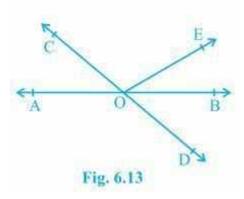


**EXERCISE: 6.1** 

(PAGE NO: 96)

1. In Fig. 6.13, lines AB and CD intersect at O. If  $\angle AOC + \angle BOE = 70^{\circ}$  and  $\angle BOD = 40^{\circ}$ , find  $\angle BOE$  and reflex  $\angle COE$ .



# **Solution:**

From the diagram, we have

 $(\angle AOC + \angle BOE + \angle COE)$  and  $(\angle COE + \angle BOD + \angle BOE)$  forms a straight line.

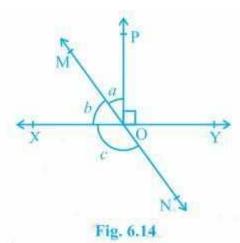
So,  $\angle AOC + \angle BOE + \angle COE = \angle COE + \angle BOD + \angle BOE = 180^{\circ}$ 

Now, by putting the values of  $\angle AOC + \angle BOE = 70^{\circ}$  and  $\angle BOD = 40^{\circ}$  we get

 $\angle COE = 110^{\circ} \text{ and } \angle BOE = 30^{\circ}$ 

So, reflex  $\angle COE = 360^{\circ} - 110^{\circ} = 250^{\circ}$ 

2. In Fig. 6.14, lines XY and MN intersect at O. If  $\angle POY = 90^{\circ}$  and a : b = 2 : 3, find c.



#### **Solution:**

We know that the sum of linear pair is always equal to 180°

So,

 $\angle POY + a + b = 180^{\circ}$ 



Putting the value of  $\angle POY = 90^{\circ}$  (as given in the question), we get,

$$a+b = 90^{\circ}$$

Now, it is given that a:b = 2:3, so

Let a be 2x and b be 3x

$$\therefore 2x+3x = 90^{\circ}$$

Solving this, we get

$$5x = 90^{\circ}$$

So, 
$$x = 18^{\circ}$$

$$\therefore a = 2 \times 18^{\circ} = 36^{\circ}$$

Similarly, b can be calculated, and the value will be

$$b = 3 \times 18^{\circ} = 54^{\circ}$$

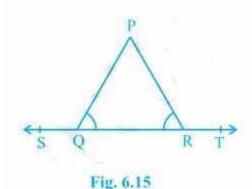
From the diagram, b+c also forms a straight angle, so

$$b+c = 180^{\circ}$$

$$c+54^{\circ} = 180^{\circ}$$

$$\therefore$$
 c = 126°

# 3. In Fig. 6.15, $\angle PQR = \angle PRQ$ , then prove that $\angle PQS = \angle PRT$ .



#### **Solution:**

Since ST is a straight line, so

 $\angle PQS + \angle PQR = 180^{\circ}$  (linear pair) and

 $\angle PRT + \angle PRQ = 180^{\circ}$  (linear pair)

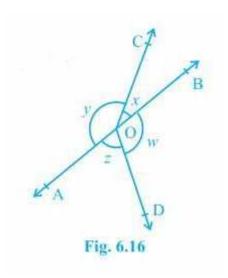
Now,  $\angle PQS + \angle PQR = \angle PRT + \angle PRQ = 180^{\circ}$ 

Since  $\angle PQR = \angle PRQ$  (as given in the question)

 $\angle PQS = \angle PRT$ . (Hence proved).

4. In Fig. 6.16, if x+y = w+z, then prove that AOB is a line.





To prove AOB is a straight line, we will have to prove x+y is a linear pair

i.e. 
$$x+y = 180^{\circ}$$

We know that the angles around a point are 360°, so

$$x+y+w+z = 360^{\circ}$$

In the question, it is given that,

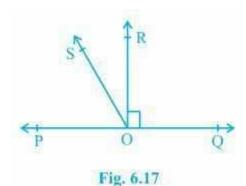
$$x+y = w+z$$

So, 
$$(x+y)+(x+y) = 360^{\circ}$$

$$2(x+y) = 360^{\circ}$$

 $\therefore$  (x+y) = 180° (Hence proved).

5. In Fig. 6.17, POQ is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that  $\angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$ .



