

Welcome to



States of matter





Something  
that occupies  
**space** and  
has **mass**

# States of Matter

# Bulk Properties



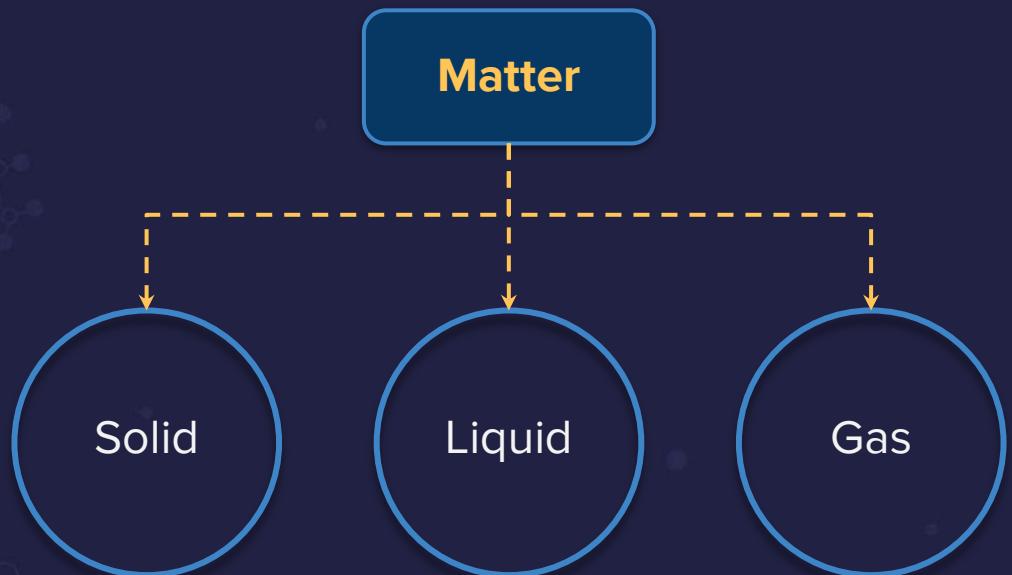
Most of the **observable characteristics** of chemical systems represent **bulk properties** of matter



Properties associated with a **collection of a large number of atoms, ions or molecules**



# Classification of Matter



**States of Matter** depends upon **Intermolecular forces** & **thermal energy**

# Intermolecular Forces

Intermolecular  
Forces

Attractive

Repulsive

# Intermolecular Attractive Forces

## Attractive Forces

Dipole-dipole attraction

Between polar and non-polar molecules

Dipole-induced dipole attraction

Between polar molecules

Between non-polar molecules

Instantaneous dipole-induced dipole attraction

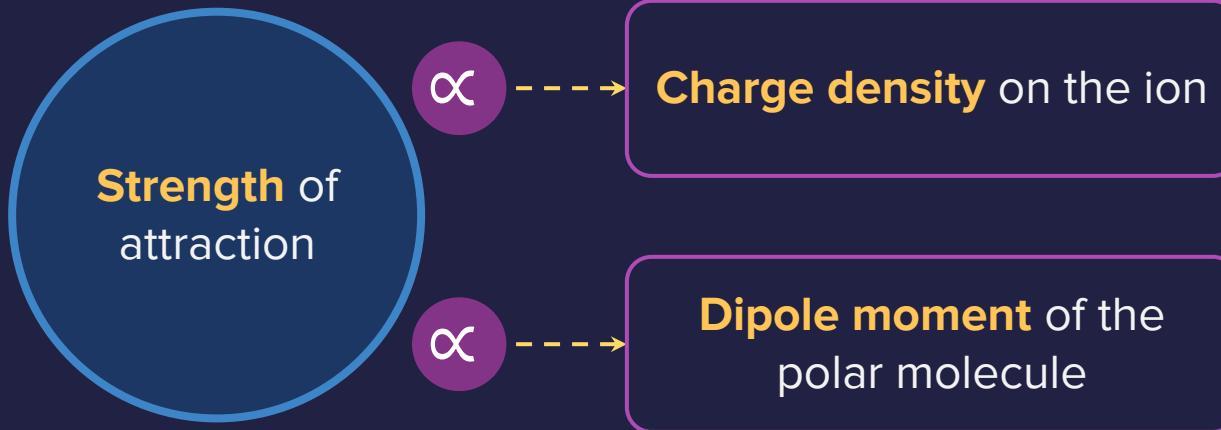
Between ion and polar molecule

Ion-dipole attraction

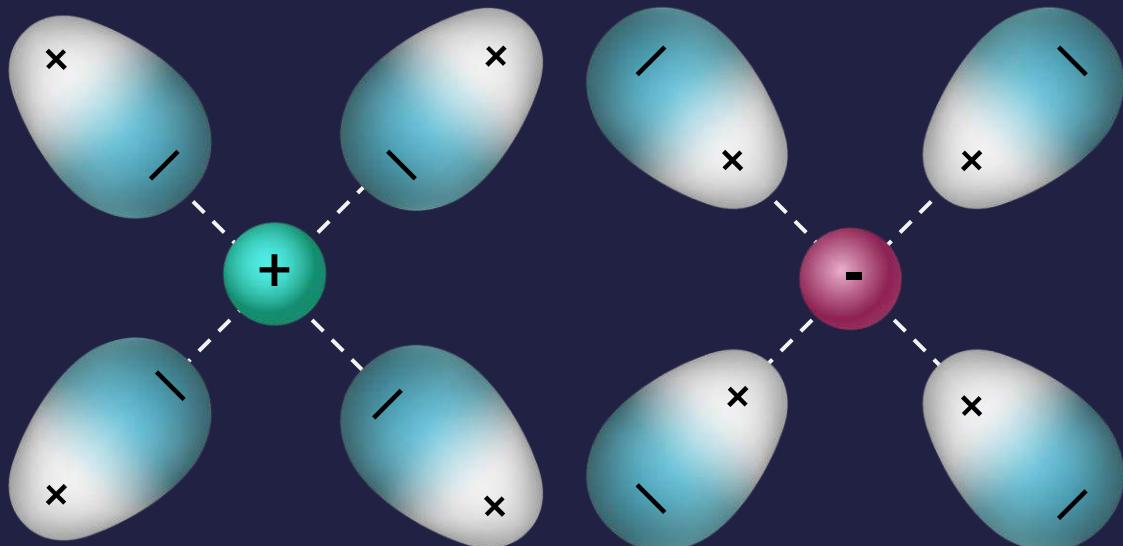
Ion-induced dipole attraction

Between ion and non-polar molecule

# Ion-Dipole Attraction



# Ion-Dipole Attraction



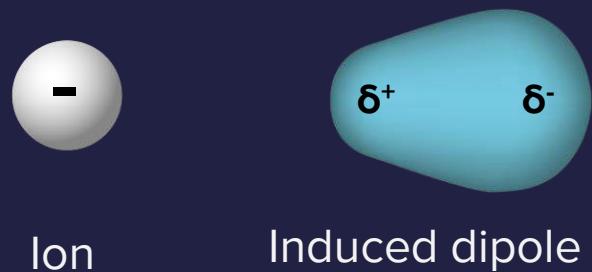
Cation-dipole  
attractions

Anion-dipole  
attractions

# Ion - Induced Dipole Attraction



# Ion - Induced Dipole Attraction



# van der Waals Forces

## van der Waals forces

Dipole-dipole  
forces

Dipole-induced  
dipole forces

Dispersion  
forces

Keesom forces

Debye forces

London forces



# Dipole-Dipole Attraction

Exists between **polar molecules**



**Electrostatic attractions** between the **oppositely charged** ends of permanent dipoles



Due to this force, gases can be **liquified**



# Dipole-Dipole Attraction

For stationary polar molecules

$$\text{Interaction energy} \propto \frac{1}{r^3}$$

For rotating polar molecules

$$\text{Interaction energy} \propto \frac{1}{r^6}$$

**r**

Distance between the polar molecules

# Dipole-Induced Dipole Attraction

Exists between a **polar** and a **non-polar molecule**



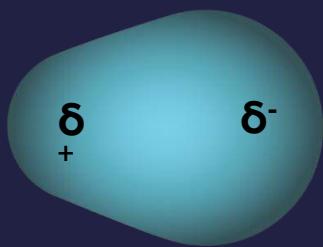
Permanent dipole **deforms the electron cloud** of the non polar molecule



**Induced dipole** gets developed in the non polar molecule



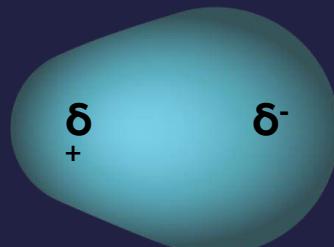
# Dipole-Induced Dipole Attraction



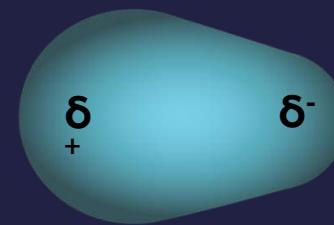
Permanent  
dipole



Non-polar  
species



Permanent  
dipole



Induced  
dipole



**Induced dipole moment**  
depends upon

Dipole moment present in  
the **permanent dipole**

**Polarizability** of the  
non-polar molecule



# Dipole-Dipole Attraction

Exists between **polar molecules**



**Electrostatic attractions** between the **oppositely charged** ends of permanent dipoles



Due to this force, gases can be **liquified**



# Dispersion Forces

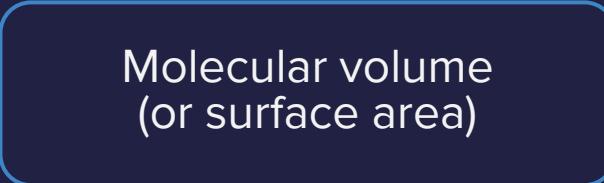


$\propto$



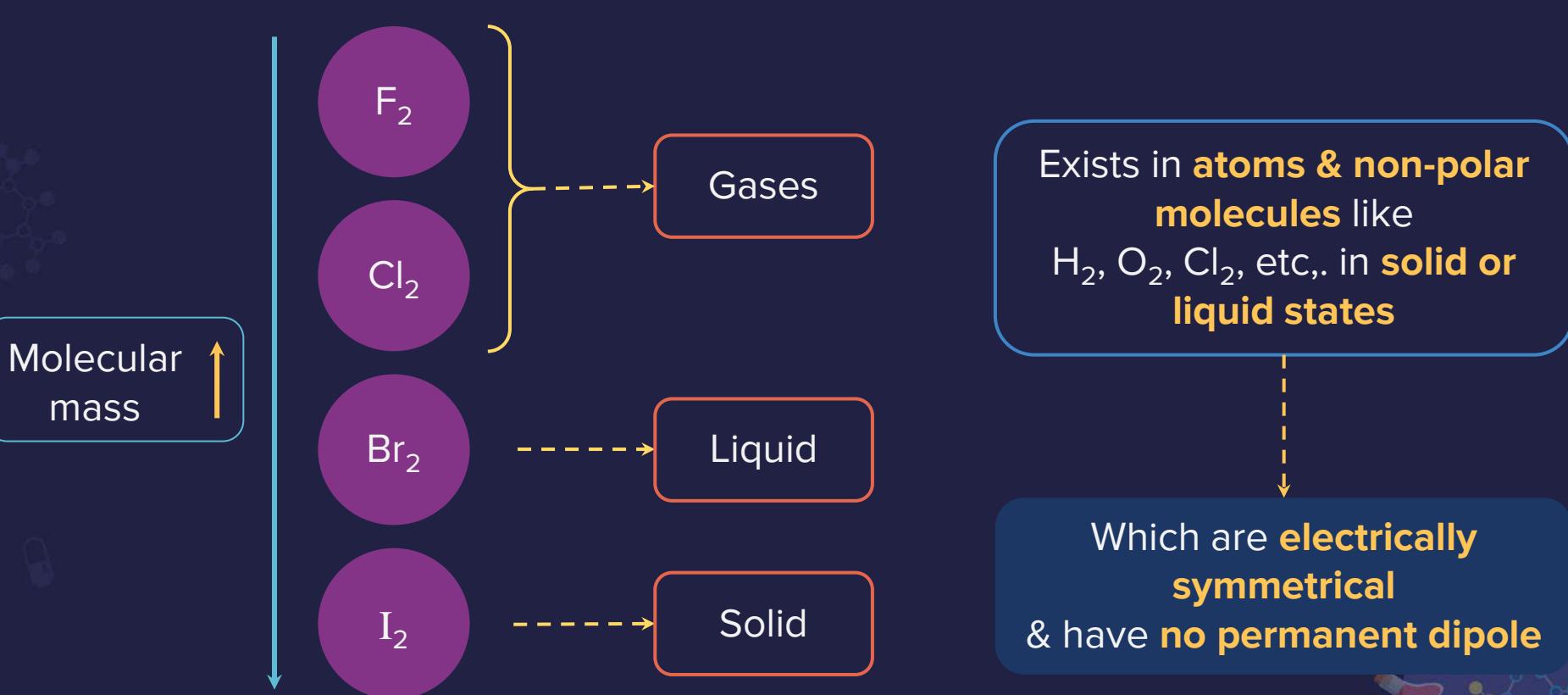
Molecular mass

$\propto$



Molecular volume  
(or surface area)

# Dispersion Forces



# Strength of London Forces

If **molecular mass** is **same**, then the factor responsible is **molecular surface area**

van der Waals force

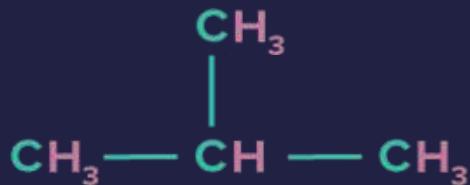
$\propto$

Surface area

# Strength of London Forces



A



B

Surface Area

A

>

B

Boiling Point

A

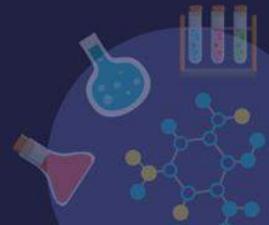
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B



# Interaction Energy v/s Distance

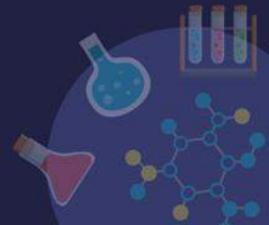
Type of interaction	Interaction energy $\propto \frac{1}{r^x}$
Ionic bond	$\frac{1}{r}$
Ion-dipole	$\frac{1}{r^2}$
Dipole-dipole	$\frac{1}{r^3}$





# Interaction Energy v/s Distance

Type of interaction	Interaction energy $\propto \frac{1}{r^x}$
Ion-induced dipole	$\frac{1}{r^4}$
Dipole-induced dipole	$\frac{1}{r^6}$
London forces	$\frac{1}{r^6}$



# Strength of Intermolecular Forces

Ion-dipole attraction

Dipole-dipole attraction

Ion-induced dipole attraction

Dipole-induced dipole attraction

Instantaneous dipole - induced dipole attraction

Strength ↓

# Thermal Energy

Energy of a body arising from **motion of its atoms or molecules**

It is the measure of **average K.E.** of the particles of the matter

Thermal Energy

$\propto$

Temperature (T)  
of substance



# Intermolecular Forces vs Thermal Energy

**Intermolecular forces** tend to keep the **molecules together** but

**Thermal energy** tends to **keep them apart**

The result of balance between these two forces

**Three states of matter**



# Intermolecular Forces vs Thermal Energy

Gas → Liquid → Solid

Predominance of **intermolecular Forces**

Gas ← Liquid ← Solid

Predominance of **thermal Energy**

# General Properties of Gaseous State

01

No fixed **shape & volume**

02

Much **lower density** than the  
solids & liquids

03

Weak forces of **attraction**

04

Exerts **pressure** equally in all  
directions

05

Infinite **expansibility** & high  
**compressibility**

06

Forms **homogeneous mixtures**

# Pressure

**Pressure** of the gas is the force exerted by the gas per unit area on the walls of the container in all directions.

## Pressure (P)

1 atm

=

$1.01325 \times 10^5$  Pa

1 bar

=

$10^5$  Pa = 750 torr = 750 mm of Hg

1 atm

=

760 torr = 760 mm of Hg = 76 cm of Hg

1 atm

=

1.01325 bar

1 N/m<sup>2</sup>

=

1 Pa = 10 dyne/cm<sup>2</sup>

# Volume & Temperature

## Volume (V)

The **volume** of the container is the volume of the gas sample as gases occupy the entire space available to them.

