of one paper = 0.016 mm

Thickness of 5 papers =  $0.016 \times 5 = 0.08$  mm

Total thickness of a stack = 100+0.08 = 100.08 mm





 $= 100.08 \times 10^2 / 10^2 \text{ mm}$ 

 $=1.0008\times10^{2}$  mm

