

# **EXERCISE 6.4**

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- 1. Is it possible to have a triangle with the following sides?
- (i) 2 cm, 3 cm, 5 cm

#### Solution:-

Clearly, we have

$$(2 + 3) = 5$$

$$5 = 5$$

Thus, the sum of any two of these numbers is not greater than the third.

Hence, it is not possible to draw a triangle whose sides are 2 cm, 3 cm and 5 cm.

# (ii) 3 cm, 6 cm, 7 cm

#### Solution:-

Clearly, we have

$$(3 + 6) = 9 > 7$$

$$(6 + 7) = 13 > 3$$

$$(7 + 3) = 10 > 6$$

Thus, the sum of any two of these numbers is greater than the third.

Hence, it is possible to draw a triangle whose sides are 3 cm, 6 cm and 7 cm.

# (iii) 6 cm, 3 cm, 2 cm

#### Solution:-

Clearly, we have

$$(3 + 2) = 5 < 6$$

Thus, the sum of any two of these numbers is less than the third.

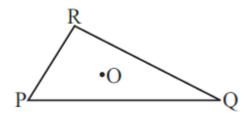
Hence, it is not possible to draw a triangle whose sides are 6 cm, 3 cm and 2 cm.

2. Take any point O in the interior of a triangle PQR. Is



(i) 
$$OP + OQ > PQ$$
?

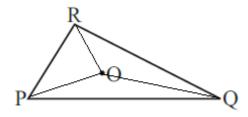
(ii) 
$$OQ + OR > QR$$
?



# Solution:-

If we take any point O in the interior of a triangle PQR and join OR, OP, OQ.

Then, we get three triangles  $\triangle OPQ$ ,  $\triangle OQR$  and  $\triangle ORP$  are shown in the figure below.



We know that,

The sum of the length of any two sides is always greater than the third side.

(i) Yes, ΔOPQ has sides OP, OQ and PQ.

(ii) Yes, ΔOQR has sides OR, OQ and QR.

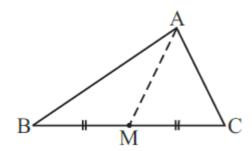
(iii) Yes, ΔORP has sides OR, OP and PR.

3. AM is a median of a triangle ABC.

Is 
$$AB + BC + CA > 2 AM$$
?

(Consider the sides of triangles  $\triangle$ ABM and  $\triangle$ AMC.)





# Solution:-

We know that,

The sum of the length of any two sides is always greater than the third side.

Now consider the  $\triangle ABM$ ,

Here, AB + BM > AM ... [equation i]

Then, consider the  $\triangle ACM$ 

Here, AC + CM > AM ... [equation ii]

By adding equations [i] and [ii], we get,

AB + BM + AC + CM > AM + AM

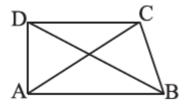
From the figure we have, BC = BM + CM

AB + BC + AC > 2 AM

Hence, the given expression is true.

4. ABCD is a quadrilateral.

Is AB + BC + CD + DA > AC + BD?



#### Solution:-

We know that,

The sum of the length of any two sides is always greater than the third side.

Now consider the  $\triangle ABC$ ,



Here, AB + BC > CA ... [equation i]

Then, consider the ΔBCD

Here, BC + CD > DB ... [equation ii]

Consider the ACDA

Here, CD + DA > AC ... [equation iii]

Consider the  $\Delta DAB$ 

Here, DA + AB > DB ... [equation iv]

By adding equations [i], [ii], [iii] and [iv], we get,

AB + BC + BC + CD + CD + DA + DA + AB > CA + DB + AC + DB

2AB + 2BC + 2CD + 2DA > 2CA + 2DB

Take out 2 on both the side,

2(AB + BC + CA + DA) > 2(CA + DB)

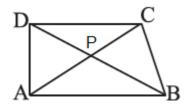
AB + BC + CA + DA > CA + DB

Hence, the given expression is true.

5. ABCD is quadrilateral. Is AB + BC + CD + DA < 2 (AC + BD)

# Solution:-

Let us consider ABCD as a quadrilateral, and P is the point where the diagonals intersect. As shown in the figure below.



We know that,

The sum of the length of any two sides is always greater than the third side.

Now consider the  $\triangle PAB$ ,

Here, PA + PB < AB ... [equation i]



Then, consider the ΔPBC

Here, PB + PC < BC ... [equation ii]

Consider the APCD

Here, PC + PD < CD ... [equation iii]

Consider the APDA

Here, PD + PA < DA ... [equation iv]

By adding equations [i], [ii], [iii] and [iv], we get,

PA + PB + PB + PC + PC + PD + PD + PA < AB + BC + CD + DA

2PA + 2PB + 2PC + 2PD < AB + BC + CD + DA

2PA + 2PC + 2PB + 2PD < AB + BC + CD + DA

2(PA + PC) + 2(PB + PD) < AB + BC + CD + DA

From the figure, we have, AC = PA + PC and BD = PB + PD

Then,

2AC + 2BD < AB + BC + CD + DA

2(AC + BD) < AB + BC + CD + DA

Hence, the given expression is true.

# 6. The lengths of two sides of a triangle are 12 cm and 15 cm. Between what two measures should the length of the third side fall?

# Solution:-

We know that,

The sum of the length of any two sides is always greater than the third side.

From the question, it is given that two sides of the triangle are 12 cm and 15 cm.

So, the third side length should be less than the sum of the other two sides,

12 + 15 = 27 cm

Then, it is given that the third side can not be less than the difference of the two sides, 15 - 12 = 3 cm

So, the length of the third side falls between 3 cm and 27 cm.