1 m<sup>3</sup>

=

10<sup>3</sup> L

1 L

=

10<sup>3</sup> cm<sup>3</sup> or c.c. or mL

1 m<sup>3</sup>

=

10<sup>6</sup> cm<sup>3</sup>

## Temperature (T)

**Temperature** is the measure of hotness of the system.

T (K)

=

t (°C) + 273.15

# Standard Temperature & Pressure (STP)

$$\left. \begin{array}{l} T = 273.15 \text{ K} \\ P = 1 \text{ bar} \end{array} \right\} \text{STP}$$

$$\text{Molar Volume of an ideal gas} = 22.71098 \text{ L mol}^{-1}$$

# Gas Laws



Behaviour of gases is governed by some laws

Relationships between measurable properties  
**pressure, volume, temperature & amount** of gases

Interdependent properties,  
**describes the state of the gas**

# Gas Laws

Boyle's Law

Charles' Law

**Gas laws**

Gay - Lussac's Law

Avogadro's Law

# Boyle's Law

P

$\propto$

$\frac{1}{V}$

- T = Constant
- Amount of gas = Constant

At **constant temperature**

The **volume** of a fixed amount  
(number of moles 'n') of gas **varies  
inversely with its pressure**

# Boyle's Law

$P$

$\propto$

$\frac{1}{V}$

(n, T constant)

$P$

$=$

$k_1 \frac{1}{V}$



$PV$

$=$

$k_1$

$P_1 V_1$

$=$

$P_2 V_2$

or

$\frac{P_1}{P_2}$

$=$

$\frac{V_2}{V_1}$

$k_1$  depends on **amount** &  
**temperature (T)** of gas

# Pressure-Density Relation

According to Boyle's law,

$$P$$

$$=$$

$$k_1 \frac{1}{V}$$

Density (d) is given by,

$$d$$

$$=$$

$$\frac{m}{V}$$

**m**

Mass

**V**

Volume

# Pressure-Density Relation



$$d = \frac{m \times P}{k_1}$$

$$d = \left(\frac{m}{k_1}\right) P$$

$$d = k' P$$

(n, T constant)

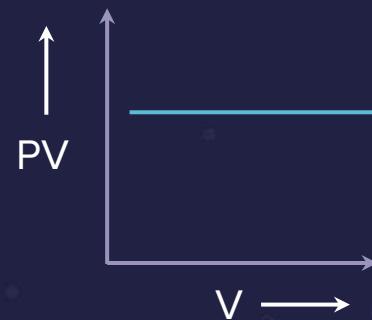
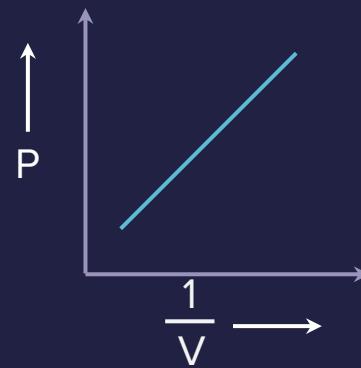
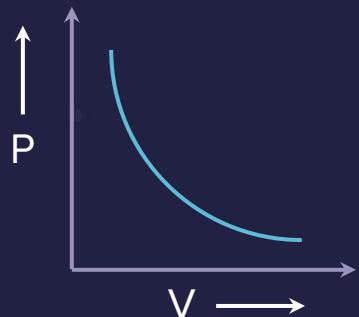
$$d \propto P$$

**Pressure ↑**

Gases become denser  
( **Density ↑** )

Same number of  
molecules  
occupy smaller space

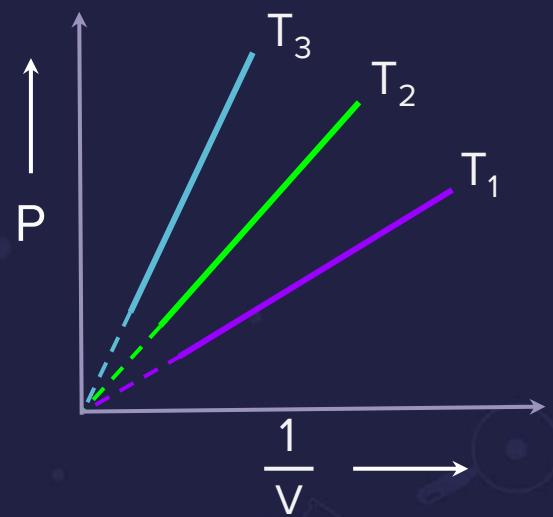
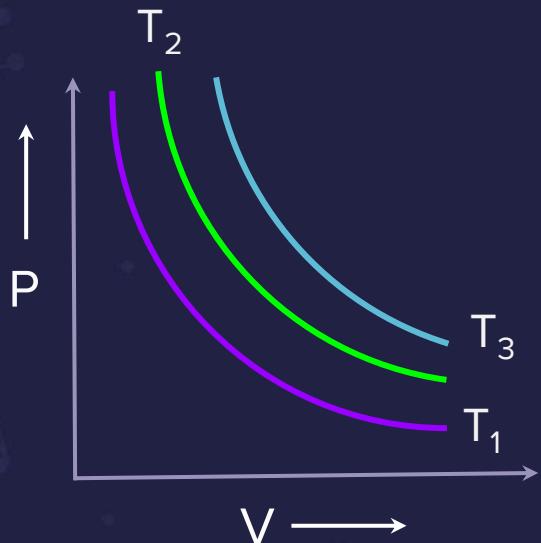
# Boyle's Law



# Boyle's Law at Different Temperatures

P-V Isotherms

Constant temperature curves



$T_3 > T_2 > T_1$

# Charles' Law

V

$\propto$

T

At **constant pressure**

The **volume** of a fixed amount of gas is directly proportional to its **absolute temperature**.

- P = Constant
- Amount of gas = constant

# Charles' Law

V

$\propto$

T

(P, n constant)

$k_2$  depends on the  
**amount** & **P** of the gas

V

=

$k_2 T$

$\frac{V}{T}$

=

$k_2$

$\frac{V_2}{V_1}$

=

$\frac{T_2}{T_1}$

# Charles' Law

For **each degree** rise in **temperature**, the **volume** of a gas **increases** by **1/273.15** of the original volume of the gas at 0 °C.

$$V_t$$

=

$$V_o + \frac{t}{273.15} V_o$$

$$V_t$$

=

$$V_o \left[ 1 + \frac{t}{273.15} \right]$$

$$V_t$$

=

$$V_o \left[ \frac{t + 273.15}{273.15} \right]$$

$$V_o$$

Initial volume  
(at 0 °C )

$$V_t$$

Final volume  
(at t °C )

# Charles' Law

$$V_t = V_o + \frac{t}{273.15} V_o$$

$$V_t = V_o \left[ 1 + \frac{t}{273.15} \right]$$

$$V_t = V_o \left[ \frac{t + 273.15}{273.15} \right]$$

$V_o$

Initial volume  
(at 0 °C)

$V_t$

Final volume  
(at t °C)

# Absolute Scale of Temperature

$$V_t = V_o \left( \frac{T_t}{T_o} \right)$$

T

Absolute scale or Kelvin scale or  
thermodynamic scale of temperature

$t^{\circ}\text{C}$

$\Rightarrow$

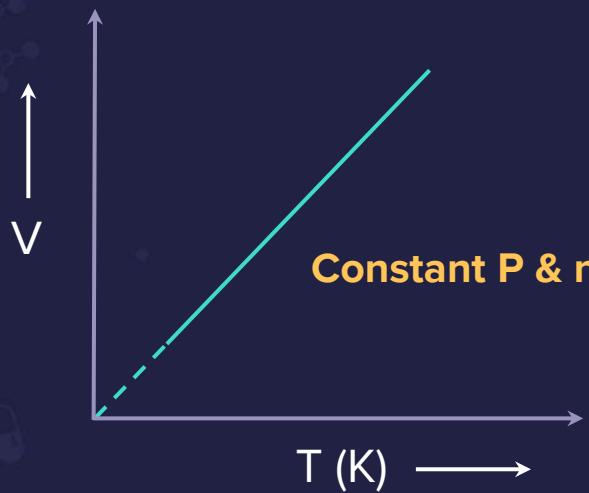
$T_t$

$=$

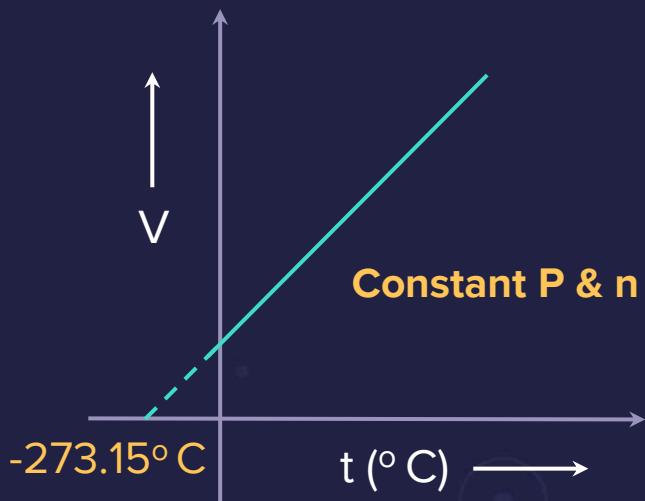
$(273.15 + t) \text{ K}$

# Charles' Law

Volume vs Temperature (K)



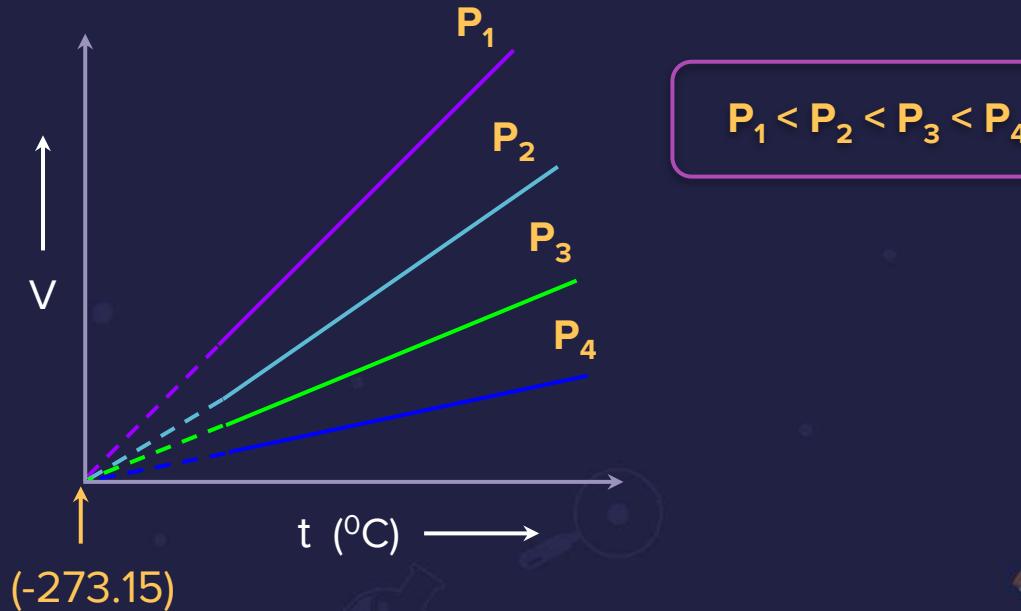
Volume vs Temperature ( $^{\circ}\text{C}$ )



# Charles' Law

T - V Isobars

Constant pressure curves

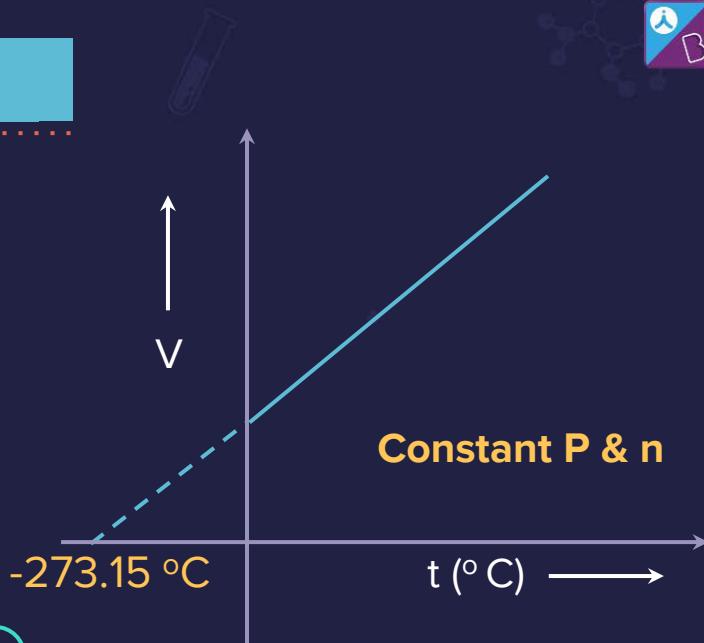


# What Happens at Absolute Zero?

$$V_t = V_o \left[ \frac{t + 273.15}{273.15} \right]$$

Let value of  $t = -273.15$

$$V_t = V_o \left[ \frac{-273.15 + 273.15}{273.15} \right] = 0$$



It means volume of gas becomes zero at -273.15 °C

# Volume of Gas is Zero!

**Absolute zero**

Lowest **hypothetical** or imaginary T at which gases supposedly occupy **zero volume**

Gas will **not exist**

All the gases get **liquified** before this temperature is reached

# Applications of Charles' Law

Athletes find it more difficult to perform in winter season!!!

When the weather is **cool**

the capacity of human lungs **decreases**

# Gay-Lussac's Law

$$P \propto T$$

- $V = \text{Constant}$
- Amount of gas = Constant

At **constant volume**

The **pressure** of a fixed amount of a gas is **directly proportional to the temperature**.

# Gay-Lussac's Law

P

$\propto$

T

(V, n constant)

P

=

$k_3 T$

----->

$\frac{P}{T}$

=

$k_3$

$\frac{P_1}{T_1}$

=

$\frac{P_2}{T_2}$

=

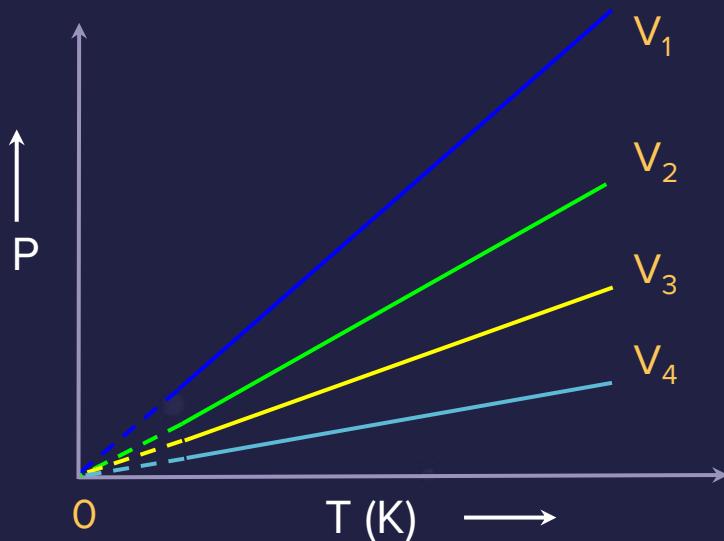
$k_3$

$k_3$  depends on **amount** & **V** of gas

# Gay-Lussac's Law

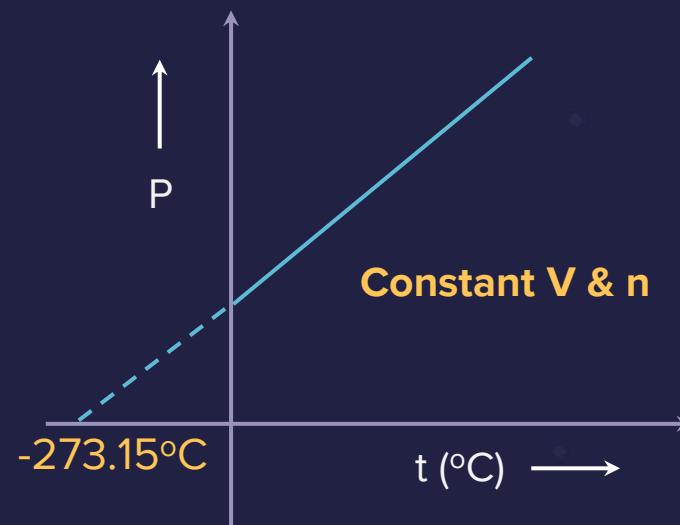
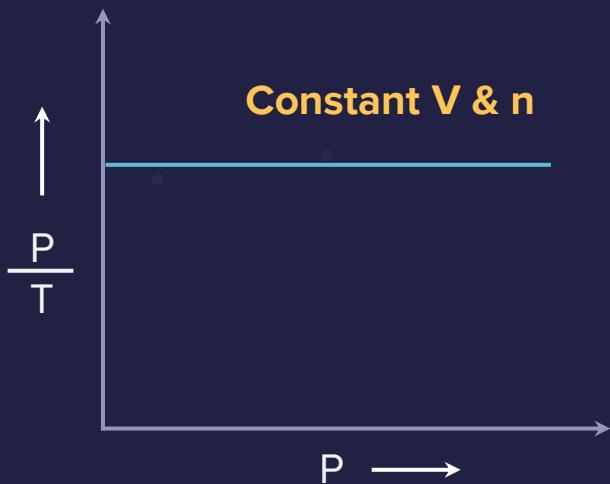
P - T **Isochores**

