EXERCISE 2.6

Solve the following equations.

1.
$$(8x - 3)/3x = 2$$

Solution:

$$(8x - 3)/3x = 2$$

$$\Rightarrow 8x/3x - 3/3x = 2$$

$$\Rightarrow$$
 8/3 - 1/x = 2

$$\Rightarrow$$
 8/3 - 2 = 1/x

$$\Rightarrow$$
 $(8-6)/3 = 1/x$

$$\Rightarrow 2/3 = 1/x$$

$$\Rightarrow$$
 x = 3/2

$$2.9x/(7-6x)=15$$

Solution:

$$9x/(7-6x) = 15$$

$$\Rightarrow$$
 9x = 15(7 - 6x)

$$\Rightarrow$$
 9x = 105 - 90x

$$\Rightarrow$$
 9x + 90x = 105

$$\Rightarrow$$
 99x = 105

$$\Rightarrow$$
 x = 105/99 = 35/33

3.
$$z/(z + 15) = 4/9$$

Solution:

$$z/(z + 15) = 4/9$$

$$\Rightarrow$$
 z = 4/9 (z + 15)

$$\Rightarrow$$
 9z = 4(z + 15)

$$\Rightarrow$$
 9z = 4z + 60

$$\Rightarrow$$
 9z - 4z = 60

$$\Rightarrow 5z = 60$$

$$\Rightarrow$$
 z = 12

4.
$$(3y + 4)/(2 - 6y) = -2/5$$

Solution:

$$(3y + 4)/(2 - 6y) = -2/5$$

$$\Rightarrow$$
 3y + 4 = -2/5 (2 - 6y)

$$\Rightarrow$$
 5(3y + 4) = -2(2 - 6y)

$$\Rightarrow 15y + 20 = -4 + 12y$$

$$\Rightarrow 15y - 12y = -4 - 20$$

$$\Rightarrow$$
 3y = -24

$$\Rightarrow$$
 y = -8

5.
$$(7y + 4)/(y + 2) = -4/3$$

Solution:

$$(7y + 4)/(y + 2) = -4/3$$

$$\Rightarrow$$
 7y + 4 = -4/3 (y + 2)

$$\Rightarrow$$
 3(7y + 4) = -4(y + 2)

$$\Rightarrow$$
 21y + 12 = -4y - 8

$$\Rightarrow$$
 21y + 4y = -8 - 12

$$\Rightarrow 25y = -20$$

$$\Rightarrow$$
 y = -20/25 = -4/5

6. The ages of Hari and Harry are in the ratio of 5:7. Four years from now, the ratio of their ages will be 3:4. Find their present ages.

Solution:

Let the age of Hari be 5x and Harry be 7x. 4 years later,

Age of Hari =
$$5x + 4$$

Age of Harry =
$$7x + 4$$

According to the question,

$$(5x + 4)/(7x + 4) = \frac{3}{4}$$

$$\Rightarrow 4(5x + 4) = 3(7x + 4)$$

$$\Rightarrow 20x + 16 = 21x + 12$$

$$\Rightarrow 21x - 20x = 16 - 12$$

$$\Rightarrow x = 4$$

Hari's age =
$$5x = 5 \times 4 = 20$$
 years

Harry's age =
$$7x = 7 \times 4 = 28$$
 years

7. The denominator of a rational number is greater than its numerator by 8. If the numerator is increased by 17 and the denominator is decreased by 1, the number obtained is 3/2. Find the rational number.

Solution:

Let the numerator be x, then the denominator will be (x + 8)

According to the question,

$$(x + 17)/(x + 8 - 1) = 3/2$$

$$\Rightarrow$$
 (x + 17)/(x + 7) = 3/2

$$\Rightarrow 2(x+17) = 3(x+7)$$

$$\Rightarrow 2x + 34 = 3x + 21$$

$$\Rightarrow$$
 34 - 21 = 3x - 2x

$$\Rightarrow 13 = x$$

The rational number is x/(x + 8) = 13/21