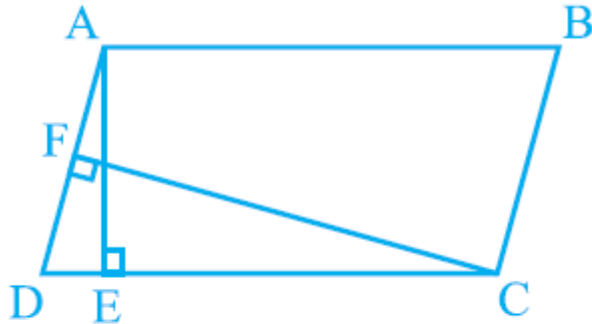


**EXERCISE 9.2**

1. In Fig. 9.15, ABCD is a parallelogram,  $AE \perp DC$  and  $CF \perp AD$ . If  $AB = 16$  cm,  $AE = 8$  cm and  $CF = 10$  cm, find AD.



**Fig. 9.15**

Solution:

Given,

$AB = CD = 16$  cm (Opposite sides of a parallelogram.)

$CF = 10$  cm and  $AE = 8$  cm

Now,

Area of parallelogram = Base  $\times$  Altitude

$$= CD \times AE = AD \times CF$$

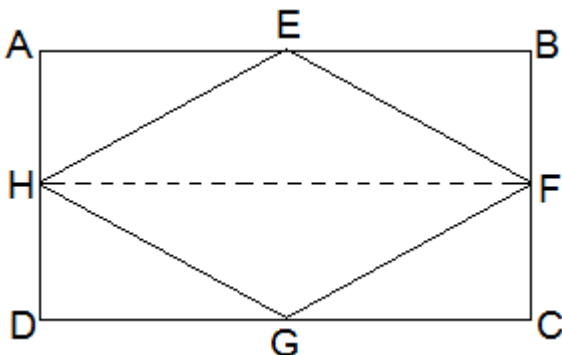
$$\Rightarrow 16 \times 8 = AD \times 10$$

$$\Rightarrow AD = 128/10 \text{ cm}$$

$$\Rightarrow AD = 12.8 \text{ cm}$$

2. If E, F, G and H are, respectively, the mid-points of the sides of a parallelogram ABCD show that  $\text{ar}(EFGH) = \frac{1}{2} \text{ar}(ABCD)$ .

Solution:



Given,

E, F, G and H are the mid-points of the sides of a parallelogram ABCD, respectively.

To prove,

$$\text{ar (EFGH)} = \frac{1}{2} \text{ar(ABCD)}$$

Construction,

H and F are joined.

Proof,

AD  $\parallel$  BC and AD = BC (Opposite sides of a parallelogram.)

$$\Rightarrow \frac{1}{2} \text{AD} = \frac{1}{2} \text{BC}$$

Also,

AH  $\parallel$  BF and DH  $\parallel$  CF

$\Rightarrow$  AH = BF and DH = CF (H and F are mid-points.)

$\therefore$ , ABFH and HFCD are parallelograms.

Now,

We know that  $\triangle EFH$  and parallelogram ABFH lie on the same FH, the common base and in-between the same parallel lines AB and HF.

$$\therefore \text{area of EFH} = \frac{1}{2} \text{area of ABFH} \text{ --- (i)}$$

$$\text{And, area of GHF} = \frac{1}{2} \text{area of HFCD} \text{ --- (ii)}$$

Adding (i) and (ii),

$$\text{Area of } \triangle EFH + \text{area of } \triangle GHF = \frac{1}{2} \text{area of ABFH} + \frac{1}{2} \text{area of HFCD}$$