Constant volume curves



$$V_1 < V_2 < V_3 < V_4$$

# Gay-Lussac's Law



# Avogadro's Law

$$V \propto n$$

- Same conditions of P & T

Same **conditions of P & T**

**Equal volume** of all gases contains **equal number of molecules**

# Avogadro's Law

V

 $\propto$ 

n

( P , T constant )

V

=

 $k_4 n$ 

-----&gt;

 $\frac{V}{n}$ 

=

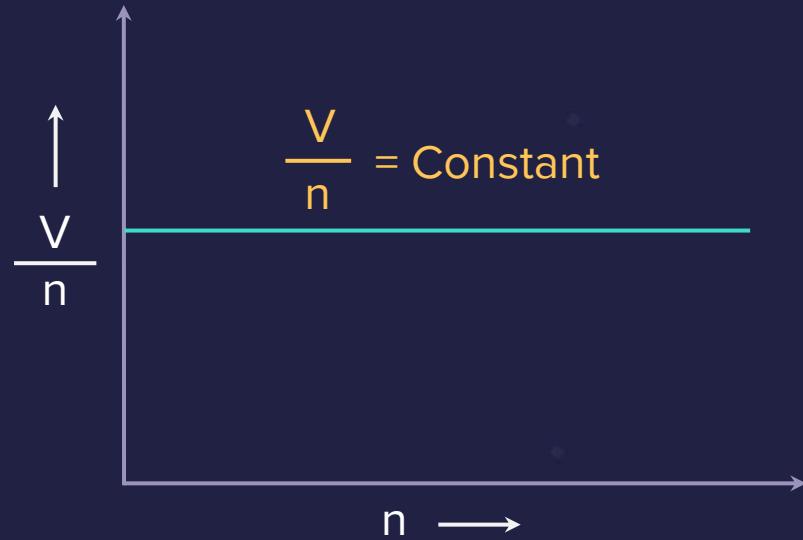
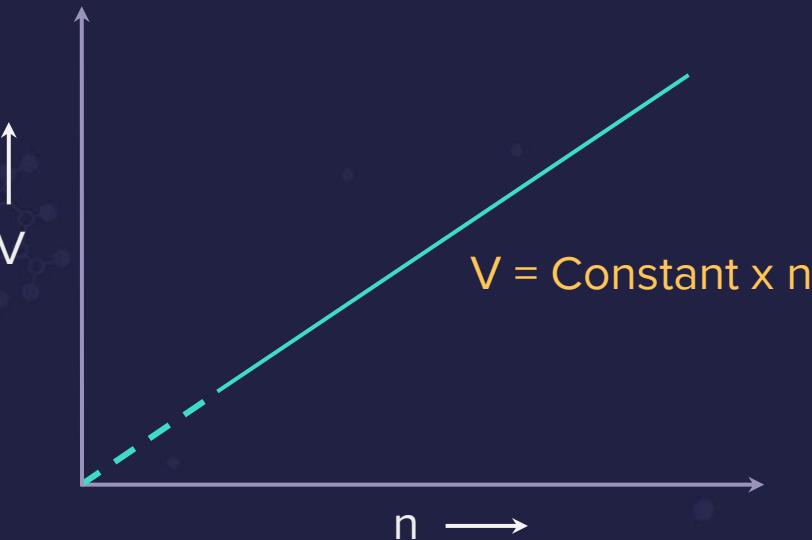
 $k_4$  $\frac{V_1}{n_1}$ 

=

 $\frac{V_2}{n_2}$ 

$k_4$  depends on P & T of gas

# Avogadro's Law



# Combining Different Gas Laws

$$V \propto \frac{1}{P}$$

**Boyle's Law**

At constant n, T

**Charles' Law**

$$V \propto T$$

At constant n, P

$$V \propto n$$

**Avogadro's Law**

At constant T, P

**Gay Lussac's Law**

$$P \propto T$$

At constant n, V

# Combining Different Gas Laws

$$\Rightarrow V = \frac{nT}{P}$$

Universal Gas Constant

**Ideal gas equation**

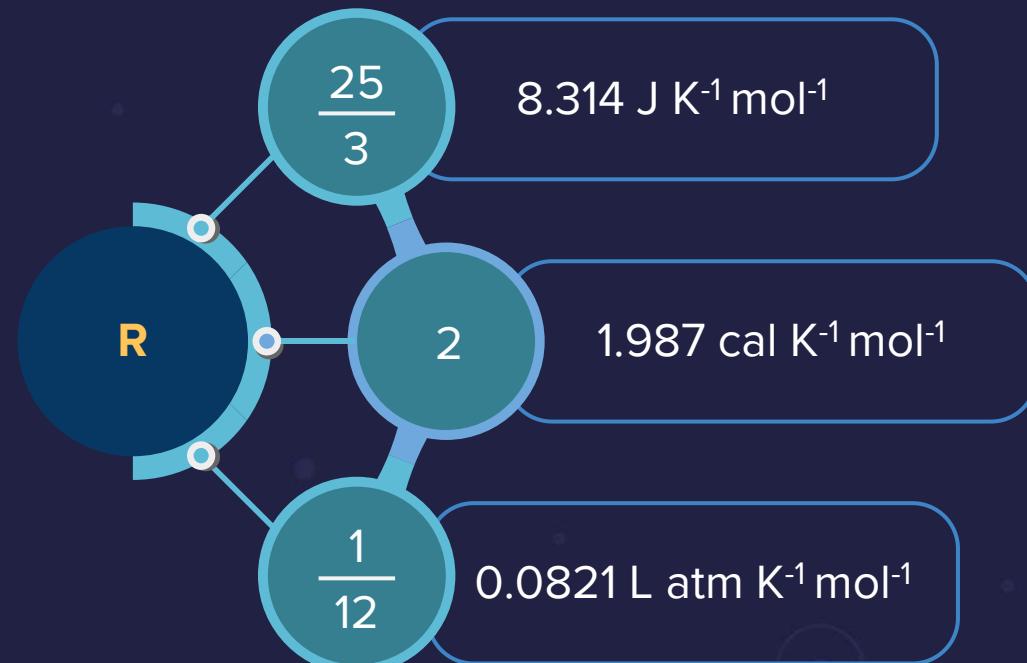
$$PV = nRT$$

**Remember!**

**Ideal gas** is hypothetical.  
The **real gas** follows the gas laws and ideal gas equation only under specific condition (**Low P and high T**).

**Ideal gas equation ( $PV = nRT$ )**  
is a relation between four variables and it describes the state of any ideal gas. Due to this, it is also known as the **equation of state**.

# Values of R



# Ideal Gas Equation in Terms of Density

$$PV = nRT$$

$$n = \frac{m}{M}$$

$$PV = \frac{m}{M} RT$$

$$PM = \frac{m}{V} RT$$

$$PM = dRT$$

- $m$  = Mass of gas
- $M$  = Molar mass of gas
- $V$  = Volume of the gas
- $d$  = Density of gas

$$d = \frac{m}{V}$$

# Density of Gases on Compression

Pressure ↑

Balloon squeezes

Volume of  
gas inside it ↓

Pressure  
inside ↑

Gases become denser ( Density ↑ )

As the balloon cannot  
withstand  
the added pressure, it  
bursts

Same number of molecules  
occupy smaller space

# Partial Pressure of a Gas Component

The pressure that a **component** of gas would exert if it

occupies the **same volume** as the **mixture** at the same temperature

Mixture of non reacting gases



# Dalton's Law of Partial Pressures

For a **non reacting** gaseous mixture **total pressure** of the mixture is the **summation of partial pressure** of the different component gases.

$$P_T = P_1 + P_2 + \dots$$

Partial pressure of a gas is **independent** of the other gases present in the mixture

# Partial Pressure in Terms of Mole Fraction

- Suppose at temperature T, three gases enclosed in volume V, exert partial pressures  $P_1$ ,  $P_2$  and  $P_3$

$$\begin{array}{ccc} P_1 & = & \frac{n_1 RT}{V} \\ P_2 & = & \frac{n_2 RT}{V} \\ P_3 & = & \frac{n_3 RT}{V} \end{array}$$

# Partial Pressure in Terms of Mole Fraction



Dalton's law

$$P_{\text{Total}} = P_1 + P_2 + P_3$$

$$P_{\text{Total}} = \frac{n_1 RT}{V} + \frac{n_2 RT}{V} + \frac{n_3 RT}{V}$$

$$P_{\text{Total}} = (n_1 + n_2 + n_3) \frac{RT}{V}$$

$$n_{\text{Total}} = n_1 + n_2 + n_3$$

# Partial Pressure in Terms of Mole Fraction

On dividing  $P_1$  by  $P_{\text{Total}}$ ,

$$\frac{P_1}{P_{\text{Total}}} = \frac{n_1}{n_1 + n_2 + n_3} \times \frac{RT}{V} \times \frac{V}{RT}$$

$$\frac{P_1}{P_{\text{Total}}} = \frac{n_1}{n_{\text{Total}}} = x_1$$

$x_1$  Mole fraction of gas 1

# Partial Pressure in Terms of Mole Fraction

Similarly,

$$\frac{P_2}{P_{\text{Total}}} = x_2$$

and

$$\frac{P_3}{P_{\text{Total}}} = x_3$$

$$P_i = x_i P_{\text{Total}}$$

$x_i$

Mole fraction of the  $i^{\text{th}}$  component  
gas in the gaseous mixture

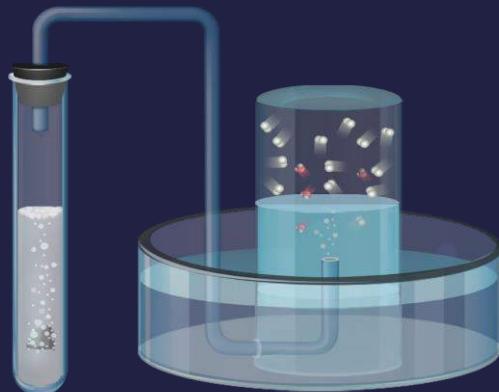
# Vapour Pressure

**Pressure exerted by the  
vapour in equilibrium with liquid,  
at a given temperature**

Vapour pressure **doesn't change** if  
the **temperature** remains **constant**

# Utility of Dalton's Law

Gases are generally collected over water and thus, become **moist**. In such cases, **Dalton's law** is useful in calculating the **pressure of gas**.



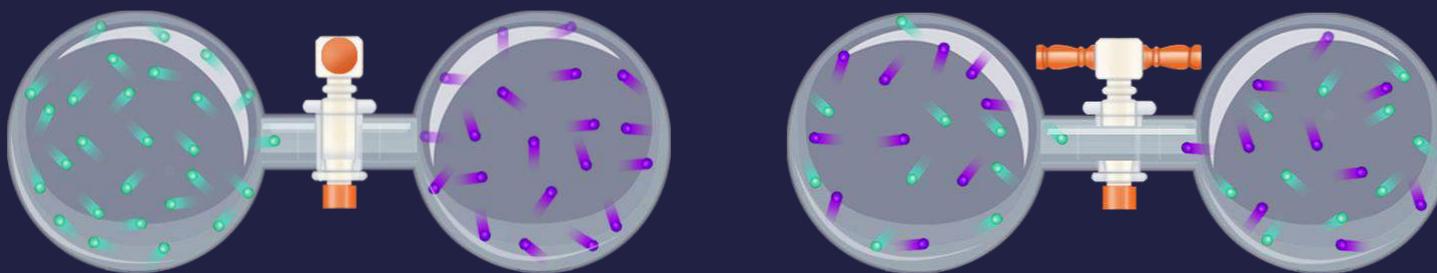
Pressure exerted by saturated water vapour is called **Aqueous tension**

$$P_T = P_g + P_w$$

Pressure of dry gas

Pressure of water vapour

# Diffusion



Net spontaneous flow of gaseous molecules from a region of **higher concentration** (higher partial pressure) to a region of **lower concentration** (lower partial pressure)

# Diffusion

Flow of gaseous molecules

Region of high concentration to lower concentration

Region of higher partial pressure to lower partial pressure

Effusion



Gas escapes through a small orifice

# Graham's Law of Diffusion

Under similar conditions of pressure & temperature, the **rate of diffusion** of gases are **inversely proportional** to the **square roots** of their **densities (d)**

Rate of diffusion ( $r_{\text{gas}}$ )

$\propto$

$\frac{1}{\sqrt{d}}$

# Graham's Law of Diffusion

General form of Graham's law

 $r_{\text{gas}}$  $\propto$ 
$$\frac{PA}{\sqrt{MT}}$$
**P**

Partial pressure of gas

**A**

Area of orifice

**M**

Molar mass of gas

**T**

Temperature of gas

# Graham's Law of Diffusion

Since,

$$PM = dRT$$

P and T constant

$$\frac{r_A}{r_B} = \sqrt{\frac{d_B}{d_A}} = \sqrt{\frac{M_B}{M_A}} = \sqrt{\frac{(V.D.)_B}{(V.D.)_A}}$$

V.D.

Vapour density

# Importance of Graham's Law

Separation of isotopes

Separation of gases having different densities

Rate of diffusion is inversely proportional to square root of molar mass. So, after doing diffusion, we get a mixture which is rich in lighter isotope. If we repeat process of diffusion several times, then we get a mixture which is very rich in lighter isotope. Hence, we can separate lighter gas and heavier gas

In determining densities and molecular masses of unknown gases

Molecular masses of unknown gases can be determined by comparing its diffusion rate with that of any known gas.

# Kinetic Molecular Theory of Gases

# Postulates / Assumptions of KTG

A gas consists of **tiny spherical particles** called **atoms/molecules of the gas** which are **identical in shape & size (mass)**

The **volume occupied** by the particles is **negligible** in comparison to the **total volume** of the gas

Gaseous molecules are always in **random motion** and **collide with each other** and with the **walls of the container**

# Postulates / Assumptions of KTG

Pressure is due to the **collisions of the particles** with the **walls of the container**

**Elastic collisions**

Newton's laws of motion are applicable on the **motion of the gaseous particles**

For an Ideal gas;

Attractive or repulsive forces

=

zero

# Postulates / Assumptions of KTG

**Effect of gravity** is negligible  
on the **molecular motion**

The **average K.E.** of the  
gaseous molecules

 $\propto$ 

**Absolute temperature**  
of the gas

# Postulates / Assumptions of KTG

Average K.E.

$\propto$

T

Average K.E.