# Solution:

In the question, it is given that (OR  $\perp$  PQ) and  $\angle$ POQ = 180°

We can write it as  $\angle ROP = \angle ROQ = 90^{\circ}$ 



We know that

$$\angle ROP = \angle ROQ$$

It can be written as

$$\angle POS + \angle ROS = \angle ROQ$$

$$\angle POS + \angle ROS = \angle QOS - \angle ROS$$

$$\angle SOR + \angle ROS = \angle QOS - \angle POS$$

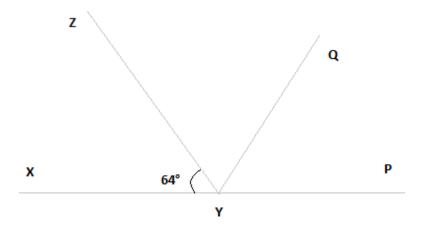
So we get

$$2\angle ROS = \angle QOS - \angle POS$$

Or, 
$$\angle ROS = 1/2 (\angle QOS - \angle POS)$$
(Hence proved).

6. It is given that  $\angle XYZ = 64^{\circ}$  and XY is produced to point P. Draw a figure from the given information. If ray YQ bisects  $\angle ZYP$ , find  $\angle XYQ$  and reflex  $\angle QYP$ .

#### **Solution:**



Here, XP is a straight line

So, 
$$\angle XYZ + \angle ZYP = 180^{\circ}$$

Putting the value of  $\angle XYZ = 64^{\circ}$ , we get

$$64^{\circ} + \angle ZYP = 180^{\circ}$$

From the diagram, we also know that  $\angle ZYP = \angle ZYQ + \angle QYP$ 

Now, as YQ bisects ∠ZYP,

$$\angle ZYQ = \angle QYP$$

Or, 
$$\angle$$
ZYP =  $2\angle$ ZYQ

$$\therefore$$
  $\angle$ ZYQ =  $\angle$ QYP = 58°

Again, 
$$\angle XYQ = \angle XYZ + \angle ZYQ$$



# NCERT Solutions for Class 9 Maths Chapter 6 – Lines and Angles

By putting the value of  $\angle XYZ = 64^{\circ}$  and  $\angle ZYQ = 58^{\circ}$ , we get.

$$\angle XYQ = 64^{\circ} + 58^{\circ}$$

Or, 
$$\angle XYQ = 122^{\circ}$$

Now, reflex 
$$\angle QYP = 180^{\circ} + XYQ$$

We computed that the value of  $\angle XYQ = 122^{\circ}$ .

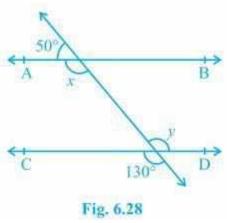
So,

$$\angle QYP = 180^{\circ} + 122^{\circ}$$



EXERCISE: 6.2 (PAGE NO: 103)

1. In Fig. 6.28, find the values of x and y and then show that AB  $\parallel$  CD.



Linguis.

**Solution:** 

We know that a linear pair is equal to  $180^{\circ}$ .

So, 
$$x+50^{\circ} = 180^{\circ}$$

$$\therefore x = 130^{\circ}$$

We also know that vertically opposite angles are equal.

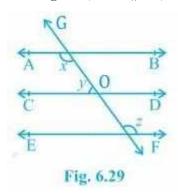
So, 
$$y = 130^{\circ}$$

In two parallel lines, the alternate interior angles are equal. In this,

$$x = y = 130^{\circ}$$

This proves that alternate interior angles are equal, so AB || CD.

2. In Fig. 6.29, if AB || CD, CD || EF and y : z = 3 : 7, find x.



### **Solution:**

It is known that AB || CD and CD||EF

As the angles on the same side of a transversal line sum up to 180°,

$$x + y = 180^{\circ}$$
—(i)



Also,

 $\angle O = z$  (Since they are corresponding angles)

and,  $y + \angle O = 180^{\circ}$  (Since they are a linear pair)

So,  $y+z = 180^{\circ}$ 

Now, let y = 3w and hence, z = 7w (As y : z = 3 : 7)

 $∴ 3w+7w = 180^{\circ}$ 

Or,  $10 \text{ w} = 180^{\circ}$ 

So,  $w = 18^{\circ}$ 

Now,  $y = 3 \times 18^{\circ} = 54^{\circ}$ 

and,  $z = 7 \times 18^{\circ} = 126^{\circ}$ 

Now, angle x can be calculated from equation (i)

 $x+y = 180^{\circ}$ 

Or,  $x+54^{\circ} = 180^{\circ}$ 

 $x = 126^{\circ}$ 

3. In Fig. 6.30, if AB || CD, EF  $\perp$  CD and  $\angle$ GED = 126°, find  $\angle$ AGE,  $\angle$ GEF and  $\angle$ FGE.

