## EXERCISE 13.1

1. The following are the car parking charges near a railway station up to,

4 hours - Rs. 60
8 hours - Rs. 100

12 hours - Rs. 140
24 hours - Rs. 180


Check if the parking charges are in direct proportion to the parking time.

## Solution:

Charges per hour:
$\mathrm{C} 1=60 / 4=$ Rs. 15
$\mathrm{C} 2=100 / 8=$ Rs. 12.50
$C 3=140 / 12=$ Rs. 11.67
$\mathrm{C} 4=180 / 24=$ Rs. 7.50
Here, the charges per hour are not the same, i.e. $\mathrm{C} 1 \neq \mathrm{C} 2 \neq \mathrm{C} 3 \neq \mathrm{C} 4$
Therefore, the parking charges are not in direct proportion to the parking time.
2. A mixture of paint is prepared by mixing 1 part of red pigments with 8 parts of the base. In the following table, find the parts of the base that need to be added.

| Parts of red pigment | 1 | 4 | 7 | 12 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Parts of base | 8 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$. |

Solution:
Let the ratio of parts of red pigment and parts of the base be $\mathrm{a} / \mathrm{b}$.
Case 1: Here, $a_{1}=1, b_{1}=8$

$$
\mathrm{a}_{1} / \mathrm{b}_{1}=1 / 8=\mathrm{k} \text { (say) }
$$

Case 2: When $\mathrm{a}_{2}=4, \mathrm{~b}_{2}=$ ?
$k=\frac{a_{2}}{b_{2}}$
$\mathrm{b}_{2}=\mathrm{a}_{2} / \mathrm{k}=4 /(1 / 8)=4 \times 8=32$
Case 3: When $\mathrm{a}_{3}=7, \mathrm{~b}_{3}=$ ?
$k=\frac{a_{3}}{b_{3}}$
$\mathrm{b}_{3}=\mathrm{a}_{3} / \mathrm{k}=7 /(1 / 8)=7 \times 8=56$
Case 4: When $\mathrm{a}_{4}=12, \mathrm{~b}_{4}=$ ?
$k=\frac{a_{4}}{b_{4}}$
$\mathrm{b}_{4}=\mathrm{a}_{4} / \mathrm{k}=12 /(1 / 8)=12 \times 8=96$
Case 5: When $a_{5}=20, b_{5}=$ ?
$k=\frac{a_{5}}{b_{5}}$
$\mathrm{b}_{5}=\mathrm{a}_{5} / \mathrm{k}=20 /(1 / 8)=20 \times 8=160$
When combining results for all the cases, we get

| Parts of red pigment | 1 | 4 | 7 | 12 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Parts of base | 8 | 32 | 56 | 96 | 160 |

3. In Question 2 above, if 1 part of a red pigment requires 75 mL of the base, how much red pigment should we mix with 1800 mL of the base?

## Solution:

Let the parts of red pigment mix with 1800 mL base be x .

| Parts of red pigment | 1 | $x$ |
| :--- | :--- | :--- |
| Parts of base | 75 | 1800 |

Since it is in direct proportion,

$$
\frac{1}{75}=\frac{x}{1800}
$$

$$
\begin{aligned}
& \Rightarrow \\
& 75 \times x=1 \times 1800 \\
& x=\frac{1 \times 1800}{75}=24
\end{aligned}
$$

Hence, with the base $1800 \mathrm{~mL}, 24$ parts of the red pigment should be mixed.
4. A machine in a soft drink factory fills $\mathbf{8 4 0}$ bottles in six hours. How many bottles will it fill in five hours?


## Solution:

Let the number of bottles filled in five hours be x .
Here, the ratio of hours and bottles is in direct proportion.

$$
\frac{6}{840}=\frac{5}{x}
$$

$6 \mathrm{x}=5 \times 840$
$x=5 \times 840 / 6=700$
Hence, the machine will fill 700 bottles in five hours.
5. A photograph of a bacteria enlarged 50,000 times attains a length of 5 cm , as shown in the diagram. What is the actual length of the bacteria? If the photograph is enlarged 20,000 times only, what would be its enlarged length?

## Solution:

Let the enlarged length of bacteria be x .
Actual length of bacteria $=5 / 50000=1 / 10000 \mathrm{~cm}=10^{-4} \mathrm{~cm}$

| Length | 5 | $x$ |
| :--- | :--- | :--- |
| Enlarged length | 50,000 | 20,000 |

Here, the length and enlarged length of bacteria are in direct proportion.
$\frac{5}{50000}=\frac{x}{20000}$
$\Rightarrow$
$x \times 50000=5 \times 20000$
$x=\frac{5 \times 20000}{50000}$
$\mathrm{x}=2 \mathrm{~cm}$
Hence, the enlarged length of bacteria is 2 cm .
6. In a model of a ship, the mast is 9 cm high, while the mast of the actual ship is 12 m high. If the length of the ship is 28 m , how long is the model ship?