=

$$\frac{3}{2} k_B T$$

Depends only on temperature  
and not on nature of the gas

$k_B$

Boltzmann constant

T

Temperature (K)

# Boltzmann Constant

$$k_B = \frac{R}{N_A}$$

$$k_B = 1.3807 \times 10^{-23} \text{ J/K}$$

R

Universal gas constant

N<sub>A</sub>

Avogadro number

# Molecular Speed

Gas molecules are always in **continuous motion**

They **collide** with each other and with the walls of the container

Change in their **speed** & redistribution of **energy**

**Speed** & **energy** of all the molecules at any instant are **not the same**

Measuring **speed** of an individual molecule is not possible

# Molecular Speeds

## Types of molecular speeds

Average speed

Most Probable speed

Root Mean Square speed

$u_{avg}$

$u_{mp}$

$u_{rms}$

# Average Speed

Arithmetic mean of the speeds of different molecules of the gas

$u_{avg}$

=

$$\left[ \frac{u_1 + u_2 + \dots + u_N}{N} \right]$$

$u_{avg}$

=

$$\left[ \frac{8RT}{\pi M} \right]^{\frac{1}{2}}$$

$u_{avg}$

Average speed of molecules

N

Total number of molecules

# Most Probable Speed

Speed possessed by the **maximum number** of **gas molecules**

$$u_{mp} = \left[ \frac{2RT}{M} \right]^{\frac{1}{2}}$$

# Root Mean Square Speed

**Square root of the mean of the squares of the speeds**  
possessed by the gas molecules

$u_{rms}$

=

$$\left[ \frac{3RT}{M} \right]^{\frac{1}{2}}$$

$u_{rms}$

=

$$\left[ \frac{u_1^2 + u_2^2 + \dots + u_N^2}{N} \right]^{\frac{1}{2}}$$

$u_{rms}$

Root of mean of square of speeds

N

Total number of molecules

# Relationship Between the Different Types of Speeds

For a particular gas at the same temperature (T),

 $u_{rms}$ 

:

 $u_{avg}$ 

:

 $u_{mp}$ 

$$\left[ \frac{3RT}{M} \right]^{\frac{1}{2}}$$

:

$$\left[ \frac{8RT}{\pi M} \right]^{\frac{1}{2}}$$

:

$$\left[ \frac{2RT}{M} \right]^{\frac{1}{2}}$$

 $\sqrt{3}$ 

:

$$\left[ \frac{8}{\pi} \right]^{\frac{1}{2}}$$

:

 $\sqrt{2}$ 

1.224

:

1.128

:

1

- T = Temperature in Kelvin
- M = Molar mass in kg
- R = 8.314 J/mol K

Conclusion:

$u_{rms} > u_{avg} > u_{mp}$

# Maxwell-Boltzmann Distribution of Speeds

Based on the theory of **probability**

Gives the **statistical average of the speeds**  
of the whole collection of the gas molecules

# Maxwell's Distribution of Molecular Speeds

Fraction of molecules with speed between 'u' & 'u + du'

$$\frac{1}{N} \frac{dN}{du}$$

=

$$4\pi \left[ \frac{M}{2\pi RT} \right]^{\frac{3}{2}} e^{-\frac{Mu^2}{2RT}} u^2$$

N

Total number of gas molecules

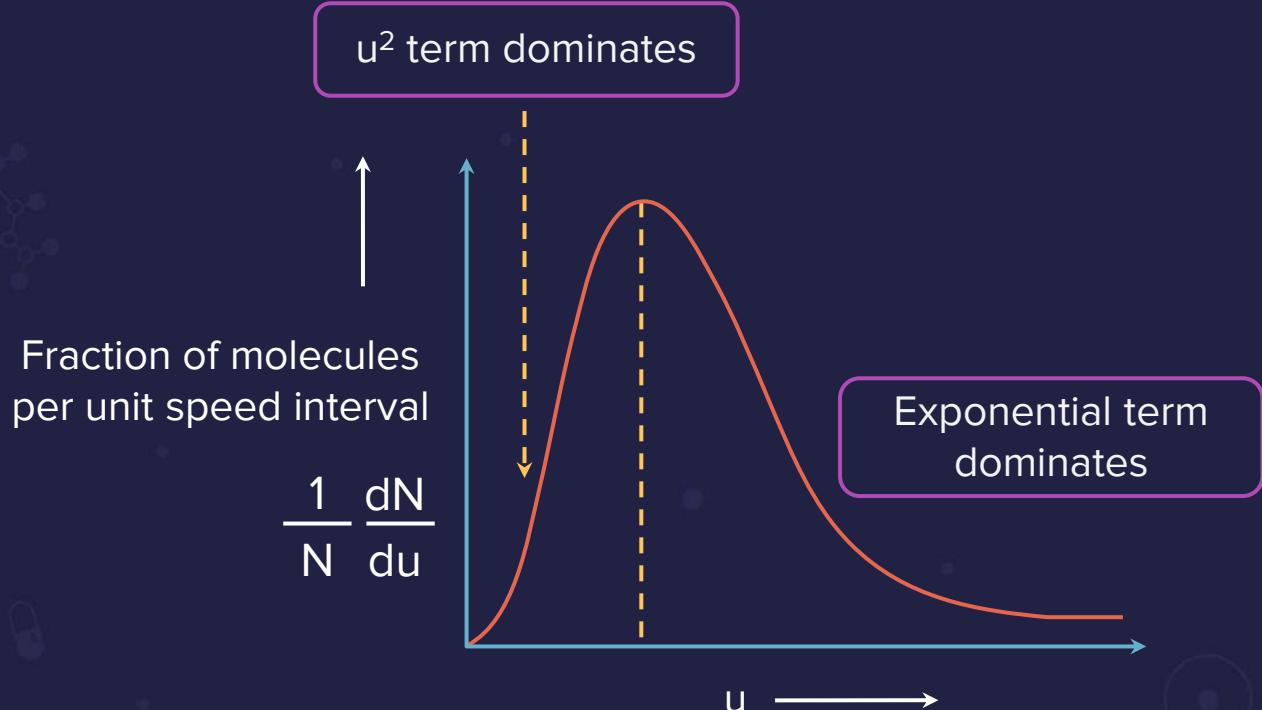
M

Molar mass

u

Speed

# Maxwell-Boltzmann Distribution of Speeds



# Maxwell-Boltzmann Distribution of Speeds

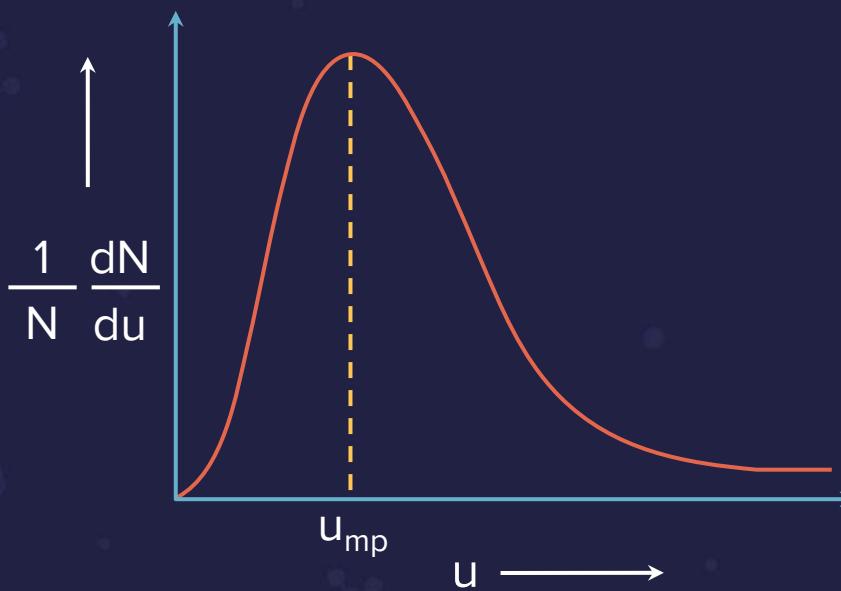
At a particular temperature,

**Individual speed** of molecules **keeps changing**

**Distribution of speeds** remains the same

# Maxwell-Boltzmann Distribution of Speeds

Maximum fraction of molecules possess a **speed** corresponding to the **peak of this curve** referred to as  $u_{mp}$

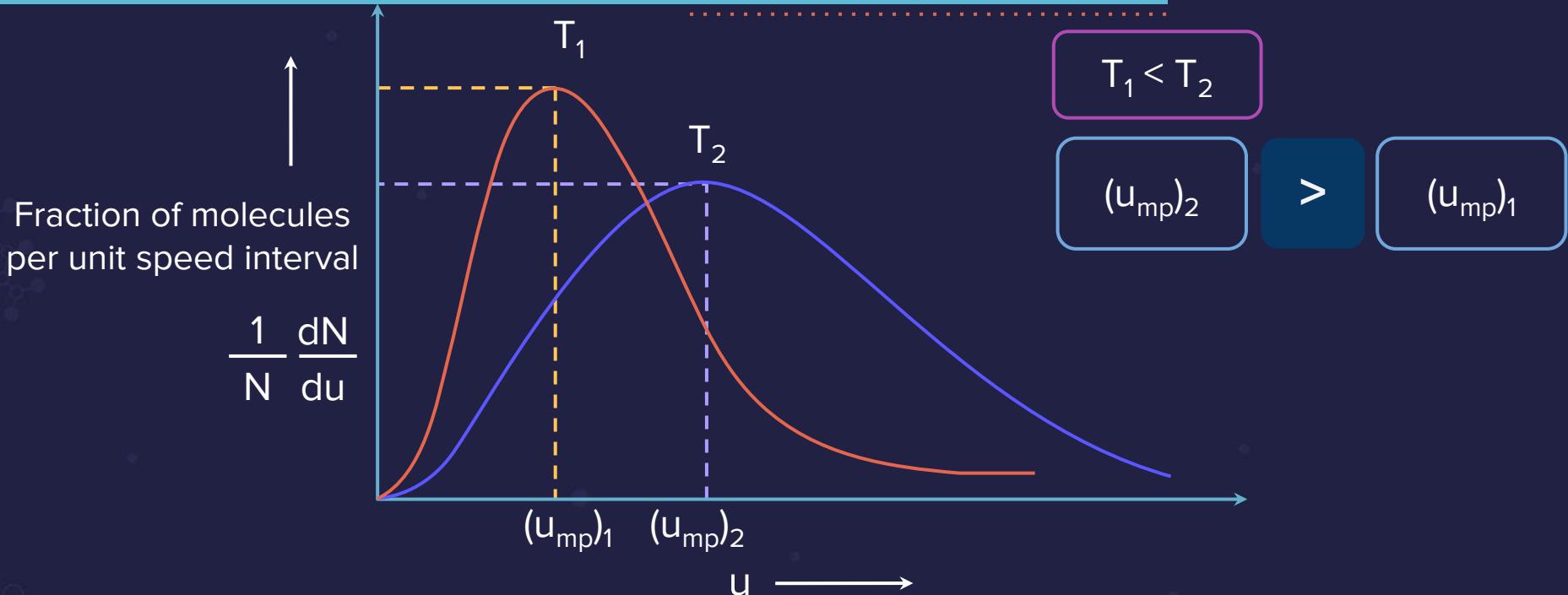


Actual distribution of **molecular speeds** in a gas depends on

Temperature

Molar Mass

# Maxwell-Boltzmann Distribution of Speeds

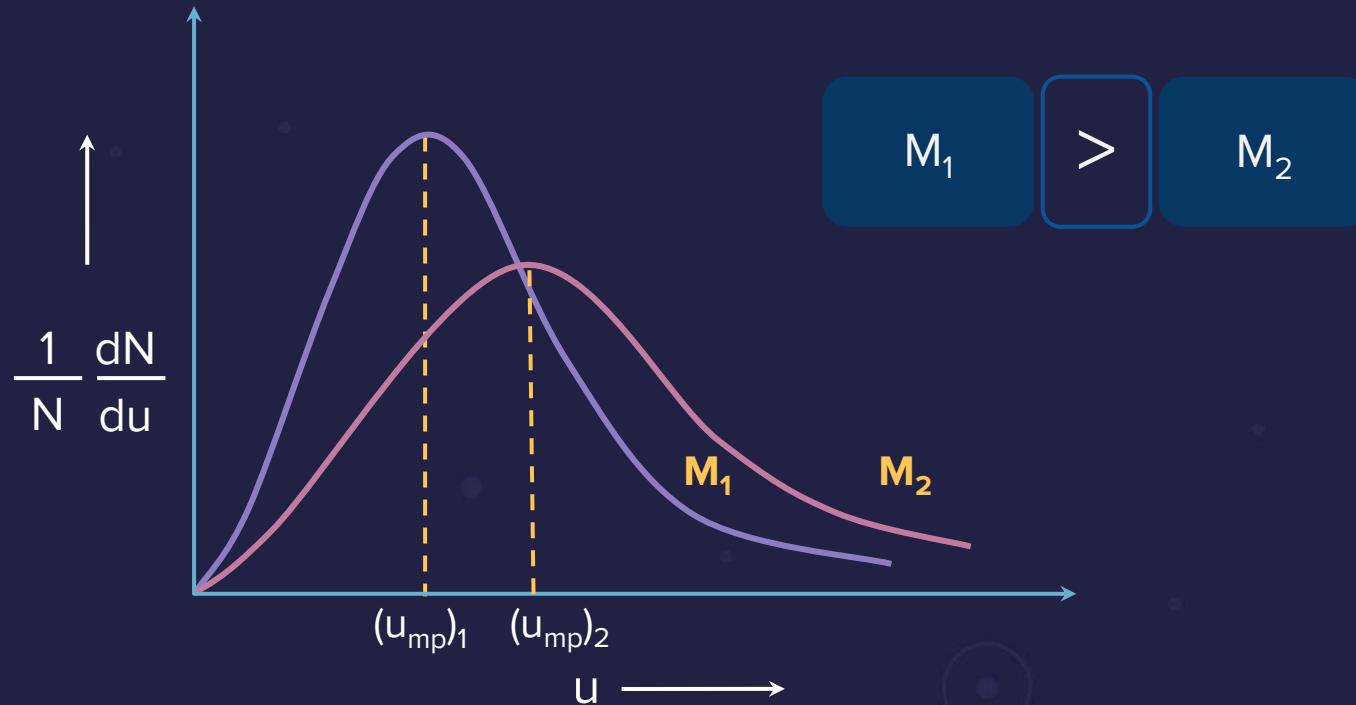


Temperature ↑

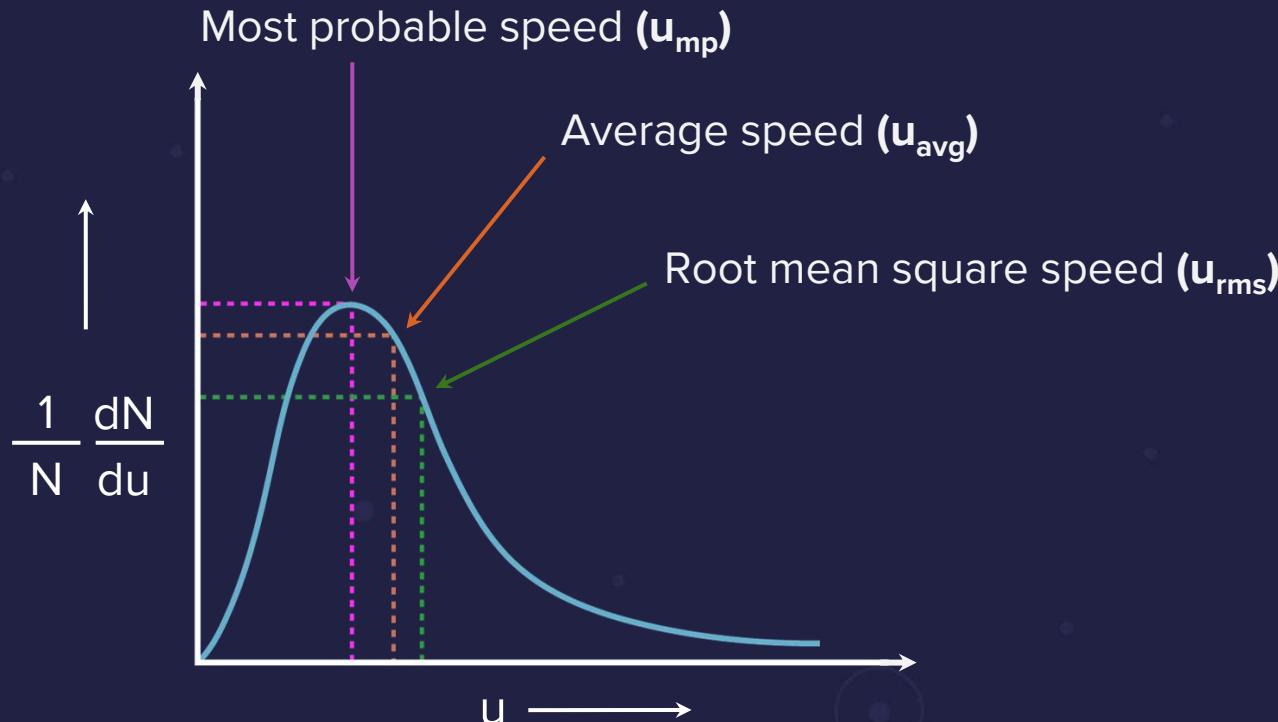
Molecular motion becomes rapid

Entire curve shifts towards the right

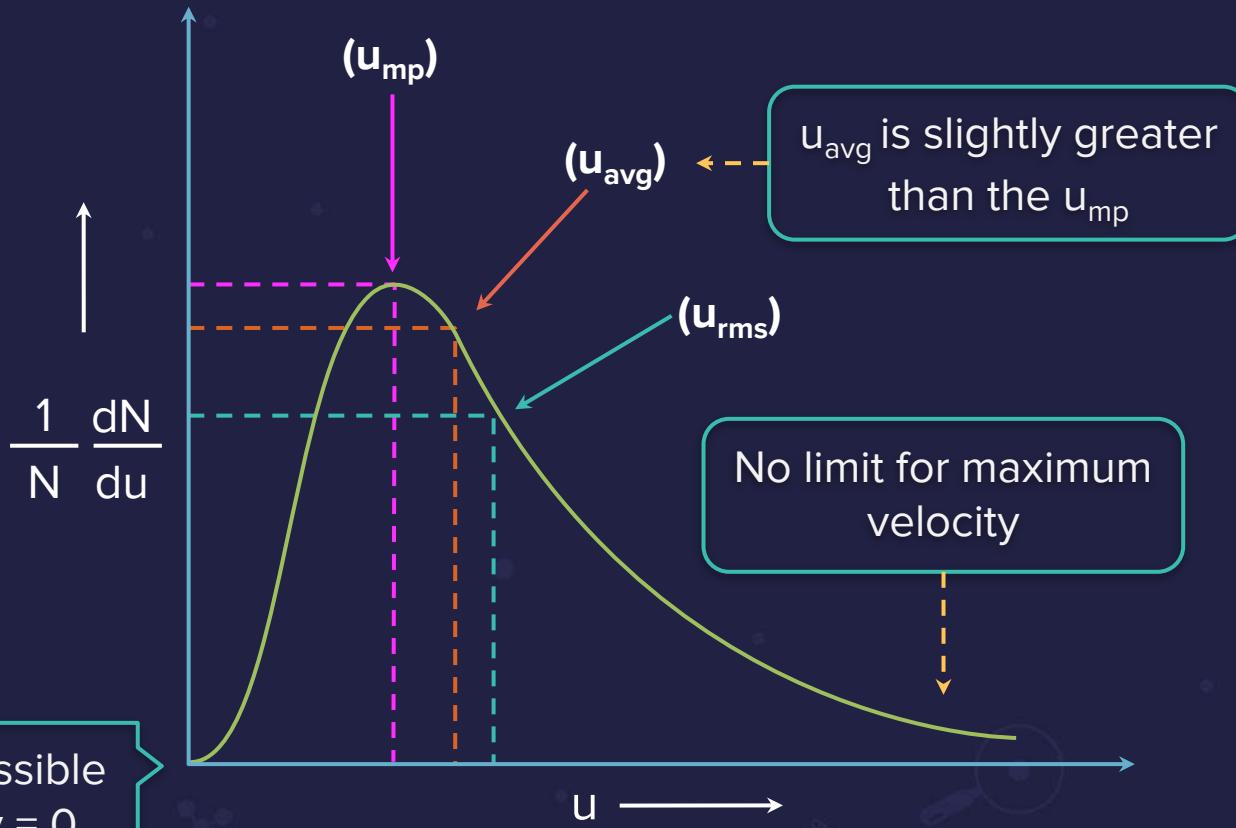
# Distribution of Speeds for Different Molar Masses