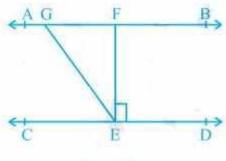


Fig. 6.30

# **Solution:**

Since AB || CD, GE is a transversal.

It is given that  $\angle GED = 126^{\circ}$ 

So,  $\angle GED = \angle AGE = 126^{\circ}$  (As they are alternate interior angles)

Also,

 $\angle GED = \angle GEF + \angle FED$ 

As EF $\perp$  CD,  $\angle$ FED = 90°

 $\therefore \angle GED = \angle GEF + 90^{\circ}$ 

Or,  $\angle GEF = 126^{\circ} - 90^{\circ} = 36^{\circ}$ 



Again,  $\angle$ FGE + $\angle$ GED = 180° (Transversal)

Putting the value of  $\angle GED = 126^{\circ}$ , we get

 $\angle FGE = 54^{\circ}$ 

So,

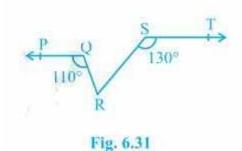
 $\angle AGE = 126^{\circ}$ 

 $\angle GEF = 36^{\circ}$  and

 $\angle FGE = 54^{\circ}$ 

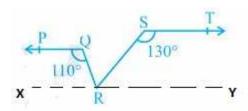
4. In Fig. 6.31, if PQ || ST,  $\angle$ PQR = 110° and  $\angle$ RST = 130°, find  $\angle$ QRS.

[Hint: Draw a line parallel to ST through point R.]



### **Solution:**

First, construct a line XY parallel to PQ.



We know that the angles on the same side of the transversal is equal to 180°.

So,  $\angle PQR + \angle QRX = 180^{\circ}$ 

Or,  $\angle QRX = 180^{\circ}-110^{\circ}$ 

 $\therefore \angle QRX = 70^{\circ}$ 

Similarly,

 $\angle RST + \angle SRY = 180^{\circ}$ 

Or,  $\angle SRY = 180^{\circ} - 130^{\circ}$ 

 $\therefore \angle SRY = 50^{\circ}$ 

Now, for the linear pairs on the line XY-



 $\angle QRX + \angle QRS + \angle SRY = 180^{\circ}$ 

Putting their respective values, we get

$$\angle QRS = 180^{\circ} - 70^{\circ} - 50^{\circ}$$

Hence,  $\angle QRS = 60^{\circ}$ 

5. In Fig. 6.32, if AB || CD,  $\angle$ APQ = 50° and  $\angle$ PRD = 127°, find x and y.

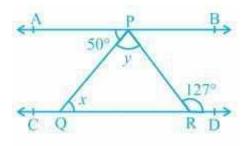


Fig. 6.32

#### **Solution:**

From the diagram,

 $\angle APQ = \angle PQR$  (Alternate interior angles)

Now, putting the value of  $\angle APQ = 50^{\circ}$  and  $\angle PQR = x$ , we get

$$x = 50^{\circ}$$

Also,

 $\angle APR = \angle PRD$  (Alternate interior angles)

Or,  $\angle APR = 127^{\circ}$  (As it is given that  $\angle PRD = 127^{\circ}$ )

We know that

 $\angle APR = \angle APQ + \angle QPR$ 

Now, putting values of  $\angle QPR = y$  and  $\angle APR = 127^{\circ}$ , we get

$$127^{\circ} = 50^{\circ} + y$$

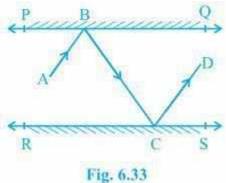
Or, 
$$y = 77^{\circ}$$

Thus, the values of x and y are calculated as:

$$x = 50^{\circ}$$
 and  $y = 77^{\circ}$ 

6. In Fig. 6.33, PQ and RS are two mirrors placed parallel to each other. An incident ray AB strikes the mirror PQ at B, the reflected ray moves along the path BC and strikes the mirror RS at C and again reflects back along CD. Prove that  $AB \parallel CD$ .