## Solution:

Let the length of the model ship be x .

| Length of actual ship (in m) | 12 | 28 |
| :--- | :--- | :--- |
| Length of model ship (in cm) | 9 | $x$ |

Here, the length of the mast and the actual length of the ship are in direct proportion.
$\frac{12}{9}=\frac{28}{x}$
$\Rightarrow$
$x \times 12=28 \times 9$
$x=\frac{28 \times 9}{12}$
$\mathrm{x}=21 \mathrm{~cm}$
Hence, the length of the model ship is 21 cm .
7. Suppose 2 kg of sugar contains $9 \times 10^{6}$ crystals. How many sugar crystals are there in
(i) 5 kg of sugar? (ii) 1.2 kg of sugar?

Solution:
(i) Let sugar crystals be x .

| Weight of sugar (in kg) | 2 | 5 |
| :--- | :--- | :--- |
| No. of crystals | $9 \times 10^{6}$ | $x$ |

Here, the weight of sugar and the number of crystals are in direct proportion.

$$
\begin{aligned}
& \frac{2}{9 \times 10^{6}}=\frac{5}{x} \\
& \Rightarrow \\
& x \times 2=5 \times 9 \times 10^{6} \\
& x=\frac{5 \times 9 \times 10^{6}}{2} \\
& = \\
& 22.5 \times 10^{6}=2.25 \times 10^{7}
\end{aligned}
$$

Hence, the number of sugar crystals is $2.25 \times 10^{7}$.
(ii) Let sugar crystals be x .

Here, the weight of sugar and the number of crystals are in direct proportion.

| Weight of sugar (in kg) | 2 | 1.2 |
| :--- | :--- | :--- |
| No. of crystals | $9 \times 10^{6}$ | $x$ |

$$
\begin{aligned}
& \frac{2}{9 \times 10^{6}}=\frac{1.2}{x} \\
& \Rightarrow \\
& x \times 2=1.2 \times 9 \times 10^{6} \\
& x=\frac{1.2 \times 9 \times 10^{6}}{2} \\
& = \\
& 0.6 \times 9 \times 10^{6}=5.4 \times 10^{6}
\end{aligned}
$$

Hence, the number of sugar crystals is $5.4 \times 10^{6}$.
8. Rashmi has a road map with a scale of 1 cm representing 18 km . She drives on the road for 72 km . What would be her distance covered on the map?

## Solution:

Let the distance covered in the map be x.

| Actual distance <br> (in km) | 18 | 72 |
| :--- | :--- | :--- |
| Distance covered in map (in cm) | 1 | $x$ |

Here, the actual distance and distance covered in the map are in direct proportion.

$$
\frac{18}{1}=\frac{72}{x}
$$

$$
\Rightarrow
$$

$$
x \times 18=72 \times 1
$$

$x=\frac{72 \times 1}{18}$
$\mathrm{x}=4 \mathrm{~cm}$
Hence, the distance covered on the map is 4 cm .
9. A 5 m 60 cm high vertical pole casts a shadow 3 m 20 cm long. Find at the same time (i) the length of the shadow cast by another pole 10 m 50 cm high (ii) the height of a pole which casts a shadow 5 m long.

## Solution:

Here, the height of the pole and the length of the shadow are in direct proportion.
And $1 \mathrm{~m}=100 \mathrm{~cm}$
$5 \mathrm{~m} 60 \mathrm{~cm}=5 \times 100+60=560 \mathrm{~cm}$
$3 \mathrm{~m} 20 \mathrm{~cm}=3 \times 100+20=320 \mathrm{~cm}$
$10 \mathrm{~m} 50 \mathrm{~cm}=10 \times 100+50=1050 \mathrm{~cm}$
$5 \mathrm{~m}=5 \times 100=500 \mathrm{~cm}$
(i) Let the length of the shadow of another pole be x .

| Height of pole (in cm) | 560 | 1050 |
| :--- | :--- | :--- |
| Length of shadow <br> (in cm) | 320 | $x$ |

$\frac{560}{320}=\frac{1050}{x}$
$\Rightarrow$
$x \times 560=1050 \times 320$
$x=\frac{1050 \times 320}{560}$
$x=600 \mathrm{~cm}=6 \mathrm{~m}$
Hence, the length of the shadow of another pole is 6 m .
(ii) Let the height of the pole be x .

| Height of pole (in cm) | 560 | $x$ |
| :--- | :--- | :--- |
| Length of shadow <br> (in cm) | 320 | 500 |

$$
\begin{aligned}
& \frac{560}{320}=\frac{x}{500} \\
& \Rightarrow \\
& x \times 320=560 \times 500 \\
& x=\frac{560 \times 500}{320} \\
& =875 \mathrm{~cm}=8 \mathrm{~m} 75 \mathrm{~cm}
\end{aligned}
$$

Hence, the height of the pole is 8 m 75 cm .
10. A loaded truck travels 14 km in 25 minutes. If the speed remains the same, how far can it travel in 5 hours?