# Maxwell's Distribution of Molecular Speeds

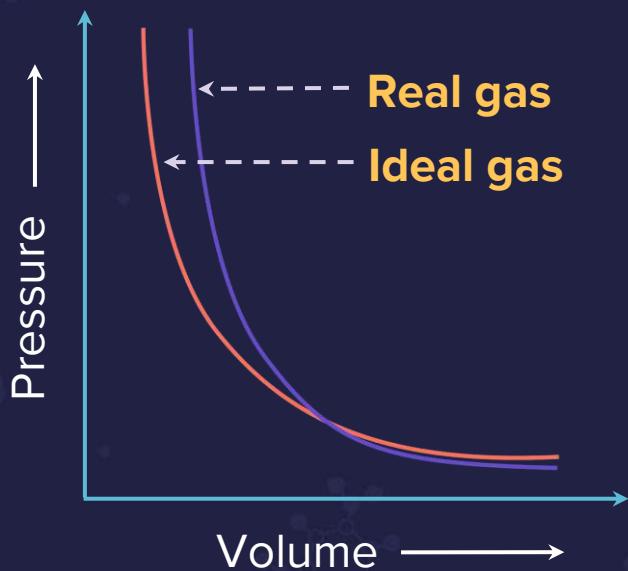


# Why Average Velocity is Towards the Right?



# Real Gas

Gases which **do not obey Ideal gas law** under all conditions of **T & P**



All gases found in **universe** **are real gases**. Real gases can behave like ideal gas at **low pressure and high temperature**.

# What is Compressibility Factor (Z)?

A measure of the **deviation of**  
real gases from ideal behaviour

$V_m$  is the Molar  
Volume

$$\frac{V_{m, \text{real}}}{V_{m, \text{ideal}}} = Z$$

Measured at the same T & P

# Compressibility Factor

Since,

$$V_{m, \text{ideal}} = \frac{RT}{P} \quad Z = \frac{V_{m, \text{real}}}{V_{m, \text{ideal}}} = \frac{PV_m}{RT}$$



# Compressibility Factor (Z)

At very low pressure

Z

$\approx$

1

Attractive forces

$\approx$

Repulsive forces

At intermediate pressure

Z

<

1

**Negative deviation**

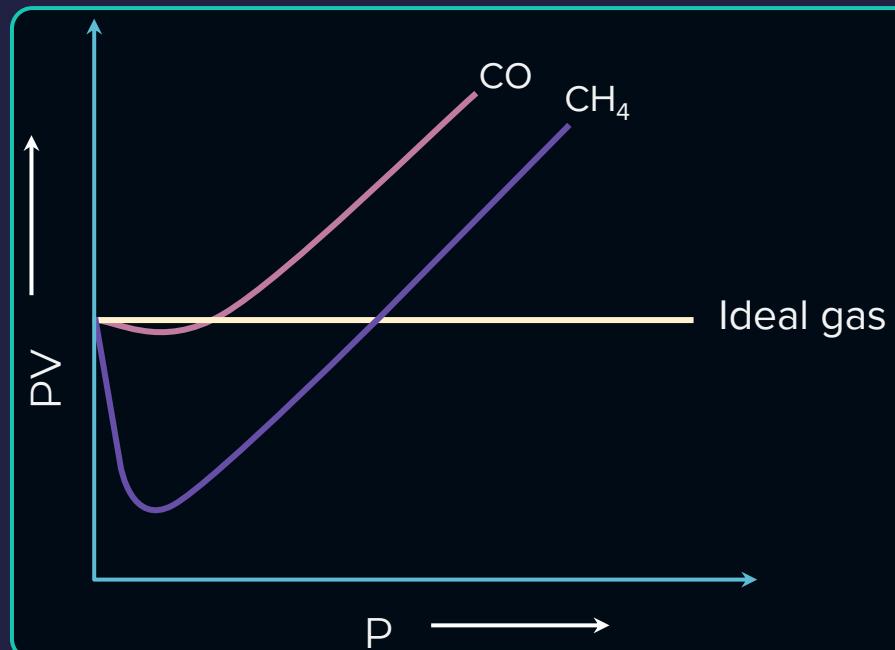
Attractive forces

>

Repulsive forces

**Gas easy to compress**

# Inferences from the Plot



First there is a **negative deviation**  
& then a **positive deviation**

# Compressibility Factor (Z)

At high pressure

Z

>

1

**Positive deviation**

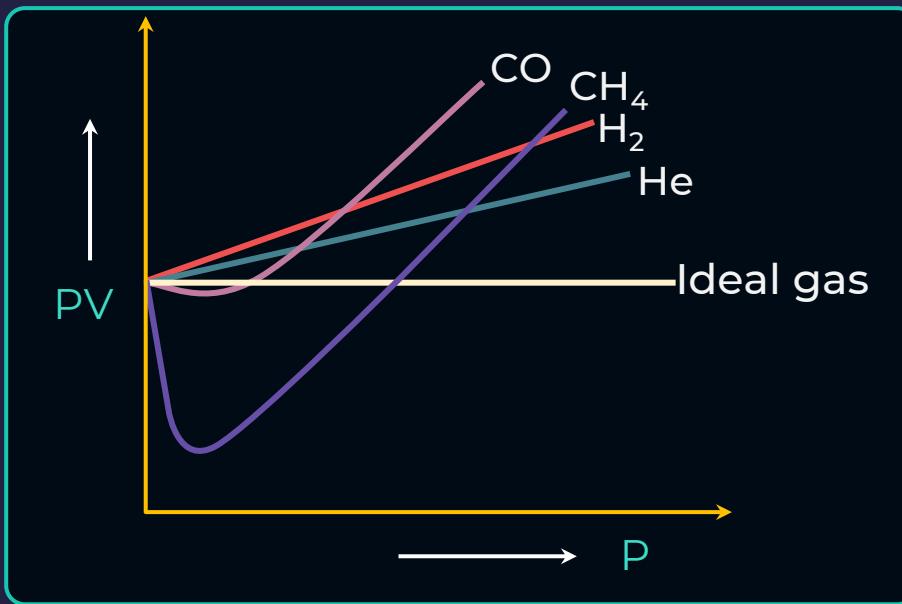
Attractive forces

<

Repulsive forces

**Gas difficult to compress**

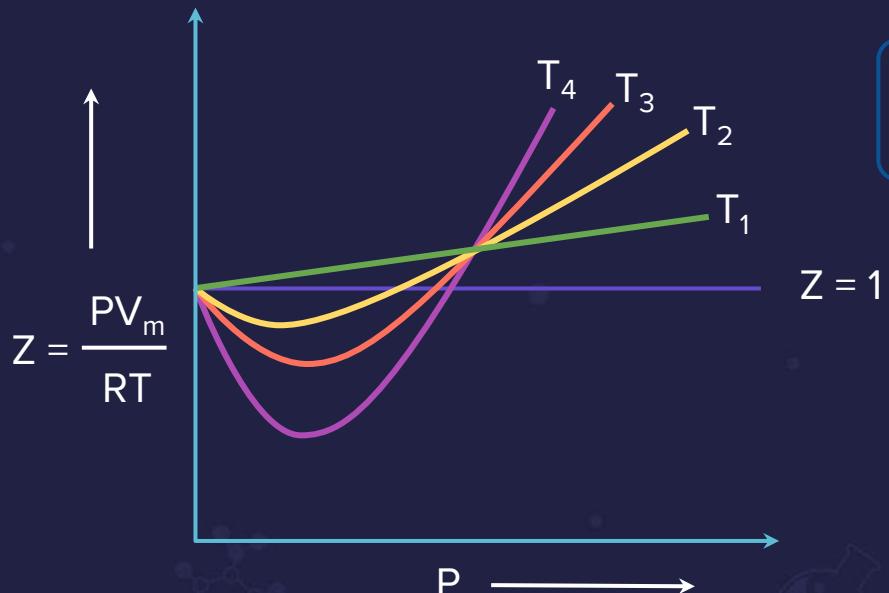
# Inferences from the Plot



**Ideal gas:**  $PV$  vs  $P$  will be a straight line parallel to x-axis

**Real gas:**  $PV$  vs  $P$  is not a horizontal straight line

# Different T, Same Gas



$T_1 > T_2 > T_3 > T_4$

For a given real gas, at very low pressure ( $P \rightarrow 0$ ), the compressibility factor,  $z=1$  and the gas behaves ideally. At intermediate pressure where attraction dominates,  $z<1$  and at very high pressure, where repulsion dominates,  $z>1$ .

# Boyle Temperature ( $T_b$ )

## Boyle point or temperature

Temperature at which a **real gas behaves like an ideal gas** at low pressure

# Boyle Temperature

$T_b$

$\propto$

Attraction between  
molecules

$T_b$  depends on the  
**nature of the gas**

$(T_b)_{CO, CH_4}$

>

273 K

$(T_b)_{H_2, He}$

<

273 K

# Conclusion

$$Z = 1$$

Ideal gas

Real gas at  
 $T = T_b$

Low pressure  
region

# Exceptional Behaviour of H<sub>2</sub> and He

Z

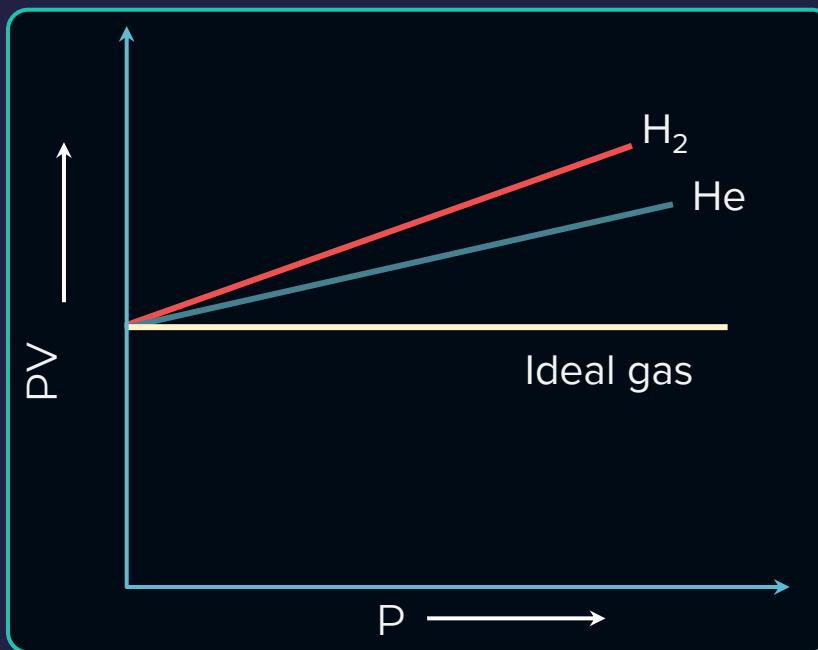
>

1

T (273 K) > T<sub>b, gas</sub>

**Repulsive forces dominate**

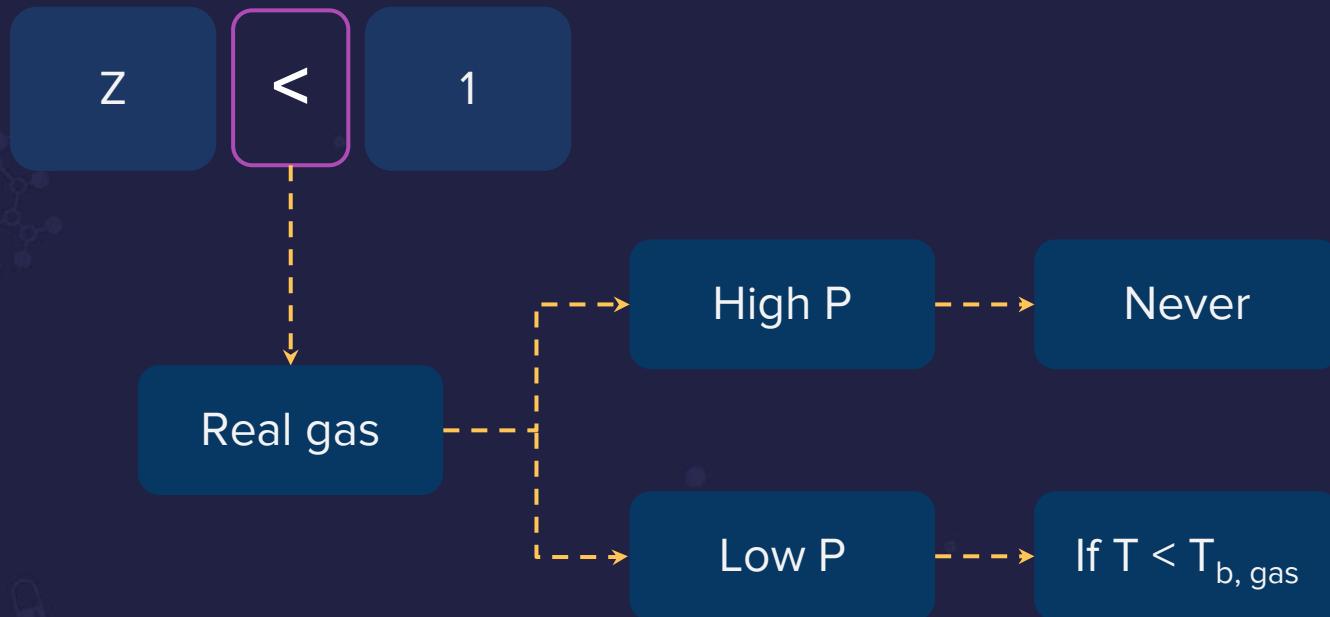
# Exceptional Behaviour of $H_2$ and He



**Ideal gas:**  $PV$  vs  $P$  will be a straight line parallel to x-axis

**Real gas:**  $PV$  vs  $P$  is not a horizontal straight line but above x-axis

# Conclusion



# Real Gases

Volume of gas particles is **not negligible** w.r.t the container

On liquefaction, occupy a finite volume

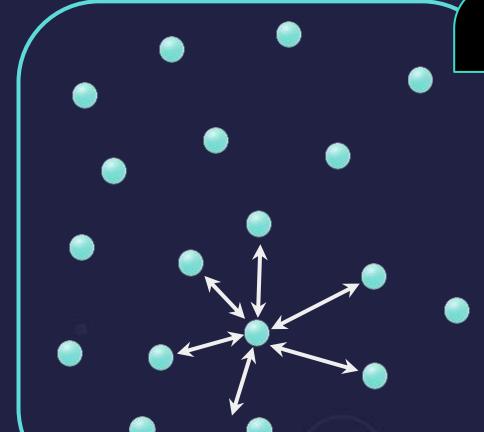
# Real Gases

**Interparticle forces** of attraction are present

Ideal gas



Real gas



# van der Waals Equation of Real Gases

$P_{\text{ideal}}$   $V_{\text{ideal}}$

=

$nRT$

$P_{\text{real}}$   $V_{\text{real}}$

≠

$nRT$

$(P_{\text{real}} \pm \text{___}) (V_{\text{real}} \pm \text{___})$

=

$nRT$

Ideal gas equation  
is affected by

Intermolecular  
forces

Molecular  
volume

# Pressure Correction

B

Intermolecular **Attractive forces** are present

Speed during  
collisions  
will be reduced

Momentum ↓

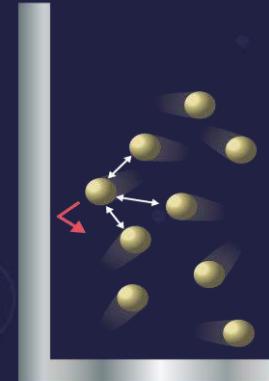
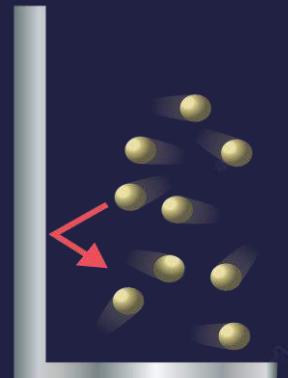
Force applied ↓