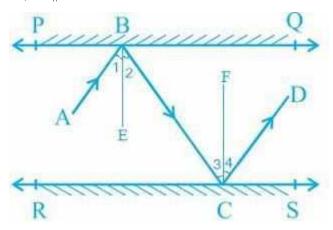




First, draw two lines, BE and CF, such that BE  $\perp$  PQ and CF  $\perp$  RS.

Now, since PQ || RS,

So, BE || CF



We know that,

Angle of incidence = Angle of reflection (By the law of reflection)

So,

 $\angle 1 = \angle 2$  and

 $\angle 3 = \angle 4$ 

We also know that alternate interior angles are equal. Here, BE  $\perp$  CF and the transversal line BC cuts them at B and C

So,  $\angle 2 = \angle 3$  (As they are alternate interior angles)

Now,  $\angle 1 + \angle 2 = \angle 3 + \angle 4$ 

Or,  $\angle ABC = \angle DCB$ 

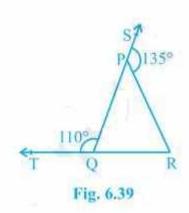
So, AB || CD (alternate interior angles are equal)



**EXERCISE:** 6.3

(PAGE NO: 107)

1. In Fig. 6.39, sides QP and RQ of  $\triangle$ PQR are produced to points S and T,respectively. If  $\angle$ SPR = 135° and  $\angle$ PQT = 110°, find  $\angle$ PRQ.



# **Solution:**

It is given the TQR is a straight line, and so, the linear pairs (i.e. ∠TQP and ∠PQR) will add up to 180°

So,  $\angle TQP + \angle PQR = 180^{\circ}$ 

Now, putting the value of  $\angle TQP = 110^{\circ}$ , we get

 $\angle PQR = 70^{\circ}$ 

Consider the  $\triangle PQR$ ,

Here, the side QP is extended to S, and so ∠SPR forms the exterior angle.

Thus,  $\angle SPR$  ( $\angle SPR = 135^{\circ}$ ) is equal to the sum of interior opposite angles. (Triangle property)

Or,  $\angle PQR + \angle PRQ = 135^{\circ}$ 

Now, putting the value of  $\angle PQR = 70^{\circ}$ , we get

 $\angle PRQ = 135^{\circ}-70^{\circ}$ 

Hence,  $\angle PRQ = 65^{\circ}$ 

2. In Fig. 6.40,  $\angle X = 62^{\circ}$ ,  $\angle XYZ = 54^{\circ}$ . If YO and ZO are the bisectors of  $\angle XYZ$  and  $\angle XZY$ , respectively of  $\Delta$  XYZ, find  $\angle OZY$  and  $\angle YOZ$ .

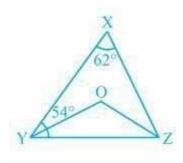


Fig. 6.40



We know that the sum of the interior angles of the triangle.

So, 
$$\angle X + \angle XYZ + \angle XZY = 180^{\circ}$$

Putting the values as given in the question, we get

$$62^{\circ} + 54^{\circ} + \angle XZY = 180^{\circ}$$

Or, 
$$\angle XZY = 64^{\circ}$$

Now, we know that ZO is the bisector, so

$$\angle OZY = \frac{1}{2} \angle XZY$$

$$\therefore$$
  $\angle$ OZY = 32°

Similarly, YO is a bisector, so

$$\angle OYZ = \frac{1}{2} \angle XYZ$$

Or, 
$$\angle OYZ = 27^{\circ} \text{ (As } \angle XYZ = 54^{\circ}\text{)}$$

Now, as the sum of the interior angles of the triangle,

$$\angle OZY + \angle OYZ + \angle O = 180^{\circ}$$

Putting their respective values, we get

$$\angle O = 180^{\circ} - 32^{\circ} - 27^{\circ}$$

Hence, 
$$\angle O = 121^{\circ}$$

3. In Fig. 6.41, if AB || DE,  $\angle$ BAC = 35° and  $\angle$ CDE = 53°, find  $\angle$ DCE.

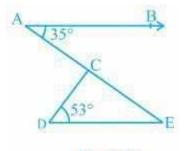


Fig. 6.41

#### **Solution:**

We know that AE is a transversal since AB || DE

Here ∠BAC and ∠AED are alternate interior angles.