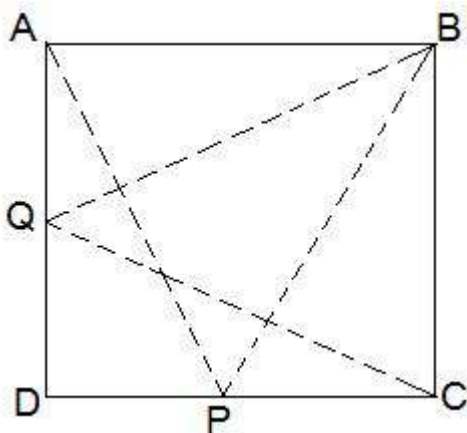
$$\Rightarrow \text{area of EFGH} = \text{area of ABFH}$$

$$\therefore \text{ar (EFGH)} = \frac{1}{2} \text{ar(ABCD)}$$

**3. P and Q are any two points lying on the sides DC and AD, respectively, of a parallelogram ABCD.**

**Show that ar(APB) = ar(BQC).**

Solution:



$\triangle APB$  and parallelogram  $ABCD$  lie on the same base  $AB$  and in-between the same parallel  $AB$  and  $DC$ .

$$\text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(\text{parallelogram } ABCD) \text{ — (i)}$$

Similarly,

$$\text{ar}(\triangle BQC) = \frac{1}{2} \text{ar}(\text{parallelogram } ABCD) \text{ — (ii)}$$

From (i) and (ii), we have

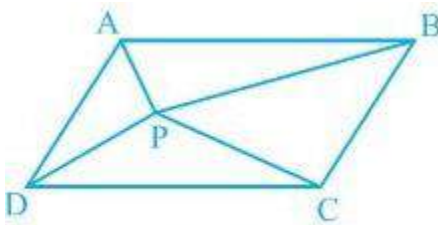
$$\text{ar}(\triangle APB) = \text{ar}(\triangle BQC)$$

**4. In Fig. 9.16, P is a point in the interior of a parallelogram ABCD. Show that**

**(i)  $\text{ar}(\triangle APB) + \text{ar}(\triangle PCD) = \frac{1}{2} \text{ar}(ABCD)$**

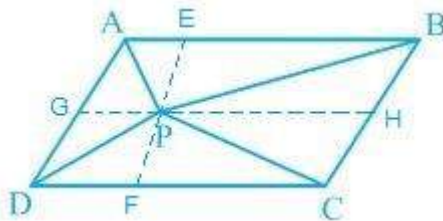
**(ii)  $\text{ar}(\triangle APD) + \text{ar}(\triangle PBC) = \text{ar}(\triangle APB) + \text{ar}(\triangle PCD)$**

[Hint: Through P, draw a line parallel to AB.]



**Fig. 9.16**

Solution:



(i) A line  $GH$  is drawn parallel to  $AB$  passing through  $P$ .

In a parallelogram,

$$AB \parallel GH \text{ (by construction) — (i)}$$

$\therefore$ ,

$$AD \parallel BC \Rightarrow AG \parallel BH \text{ — (ii)}$$

From equations (i) and (ii),

$ABHG$  is a parallelogram.

Now,

$\triangle APB$  and parallelogram  $ABHG$  are lying on the same base  $AB$  and in-between the same parallel lines  $AB$  and  $GH$ .

$$\therefore \text{ar}(\triangle APB) = \frac{1}{2} \text{ar}(ABHG) \text{ — (iii)}$$

also,

$\Delta PCD$  and parallelogram  $CDGH$  are lying on the same base  $CD$  and in-between the same parallel lines  $CD$  and  $GH$ .

$$\therefore \text{ar}(\Delta PCD) = \frac{1}{2} \text{ar}(CDGH) \text{ — (iv)}$$

Adding equations (iii) and (iv),

$$\text{ar}(\Delta APB) + \text{ar}(\Delta PCD) = \frac{1}{2} [\text{ar}(ABHG) + \text{ar}(CDGH)]$$

$$\Rightarrow \text{ar}(APB) + \text{ar}(PCD) = \frac{1}{2} \text{ar}(ABCD)$$

(ii) A line  $EF$  is drawn parallel to  $AD$  passing through  $P$ .

In the parallelogram,

$$AD \parallel EF \text{ (by construction) — (i)}$$

$\therefore$ ,

$$AB \parallel CD \Rightarrow AE \parallel DF \text{ — (ii)}$$

From equations (i) and (ii),

$AEDF$  is a parallelogram.