Pressure ↓

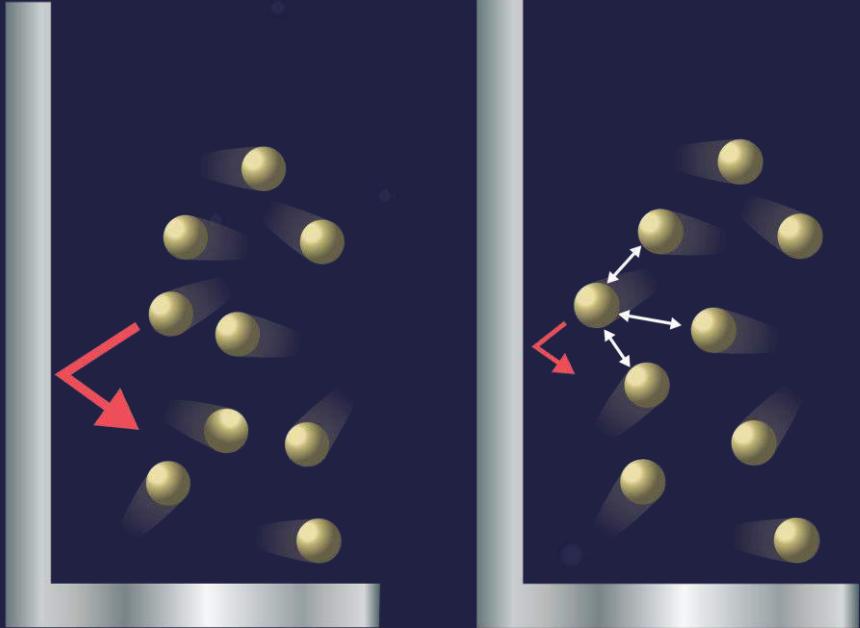
$P_{\text{ideal}}$

>

$P_{\text{real}}$



# Pressure Correction



Molecules are dragged back by other molecules due to **intermolecular attractive forces**

$P_{\text{ideal}}$

=

$(P_{\text{actual}} + \text{___})$

$P_{\text{ideal}}$

=

$P_{\text{actual}}$

+

**Pressure correction term**

# Pressure Correction

Correction term

$$\propto$$

**Number of molecules**  
attracting the colliding molecule

$$\propto$$

$$\frac{n}{V}$$

Correction term

$$\propto$$

**Concentration** of the  
colliding molecules

$$\propto$$

$$\frac{n}{V}$$

# Pressure Correction

Correction term

$\alpha$

$\frac{n}{V}$

$X$

$\frac{n}{V}$

Correction term

$\alpha$

$\frac{n^2}{V^2}$

Correction term

=

$\frac{an^2}{V^2}$

**a**

van der Waals constant

‘a’ depends on force of attraction

# Unit of "a"

$P_{\text{correction}}$

=

$$\left[ \frac{an^2}{V^2} \right]$$

a

=

$$\frac{P_{\text{correction}} [V]^2}{n^2}$$

Unit

=

atm L<sup>2</sup> mol<sup>-2</sup>

# Significance of 'a'

Stronger the forces of attraction,  
greater will be 'a'

As  $a \uparrow$ ,  
Liquefaction  $\uparrow$

Value of 'a' depends on  
the nature of the gas

# Remember!!

$a$   
↑

Boiling Point  
↑

$a$  (Polar molecules)

>

$a$  (Non polar molecules)

For **non polar** molecules

Surface area  
↑

van der  
Waals forces  
↑

$a$   
↑

# Volume Correction

$$V_{\text{ideal}}$$

=

Volume available for free movement of the gaseous molecules

$$V_{\text{ideal}}$$

=

$$V$$

-

Volume not available for free movement

$$V$$

Volume of container

$$V_{\text{ideal}}$$

=

$$V_{\text{container}}$$

-

$$V_{\text{excluded}}$$

$$V_{\text{excluded}}$$

Volume that is **not available** for free movement is called excluded volume

# Remember!!

For **ideal** gas

$$V_i$$

=

$$V$$

For **real** gas

$$V_i$$

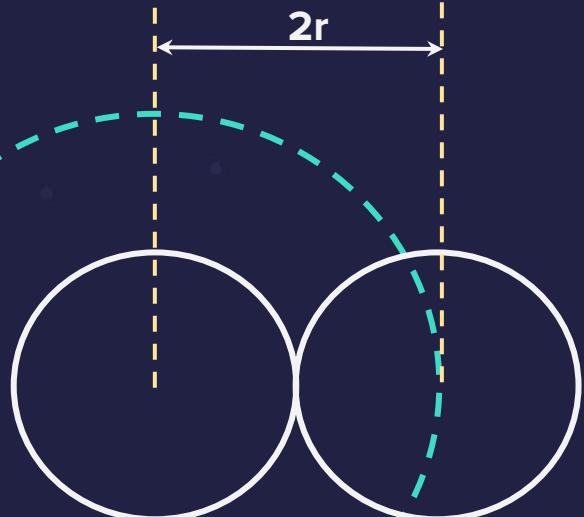
≠

$$V$$

All volume is not available  
for free movement

# Volume Correction

Excluded  
volume



$$V_{\text{excluded}}$$

=

$$\frac{1}{2} \left[ \frac{4}{3} \pi (2r)^3 \right]$$

=

$$4 \left[ \frac{4}{3} \pi r^3 \right]$$

For a pair  
of molecules

$$V_{\text{excluded}}$$

=

$$\frac{4}{3} \pi (2r)^3$$

For a  
molecule,

# Volume Correction

**b**

Excluded volume per mole of gas

**b**

van der Waals constant

‘b’ depends on size of the gas molecules

b

=

$4 \times \text{Volume of individual molecules} \times N_A$

b

=

$$4 \times \frac{4}{3} \pi r^3 \times N_A$$

b

$\propto$

Size of the molecules

# Volume Correction and Unit of "b"

For n moles

[V]

=

[nb]

$V_{\text{excluded}}$

=

$nb$

$b$

=

$\frac{[V]}{n}$

$V_{\text{ideal}}$

=

$V - nb$

Unit

=

$\text{L mol}^{-1}$

## Remember!!

If two gases have the **same 'b'**  
but **different 'a'** then

Gas having the **larger value of 'a'**  
will occupy **lesser volume**

Force of attraction

Distance between  
the molecules

# van der Waals Equation of Real Gases

$$\left[ P + \frac{an^2}{V^2} \right] [ V - nb ] = nRT$$

Pressure  
correction term

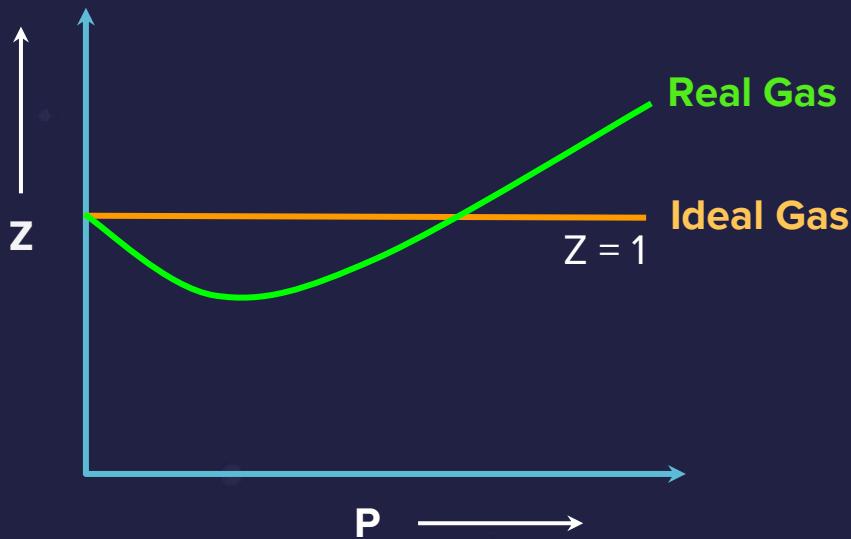
Volume  
correction term

- a & b = van der Waals constants
- n = Number of moles of gas



## Verification of van der Waals equation

# Compressibility Factor



# van der Waals Equation

$$\left[ P + \frac{a}{V_m^2} \right] (V_m - b) = RT$$

$$V_m = \frac{V}{n}$$

Volume of 1 mole of gas

# Verification of van der Waals Equation

1

At Low pressure (moderate temperature)

Pressure



$V_m$



$b$

can be neglected in comparison to  
 $V_m$

$$\left[ P + \frac{a}{V_m^2} \right] V_m$$

=

$RT$

$$PV_m + \frac{a}{V_m}$$

=

$RT$

$$\frac{PV_m}{RT} + \frac{a}{V_m RT}$$

=

1

# Verification of van der Waals Equation

$$\frac{PV_m}{RT} \rightarrow Z = 1 - \frac{a}{V_m RT}$$

$$Z < 1$$

Real gas is **more compressible** as compared to an **Ideal gas**

# Verification of van der Waals Equation



At high pressure (moderate temperature)

Pressure



$V_m$



b

can't be neglected in comparison to  $V_m$

Pressure



$\frac{a}{V_m^2}$  can be neglected

# Verification of van der Waals Equation

$$P(V_m - b)$$

 $=$ 

$$RT$$

$$Z$$

 $=$ 

$$1 + \frac{Pb}{RT}$$

$$PV_m - Pb$$

 $=$ 

$$RT$$

$$Z$$

 $>$ 

$$1$$

$$\frac{PV_m}{RT}$$

 $=$ 

$$1 + \frac{Pb}{RT}$$

**Real gas** is **less compressible** as compared to an **Ideal gas**

# Verification of van der Waals Equation



Real gas having very large molar volume

$$\left[ P + \frac{a}{V_m^2} \right] (V_m - b) = RT$$

b

can be neglected in comparison to  $V_m$

$V_m$  is very large

$\frac{a}{V_m^2}$  can be neglected

# Verification of van der Waals Equation

$$PV_m$$

$$\approx$$

$$RT$$

4

$H_2 / He$

$$Z$$

$$\approx$$

$$1$$

$$a$$

$$\approx$$

$$0$$

Ideal gas condition

$$Z$$

$$=$$

$$1 + \frac{Pb}{RT}$$

$$>$$

$$1$$

# Liquefaction of Gases

Phenomenon  
of converting a  
**gas into liquid**

Occurs when the  
**intermolecular forces of  
attraction become high**

Gas liquification

Pressure ↑

Temperature ↓

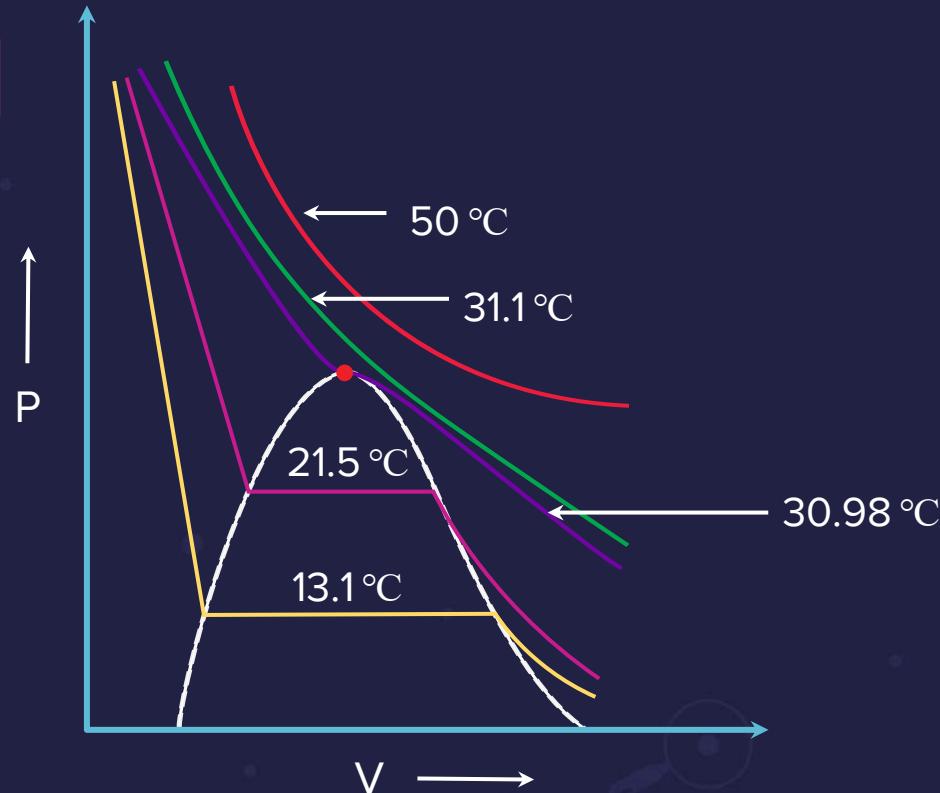
# Andrew's Isotherm



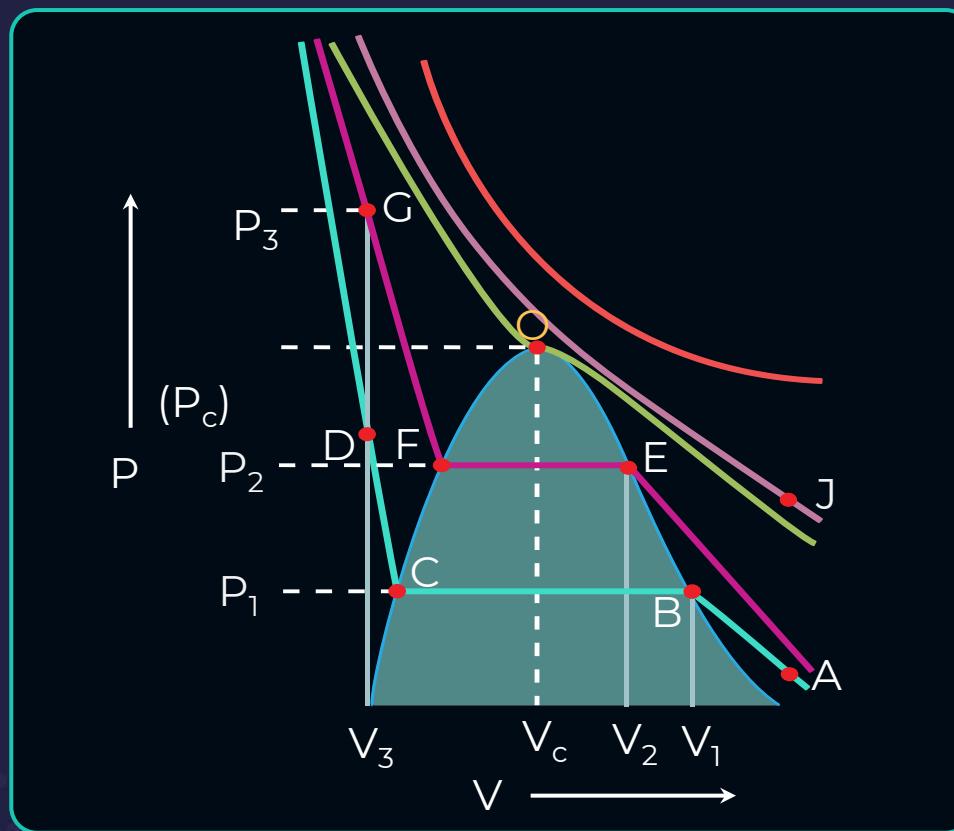
**P - V** relationship  
(isotherms)  
for  $\text{CO}_2$