Hence,  $\angle BAC = \angle AED$ 

It is given that  $\angle BAC = 35^{\circ}$ 

$$\angle AED = 35^{\circ}$$

Now consider the triangle CDE. We know that the sum of the interior angles of a triangle is 180°.

$$\therefore \angle DCE + \angle CED + \angle CDE = 180^{\circ}$$

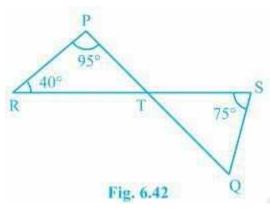


Putting the values, we get

$$\angle DCE+35^{\circ}+53^{\circ}=180^{\circ}$$

Hence,  $\angle DCE = 92^{\circ}$ 

4. In Fig. 6.42, if lines PQ and RS intersect at point T, such that  $\angle PRT = 40^{\circ}$ ,  $\angle RPT = 95^{\circ}$  and  $\angle TSQ = 75^{\circ}$ , find  $\angle SQT$ .



# **Solution:**

Consider triangle PRT.

$$\angle PRT + \angle RPT + \angle PTR = 180^{\circ}$$

So, 
$$\angle PTR = 45^{\circ}$$

Now ∠PTR will be equal to ∠STQ as they are vertically opposite angles.

So, 
$$\angle PTR = \angle STQ = 45^{\circ}$$

Again, in triangle STQ,

$$\angle TSQ + \angle PTR + \angle SQT = 180^{\circ}$$

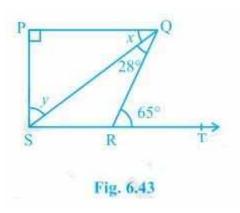
Solving this, we get

$$74^{\circ} + 45^{\circ} + \angle SQT = 180^{\circ}$$

$$\angle SQT = 60^{\circ}$$

5. In Fig. 6.43, if PQ  $\perp$  PS, PQ  $\parallel$  SR,  $\angle$ SQR = 28° and  $\angle$ QRT = 65°, then find the values of x and y.





 $x + \angle SQR = \angle QRT$  (As they are alternate angles since QR is transversal)

So, 
$$x+28^{\circ} = 65^{\circ}$$

$$\therefore x = 37^{\circ}$$

It is also known that alternate interior angles are the same, and so

$$\angle$$
QSR = x = 37°

Also, now

 $\angle QRS + \angle QRT = 180^{\circ}$  (As they are a Linear pair)

Or, 
$$\angle QRS+65^{\circ} = 180^{\circ}$$

So, 
$$\angle QRS = 115^{\circ}$$

Using the angle sum property in  $\Delta$  SPQ,

$$\angle SPQ + x + y = 180^{\circ}$$

Putting their respective values, we get

$$90^{\circ} + 37^{\circ} + y = 180^{\circ}$$

$$y = 180^{\circ} - 127^{\circ} = 53^{\circ}$$

Hence, 
$$y = 53^{\circ}$$

6. In Fig. 6.44, the side QR of  $\triangle$ PQR is produced to a point S. If the bisectors of  $\angle$ PQR and  $\angle$ PRS meet at point T, then prove that  $\angle$ QTR =  $\frac{1}{2}$   $\angle$ QPR.



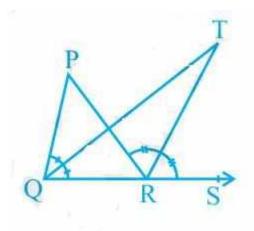


Fig. 6.44

Consider the  $\triangle PQR$ .  $\angle PRS$  is the exterior angle, and  $\angle QPR$  and  $\angle PQR$  are the interior angles.

So,  $\angle PRS = \angle QPR + \angle PQR$  (According to triangle property)

Or,  $\angle PRS - \angle PQR = \angle QPR$  ———(i)

Now, consider the  $\Delta QRT$ ,

 $\angle TRS = \angle TQR + \angle QTR$ 

Or,  $\angle QTR = \angle TRS - \angle TQR$ 

We know that QT and RT bisect ∠PQR and ∠PRS, respectively.

So,  $\angle PRS = 2 \angle TRS$  and  $\angle PQR = 2 \angle TQR$ 

Now,  $\angle QTR = \frac{1}{2} \angle PRS - \frac{1}{2} \angle PQR$ 

Or,  $\angle QTR = \frac{1}{2} (\angle PRS - \angle PQR)$ 

From (i), we know that  $\angle PRS - \angle PQR = \angle QPR$ 

So,  $\angle QTR = \frac{1}{2} \angle QPR$  (hence proved).