## Solution:

Let the distance covered in 5 hours be x km .
1 hour $=60$ minutes
Therefore, 5 hours $=5 \times 60=300$ minutes

| Distance (in km) | 14 | $x$ |
| :--- | :--- | :--- |
| Time (in minutes) | 25 | 300 |

Here, the distance covered and time are in direct proportion.
$\frac{14}{25}=\frac{x}{300}$
$\Rightarrow 25 \mathrm{x}=300(14)$
$x=\frac{14 \times 300}{25}$
$x=168$
Therefore, the truck can travel 168 km in 5 hours.

## EXERCISE 13.2

1. Which of the following are in inverse proportion?
(i) The number of workers on a job and the time to complete the job.
(ii) The time taken for a journey and the distance travelled at a uniform speed.
(iii) Area of cultivated land and the crop harvested.
(iv) The time taken for a fixed journey and the speed of the vehicle.
(v) The population of a country and the area of land per person.

## Solution:

(i) The number of workers and the time to complete the job is in inverse proportion because less workers will take more time to complete a job, and more workers will take less time to complete the same job.
(ii) Time and distance covered in direct proportion.
(iii) It is a direct proportion because more are of cultivated land will yield more crops.
(iv) Time and speed are in inverse proportion because if time is less, speed is more.
(v) It is an inverse proportion. If the population of a country increases, the area of land per person decreases.
2. In a Television game show, the prize money of Rs. $1,00,000$ is to be divided equally amongst the winners. Complete the following table and find whether the prize money given to an individual winner is directly or inversely proportional to the number of winners:

| No. of winners | 1 | 2 | 4 | 5 | 8 | 10 | 20 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Prize for each winner (in $\operatorname{RO}_{5}$ ) | $1,00,000$ | 50,000 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
|  |  |  |  |  |  |  |  |

## Solution:

Here, the number of winners and prize money are in inverse proportion because winners are increasing, and prize money is decreasing.

When the number of winners is 4 , each winner will get $=100000 / 4=$ Rs. 25,000
When the number of winners is 5 , each winner will get $=100000 / 5=$ Rs. 20,000

When the number of winners is 8 , each winner will get $=100000 / 8=$ Rs. 12,500
When the number of winners is 10 , each winner will get $=100000 / 10=$ Rs. 10,000
When the number of winners is 20 , each winner will get $=100000 / 20=$ Rs. 5,000
3. Rehman is making a wheel using spokes. He wants to fix equal spokes in such a way that the angles between any pair of consecutive spokes are equal. Help him by completing the following table:


| Number of spokes | 4 | 6 | 8 | 10 | 12 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Angle between <br> a pair of consecutive <br> spokes | $90^{\circ}$ | $60^{\circ}$ | $\ldots$ | $\ldots$ | $\ldots$ |

(i) Are the number of spokes and the angles formed between the pairs of consecutive spokes in inverse proportion?
(ii) Calculate the angle between a pair of consecutive spokes on a wheel with 15 spokes.
(iii) How many spokes would be needed, if the angle between a pair of consecutive spokes is 40 degree?

## Solution:

Here, the number of spokes is increasing, and the angle between a pair of consecutive spokes is decreasing. So, it is an inverse proportion, and the angle at the centre of a circle is 360 degree.

When the number of spokes is 8 , then the angle between a pair of consecutive spokes $=360 / 8=45$ degree
When the number of spokes is 10 , then the angle between a pair of consecutive spokes $=360 / 10=36$ degree.
When the number of spokes is 12 , then the angle between a pair of consecutive spokes $=360 / 12=30$ degree .

| No. of spokes | 4 | 6 | 8 | 10 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Angle between a pair of consecutive spokes |  |  |  |  |  |
|  | $90^{\circ}$ | $60^{\circ}$ | $45^{\circ}$ | $36^{\circ}$ | $30^{\circ}$ |
|  |  |  |  |  |  |

(i) Yes, the number of spokes and the angles formed between a pair of consecutive spokes is in inverse proportion.
(ii) When the number of spokes is 15 , then the angle between a pair of consecutive spokes $=360 / 15=24$ degree.
(iii) The number of spokes would be needed $=360 / 40=9$
4. If a box of sweets is divided among 24 children, they will get 5 sweets each. How many would each get, if the number of children is reduced by 4 ?