# The 'Dome' of Andrew's Isotherm

Different isotherms for the same gas

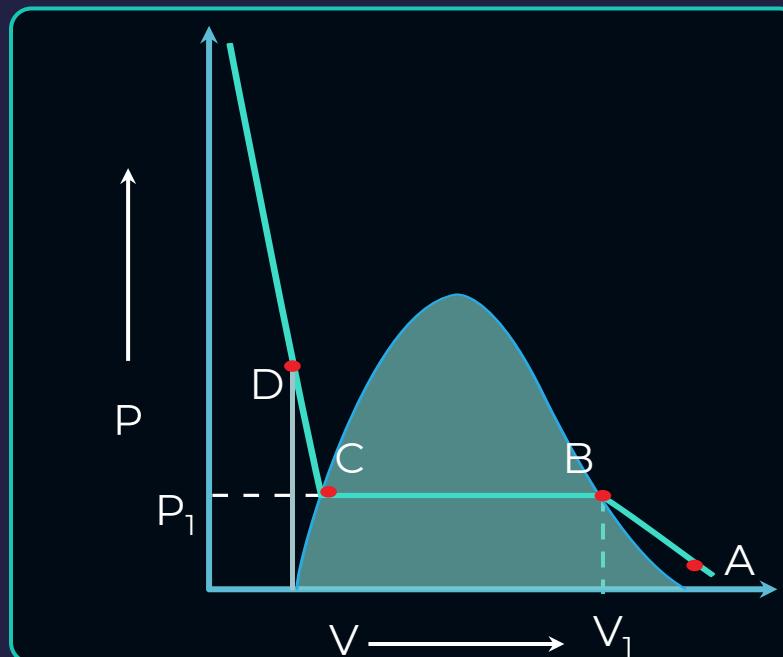


# Isotherm of $\text{CO}_2$

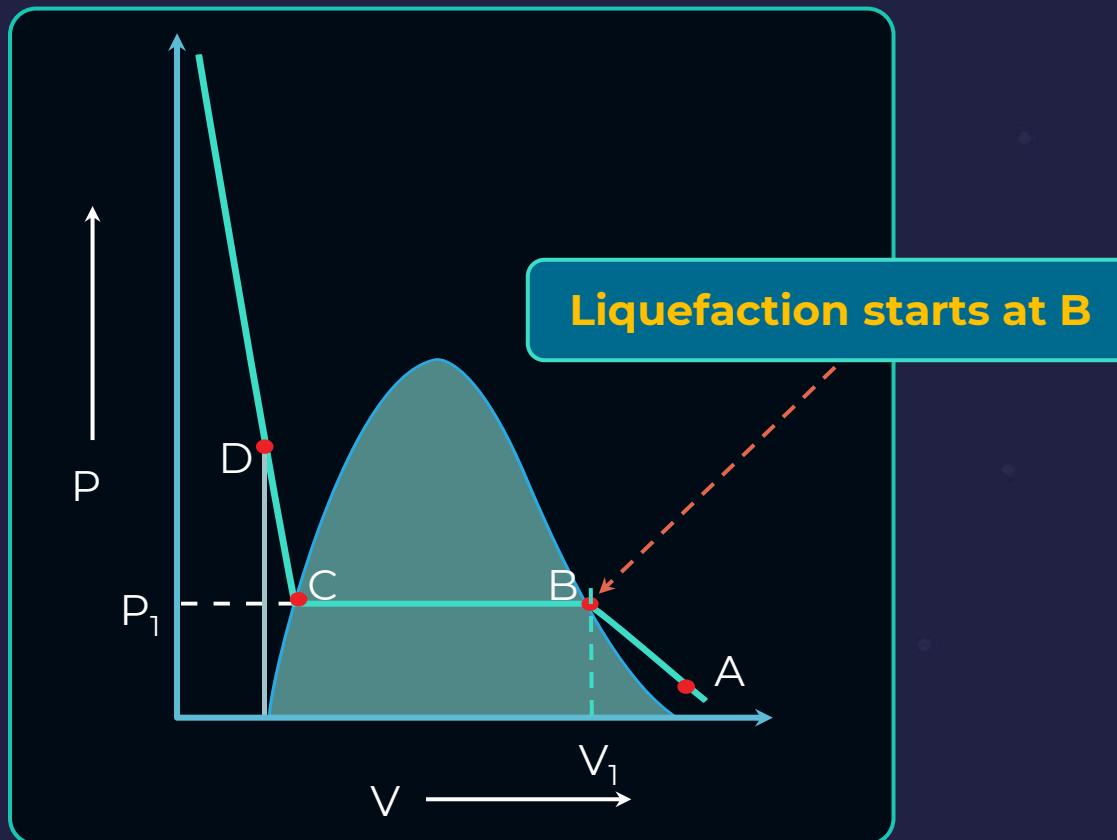


# Isotherm of $\text{CO}_2$

**Region AB → Gaseous phase  
→ Compression at constant T**



# Isotherm of $\text{CO}_2$



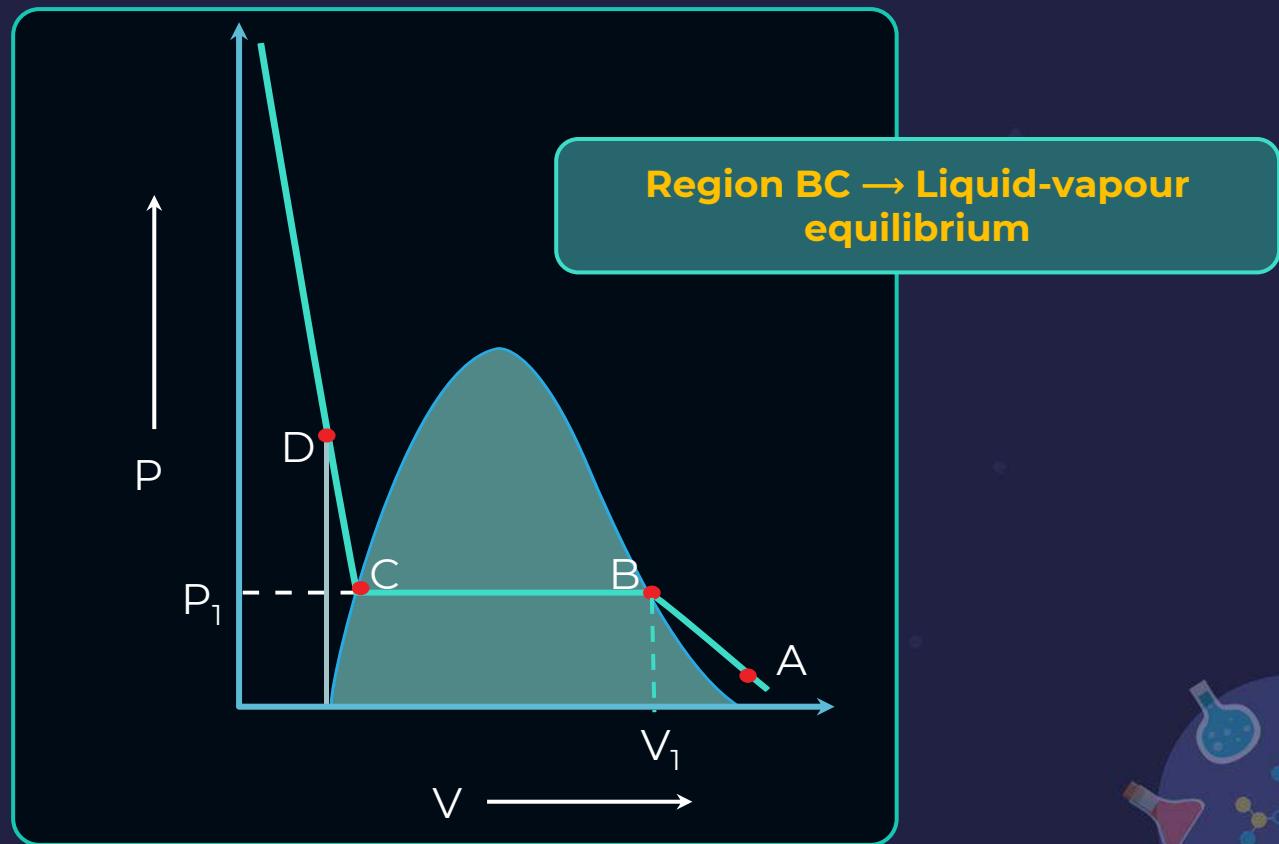
# Isotherm of $\text{CO}_2$

$$P \quad \alpha \quad \frac{n}{V}$$

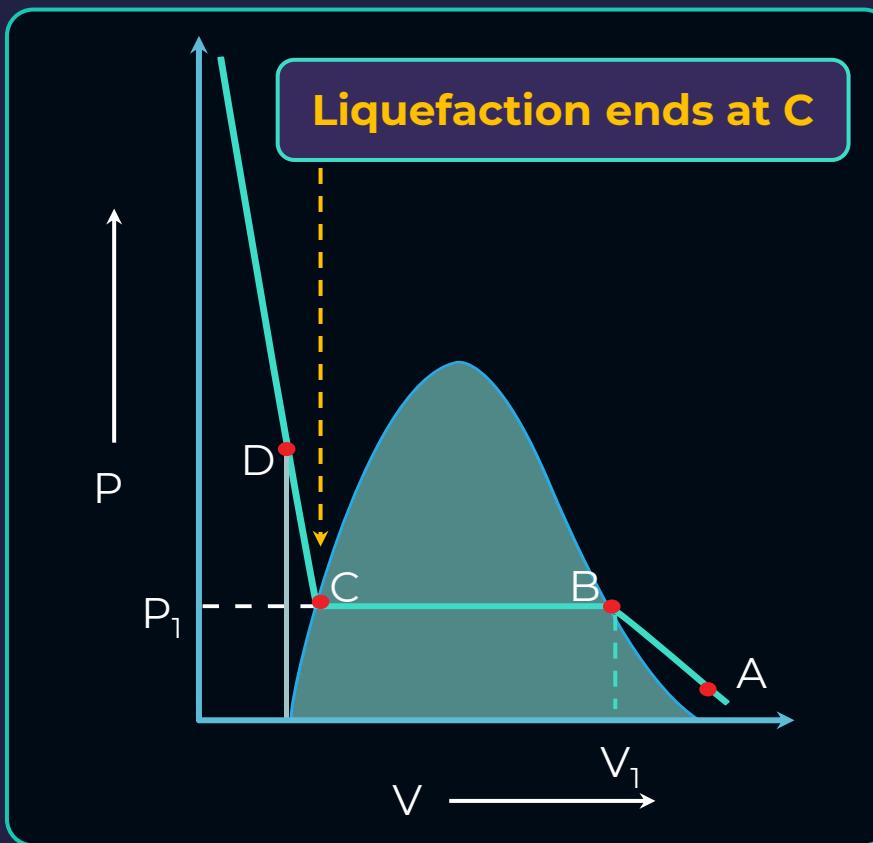
$$n \downarrow \quad V \downarrow$$

↓

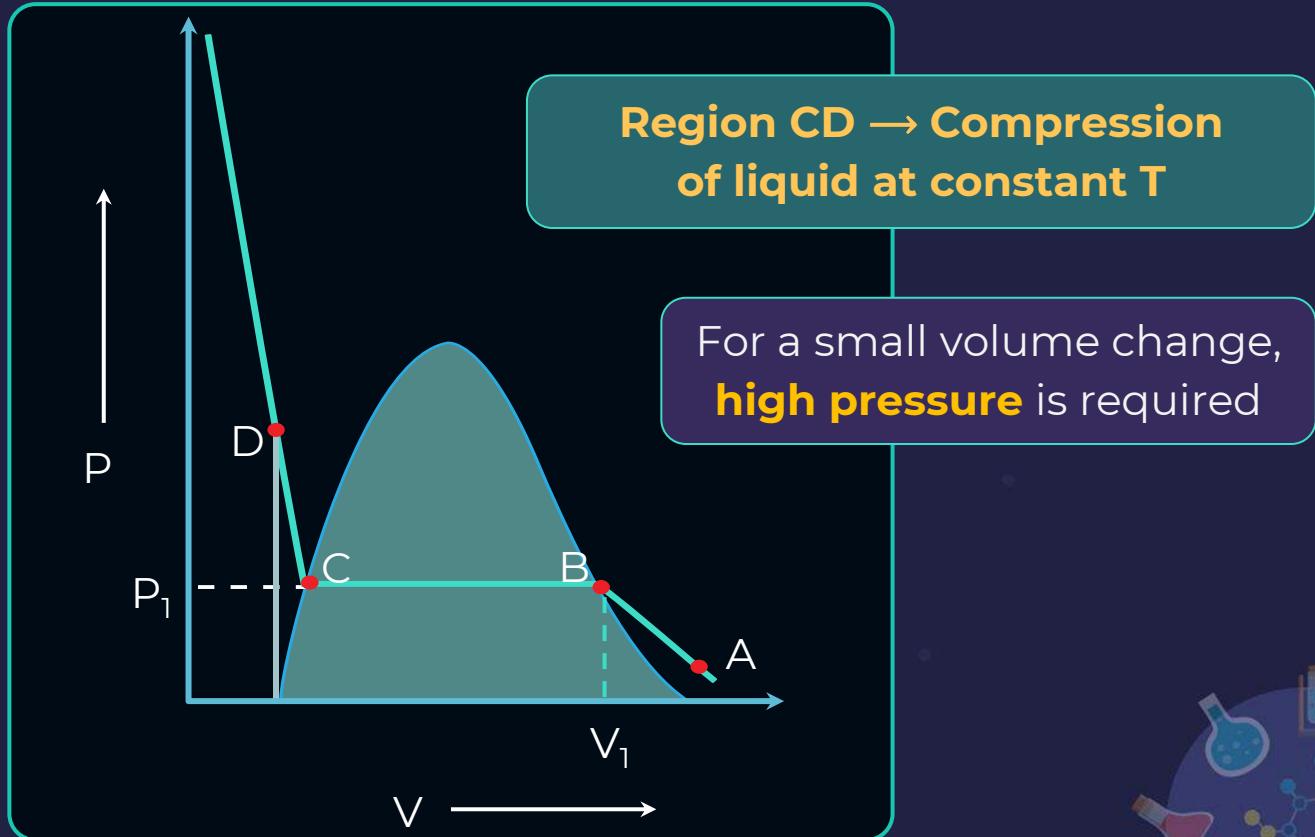
Pressure remains constant



# Isotherm of $\text{CO}_2$



# Isotherm of $\text{CO}_2$



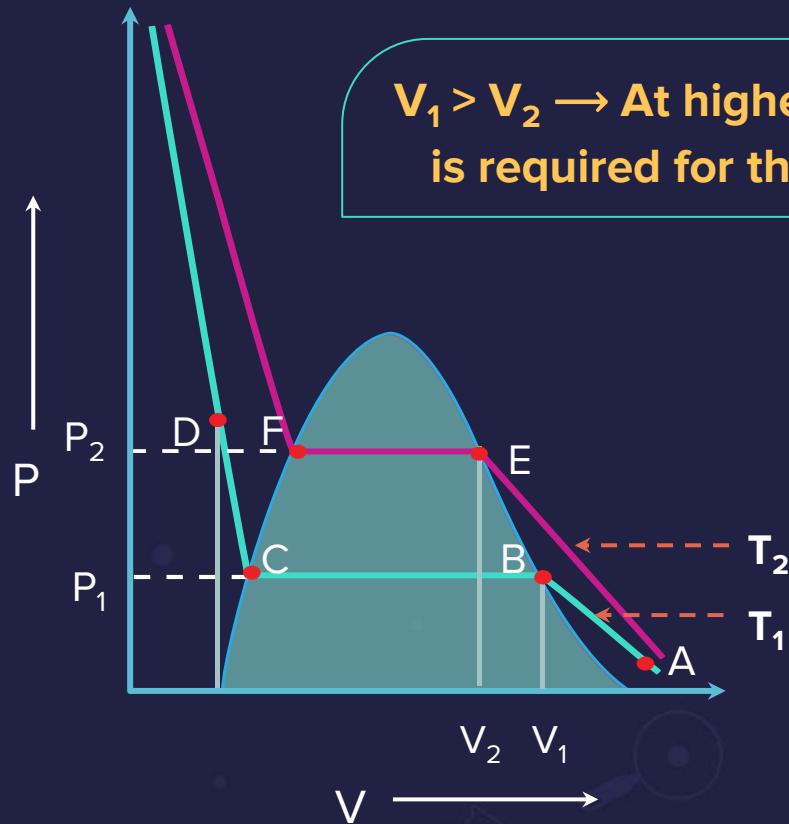
# Isotherm of $\text{CO}_2$

B

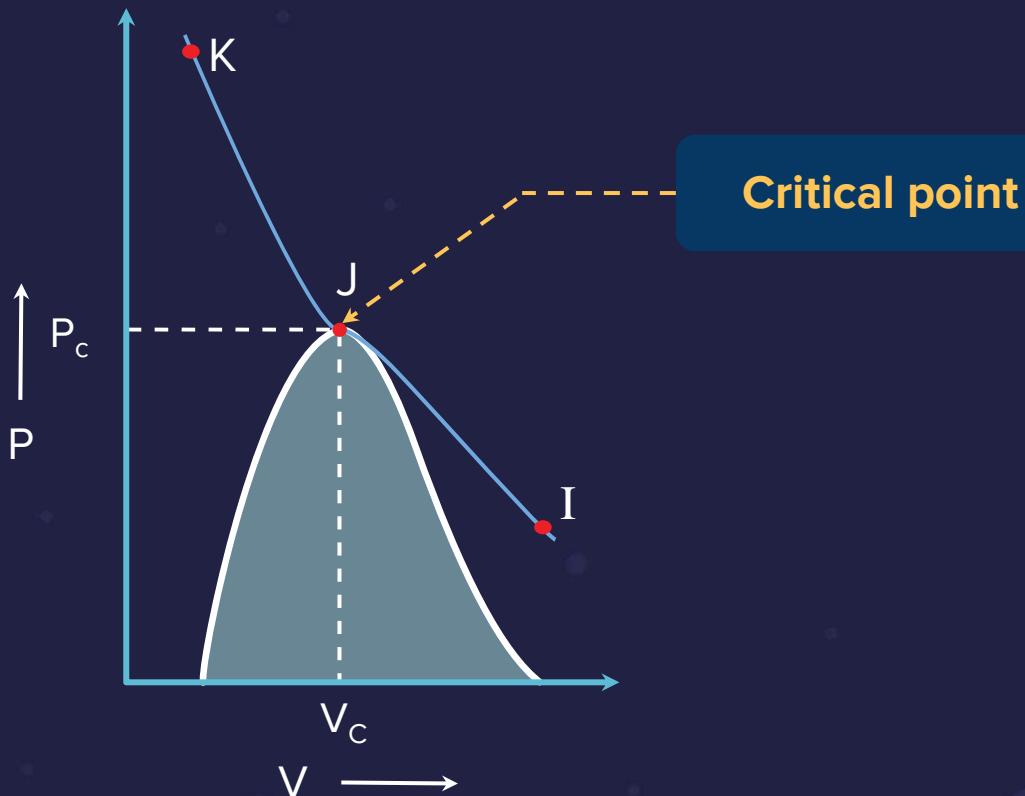


Region BC > Region EF

$T_2 > T_1$



# Critical Isotherm



Critical point

## Critical Point

A point on the critical isotherm where **gas** & **liquid** are in **equilibrium**

# Critical Temperature ( $T_c$ )

Temperature **above** which the gas **cannot be liquefied**, regardless of the pressure

Below  $T_c$

Two phases can be **distinguished**

At  $T_c$

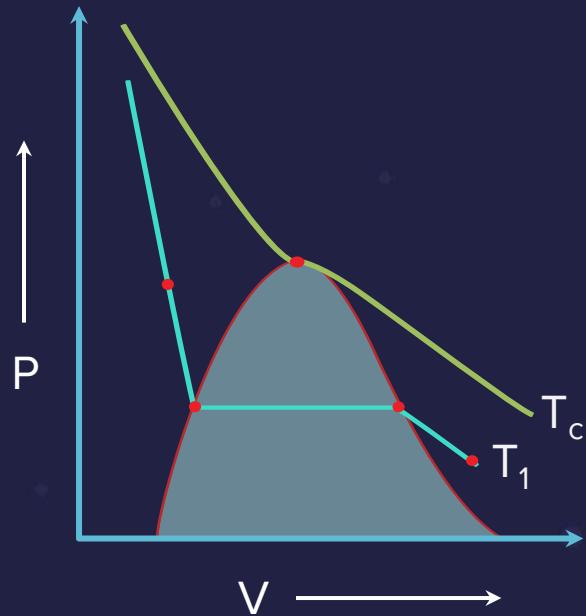
**Liquid passes** into the **gaseous phase** continuously and the boundary between the two phases disappears

# Continuity of States

At the **critical temperature** ( $T_c$ ), the densities of the liquid & the vapour phase becomes identical

**No distinction between vapour & liquid**

# Density Variation with Temperature



At  $T_1$ ,

Density of liquid

>

Density of vapour

At  $T_c$ ,

Density of liquid

=

Density of vapour

At  $T_1 < T_c$

Gas can be liquefied

# Density Variation with Temperature

In liquid-vapour equilibrium region

Temperature ↑

Density of liquid ↓

Density of vapour ↑

# Did you know?



Term **vapour** is used when

$T$

$<$

$T_c$

Term **gas** is used when

$T$

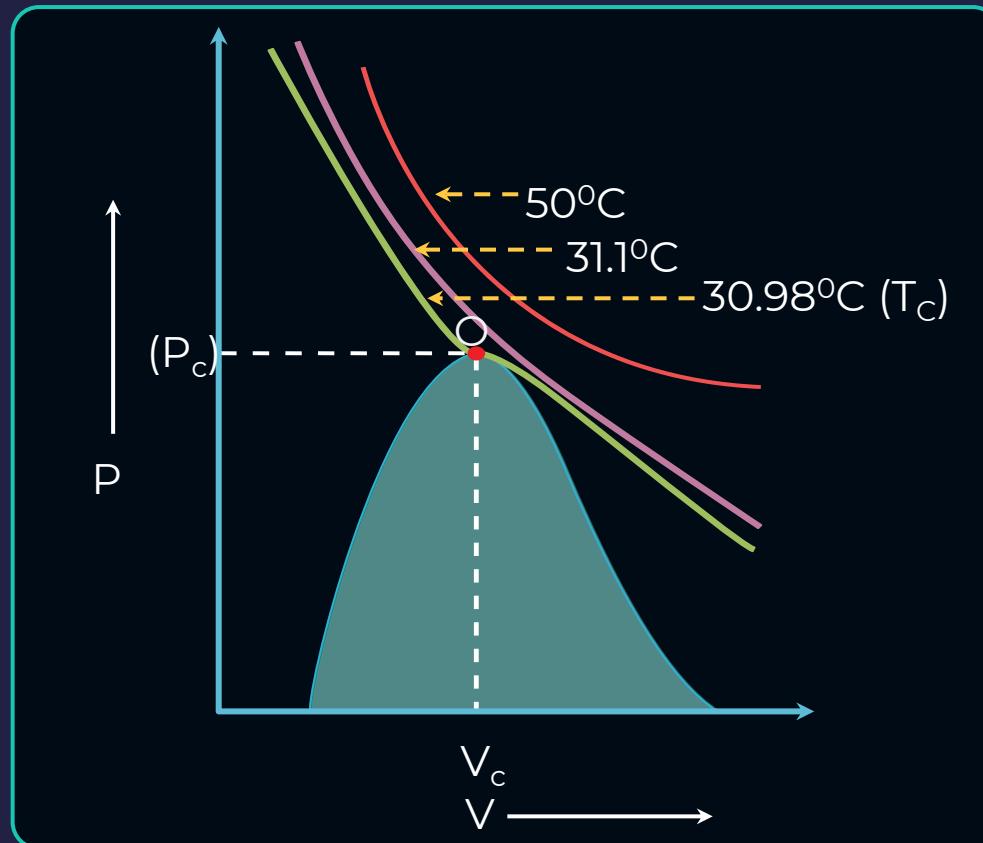
$>$

$T_c$

# Critical Temperature ( $T_c$ )

At  $T > T_c$

Gas cannot be liquefied



# Significance of Critical Temperature

As **intermolecular forces** increase,  $T_c$  also increases

**Ease of liquefaction**

# Critical Pressure ( $P_c$ ) and Critical Volume( $V_c$ )

Minimum pressure which must be applied **at critical temperature** to convert a **gas into liquid**

Volume occupied by one mole of a gas **at critical temperature ( $T_c$ ) & critical pressure ( $P_c$ )**

# Critical Constants

**Critical  
constants**

Critical Temperature ( $T_c$ )

Critical Pressure ( $P_c$ )

Critical Volume ( $V_c$ )

# Critical Constants in Terms of van der Waals Constants

$$V_c$$

 $=$ 

$3b$

$$P_c$$

 $=$ 