Now,

$\Delta APD$  and parallelogram  $Aefd$  are lying on the same base  $AD$  and in-between the same parallel lines  $AD$  and  $EF$ .

$$\therefore \text{ar}(\Delta APD) = \frac{1}{2} \text{ar}(Aefd) \text{ — (iii)}$$

also,

$\Delta PBC$  and parallelogram  $BCFE$  are lying on the same base  $BC$  and in-between the same parallel lines  $BC$  and  $EF$ .

$$\therefore \text{ar}(\Delta PBC) = \frac{1}{2} \text{ar}(BCFE) \text{ — (iv)}$$

Adding equations (iii) and (iv),

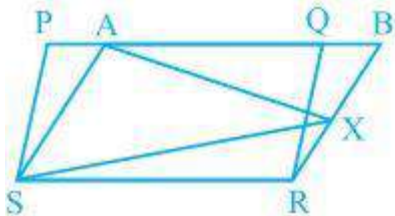
$$\text{ar}(\Delta APD) + \text{ar}(\Delta PBC) = \frac{1}{2} \{ \text{ar}(Aefd) + \text{ar}(BCFE) \}$$

$$\Rightarrow \text{ar}(APD) + \text{ar}(PBC) = \text{ar}(APB) + \text{ar}(PCD)$$

**5. In Fig. 9.17, PQRS and ABRS are parallelograms, and X is any point on side BR. Show that**

**(i)  $\text{ar}(PQRS) = \text{ar}(ABRS)$**

**(ii)  $\text{ar}(AXS) = \frac{1}{2} \text{ar}(PQRS)$**



**Fig. 9.17**

Solution:

(i) Parallelogram  $PQRS$  and  $ABRS$  lie on the same base  $SR$  and in-between the same parallel lines  $SR$  and  $PB$ .

$$\therefore \text{ar}(PQRS) = \text{ar}(ABRS) \text{ — (i)}$$

(ii)  $\triangle AXS$  and parallelogram  $ABRS$  are lying on the same base  $AS$  and in-between the same parallel lines  $AS$  and  $BR$ .

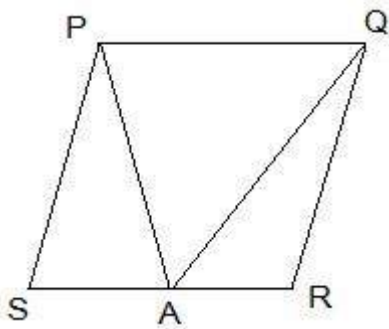
$$\therefore \text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(\text{ABRS}) \text{ — (ii)}$$

From (i) and (ii), we find that

$$\text{ar}(\triangle AXS) = \frac{1}{2} \text{ar}(\text{PQRS})$$

**6. A farmer was having a field in the form of a parallelogram  $PQRS$ . She took any point  $A$  on  $RS$  and joined it to points  $P$  and  $Q$ . In how many parts are the fields divided? What are the shapes of these parts? The farmer wants to sow wheat and pulses in equal portions of the field separately. How should she do it?**

Solution:



The field is divided into three parts, each in a triangular shape.

Let  $\triangle PSA$ ,  $\triangle PAQ$  and  $\triangle QAR$  be the triangles.

$$\text{Area of } (\triangle PSA + \triangle PAQ + \triangle QAR) = \text{Area of PQRS} \text{ — (i)}$$

$$\text{Area of } \triangle PAQ = \frac{1}{2} \text{ area of PQRS} \text{ — (ii)}$$

Here, the triangle and parallelogram are on the same base and in-between the same parallel lines.

From (i) and (ii),

$$\text{Area of } \triangle PSA + \text{Area of } \triangle QAR = \frac{1}{2} \text{ area of PQRS} \text{ — (iii)}$$

From (ii) and (iii), we can conclude that

The farmer must sow wheat or pulses in  $\triangle PAQ$  or either in both  $\triangle PSA$  and  $\triangle QAR$ .