## Solution:

Each child gets $=5$ sweets
24 children will get $24 \times 5=120$ sweets.
Total number of sweets $=120$
If the number of children is reduced by 4 , then children left $=24-4=20$
Now, each child will get sweets $=120 / 20=6$ sweets
5. A farmer has enough food to feed 20 animals in his cattle for 6 days. How long would the food last if there were 10 more animals in his cattle?

## Solution:

Let the number of days be $x$.
Total number of animals $=20+10=30$

| Animals | 20 | 30 |
| :--- | :--- | :--- |
| Days | 6 | $x$ |

Here, the number of animals and the number of days are in inverse proportion.

$$
\frac{20}{30}=\frac{x}{6}
$$

$30 \times x=20 \times 6$
$x=\frac{20 \times 6}{30}$
$x=4$
Hence, the food will last for four days.
6. A contractor estimates that 3 persons could rewire Jasminder's house in 4 days. If he uses 4 persons instead of three, how long should they take to complete the job?

## Solution:

Let the time taken to complete the job be x .

| Persons | 3 | 4 |
| :--- | :--- | :--- |
| Days | 4 | $x$ |

Here, the number of persons and the number of days are in inverse proportion.
$3 / 4=x / 4$
$3 \times 4=4 \mathrm{x}$
$x=3 \times 4 / 4$
$\mathrm{x}=3$
Hence, 4 persons will complete the job in 3 days.
7. A batch of bottles was packed in 25 boxes, with 12 bottles in each box. If the same batch is packed using 20 bottles in each box, how many boxes would be filled?

## Solution:

Let the number of boxes be $x$.

| No. of bottles in each box | 12 | 20 |
| :--- | :--- | :--- |
| Boxes | 25 | $x$ |

Here, the number of bottles and the number of boxes are in inverse proportion.
$12 / 20=x / 25$
$12 \times 25=20 x$
$x=12 \times 25 / 20=15$
Hence, 15 boxes would be filled.
8. A factory requires 42 machines to produce a given number of articles in 63 days. How many machines would be required to produce the same number of articles in $\mathbf{5 4}$ days?

## Solution:

Let the number of machines required be x .

| Days | 63 | 54 |
| :--- | :--- | :--- |
| Machines | 42 | $x$ |

Here, the number of machines and the number of days are in inverse proportion.
$63 / 54=x / 42$
$63 \times 42=54 x$
$x=63 \times 42 / 54$
$x=49$
Hence, 49 machines would be required.
9. A car takes 2 hours to reach a destination by travelling at the speed of $60 \mathrm{~km} / \mathrm{hr}$. How long will it take when the car travels at the speed of $80 \mathrm{~km} / \mathrm{hr}$ ?

Solution :
Let the number of hours be $x$.

| Speed (in km/hr) | 60 | 80 |
| :--- | :--- | :--- |
| Time (in hours) | 2 | $x$ |

Here, the speed of the car and time are in inverse proportion.
$60 / 80=x / 2$
$60 \times 2=80 \mathrm{x}$
$x=60 \times 2 / 80$
$\mathrm{x}=3 / 2=1 \frac{1}{2} \mathrm{hrs}$.

## Hence the car will take $1 \frac{1}{2}$ hours to reach its destination.

10. Two persons could fit new windows in a house in 3 days.
(i) One of the persons fell ill before the work started. How long would the job take now?
(ii) How many persons would be needed to fit the windows in one day?

Solution:
(i) Let the number of days be x .

| Persons | 2 | 1 |
| :--- | :--- | :--- |
| Days | 3 | $x$ |

Here, the number of persons and the number of days are in inverse proportion.
$2 / 1=x / 3$
$6=x$
Or
$x=6$ days
(ii) Let the number of persons be x .

| Persons | 2 | $x$ |
| :--- | :--- | :--- |
| Days | 3 | 1 |

Here, the number of persons and the number of days are in inverse proportion.
$2 / \mathrm{x}=1 / 3$
$6=x$
Or
$x=6$ persons
11. A school has 8 periods a day, each of 45 minutes duration. How long would each period be, if the school has 9 periods a day, assuming the number of school hours to be the same?

## Solution:

Let the duration of each period be x .

| Period | 8 | 9 |
| :--- | :--- | :--- |
| Duration of period (in minutes) | 45 | $x$ |

Here, the number of periods and the duration of periods are in inverse proportion.
$8 / 9=x / 45$
$8 \times 45=9 x$
$x=40$
Hence, the duration of each period would be 40 minutes.