$$\frac{a}{27b^2}$$

$$T_c$$

 $=$ 

$$\frac{8a}{27Rb}$$

**Value of  $V_c$  is not reliable** as it can't be measured properly

Determine van der Waals constants ('a' & 'b') using  $T_c$  &  $P_c$

# Liquid State

# Properties of Liquids



Have definite volume

1

2

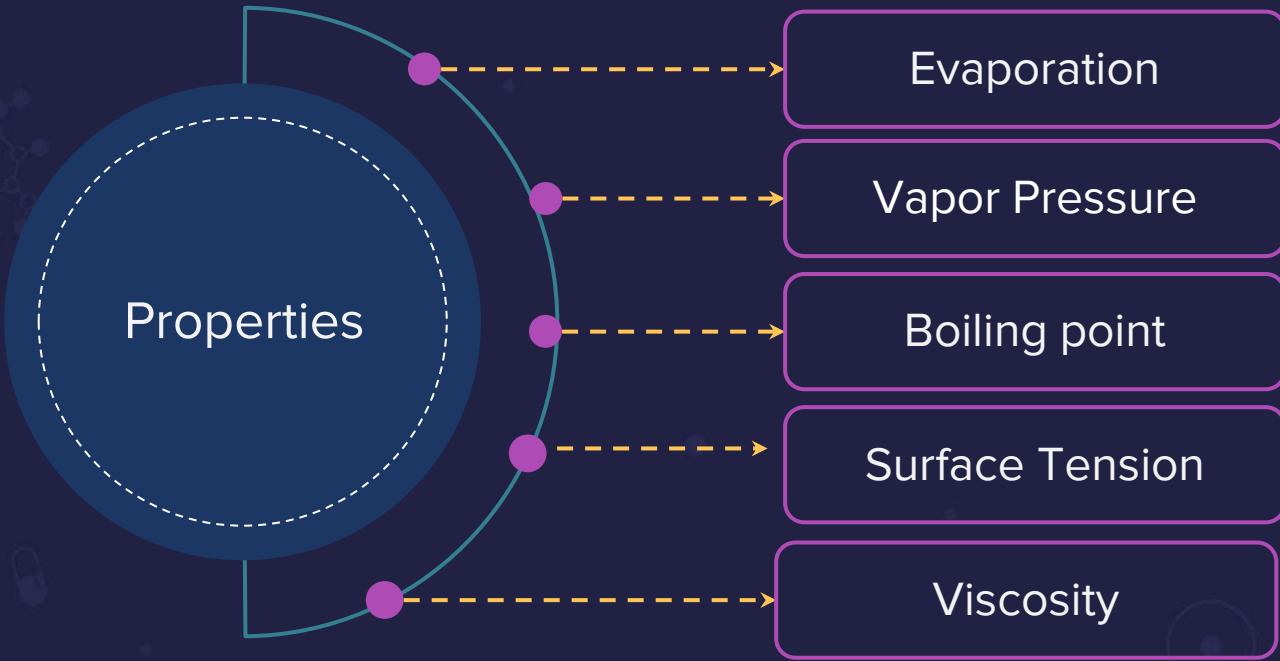
Can flow

3

Denser than gases

**Intermolecular forces** are stronger than in gaseous state and weaker than that in solid state

# Liquid State - Physical Properties



# Evaporation

Liquid → Vapor

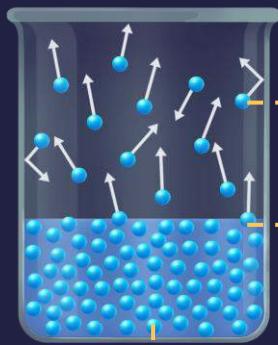


Below its boiling point

Molecules at the liquid's surface having **sufficient K.E.**

Escape into the vapor phase

# Evaporation

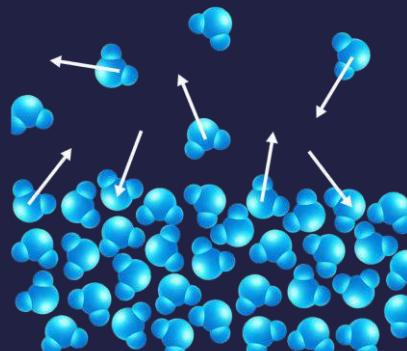


Gas particle

Particles with  
higher K.E. leaves  
the liquid surface

Liquid particles

Requires energy to **overcome** the  
**intermolecular forces** between  
the molecules of the liquid



# Vapor Pressure (V.P.)

**Pressure** exerted by the **vapors**  
over its liquid when it is in  
equilibrium with the liquid

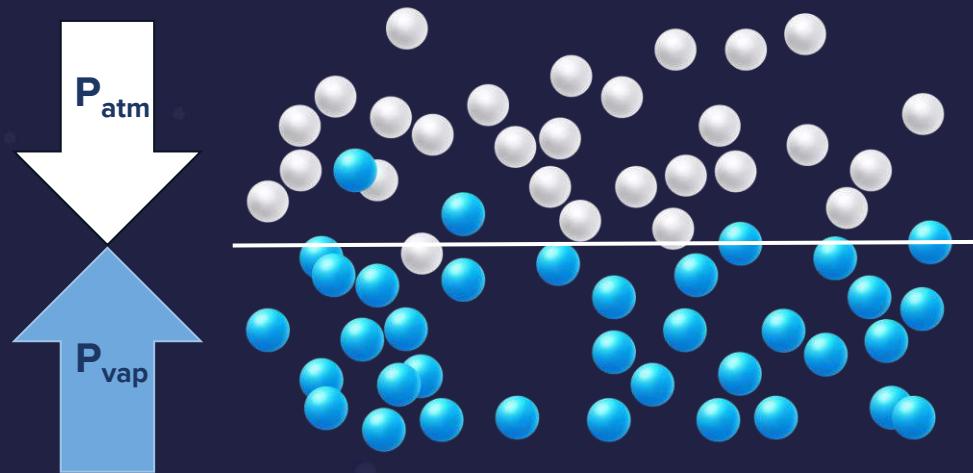


Initially, the molecules start going in vapour phase from the liquid surface but after some time some molecules start coming back to the liquid surface. At equilibrium, the number of molecules going from the surface and the molecules coming back becomes equal.

# Boiling Point

**Temperature** at which  
the vapour pressure  
of liquid is equal to  
the external pressure

# Boiling Point



$$P_{atm}$$

=

$$P_{vap}$$

# Surface Tension

**Surface tension** is defined as the force acting per unit length perpendicular to the line drawn on the surface of liquid.

Surface Tension( $\gamma$ )

=

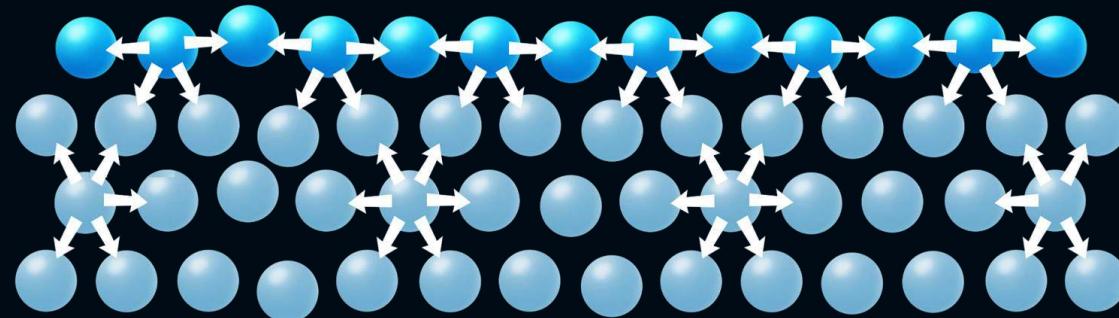
$$\frac{F}{L}$$

S.I Unit of  $\gamma$  :  $N\ m^{-1}$

The measure of **inward force** on the surface of the liquid. It tends to **minimize the surface area**.

# Surface Tension

**Surface molecule** : Net attraction into the liquid (downwards)



**Interior molecule** : Attracted in all directions

# Factors Affecting Surface Tension

Temperature ↑ Surface tension ↓

Intermolecular attractive forces ↑  
Surface tension ↑

# Applications of Surface Tension

Soaps and Detergents

Disinfectants

Industrial Processes

Human Health

# Viscosity

**Measure of resistance**  
to flow of a liquid



Arises due to the **internal friction** between the layers of the fluid while it flows

# Viscosity



Why does milk flow faster than honey?

Because of the difference in the intermolecular forces of attraction



More force of attraction in honey causes more viscosity as compared to milk.