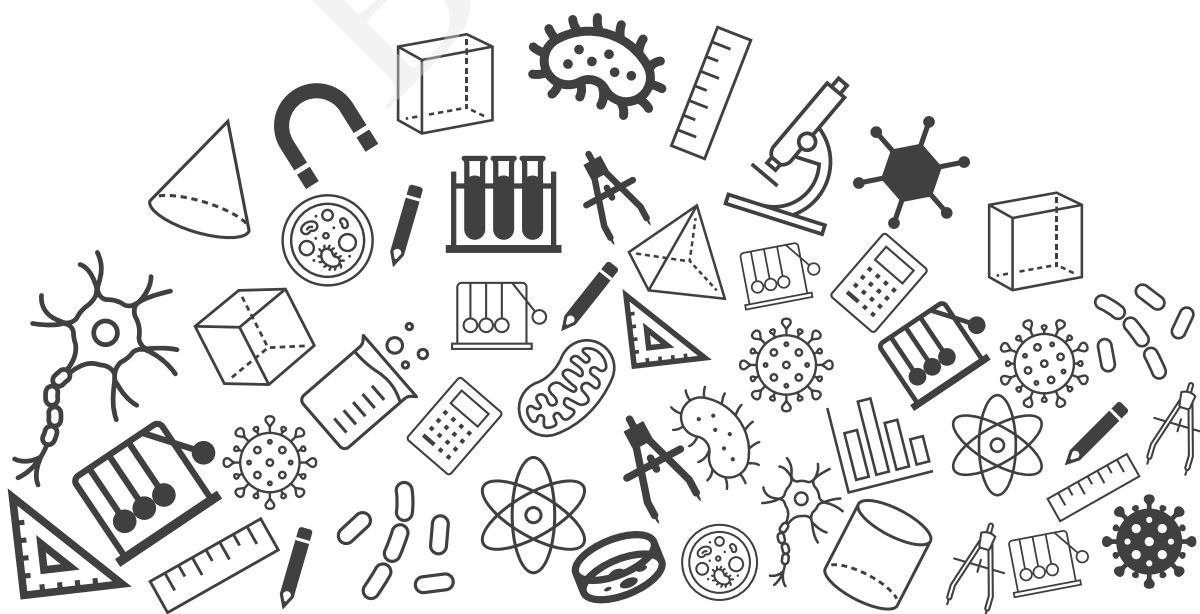




# Grade 10

## Mathematics Chapter Notes



# Pair of Linear Equations in Two Variables





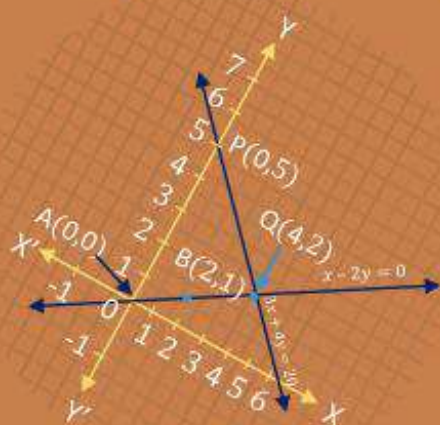
# Topics



1. General Form of a Linear Equation

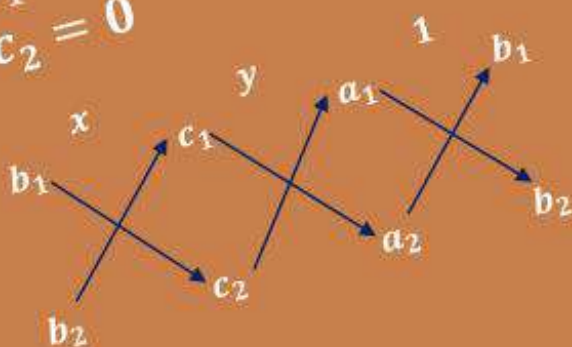
2. Types of Pairs of Linear Equations

3. Methods of Solving Pairs of Linear Equations



$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$



# 1. Linear Equations in Two Variables

## General Form

$$ax + by + c = 0$$

Diagram illustrating the components of the general form of a linear equation in two variables:

- Coefficients:**  $a$  and  $b$  (indicated by a green arrow pointing to  $a$  and  $b$ ).
- Variables:**  $x$  and  $y$  (indicated by an orange arrow pointing to  $x$  and  $y$ ).
- Constant:**  $c$  (indicated by a blue arrow pointing to  $c$ ).



where,  $a$  and  $b$  are non-zero real numbers

## Pair of Linear Equations in Two Variables

Consider two different equations in  $x$  and  $y$ ,

$$2x + 7y + 5 = 0$$

$$8x + 3y + 3 = 0$$

These two combined are known as pair of **linear equations** in two variables.

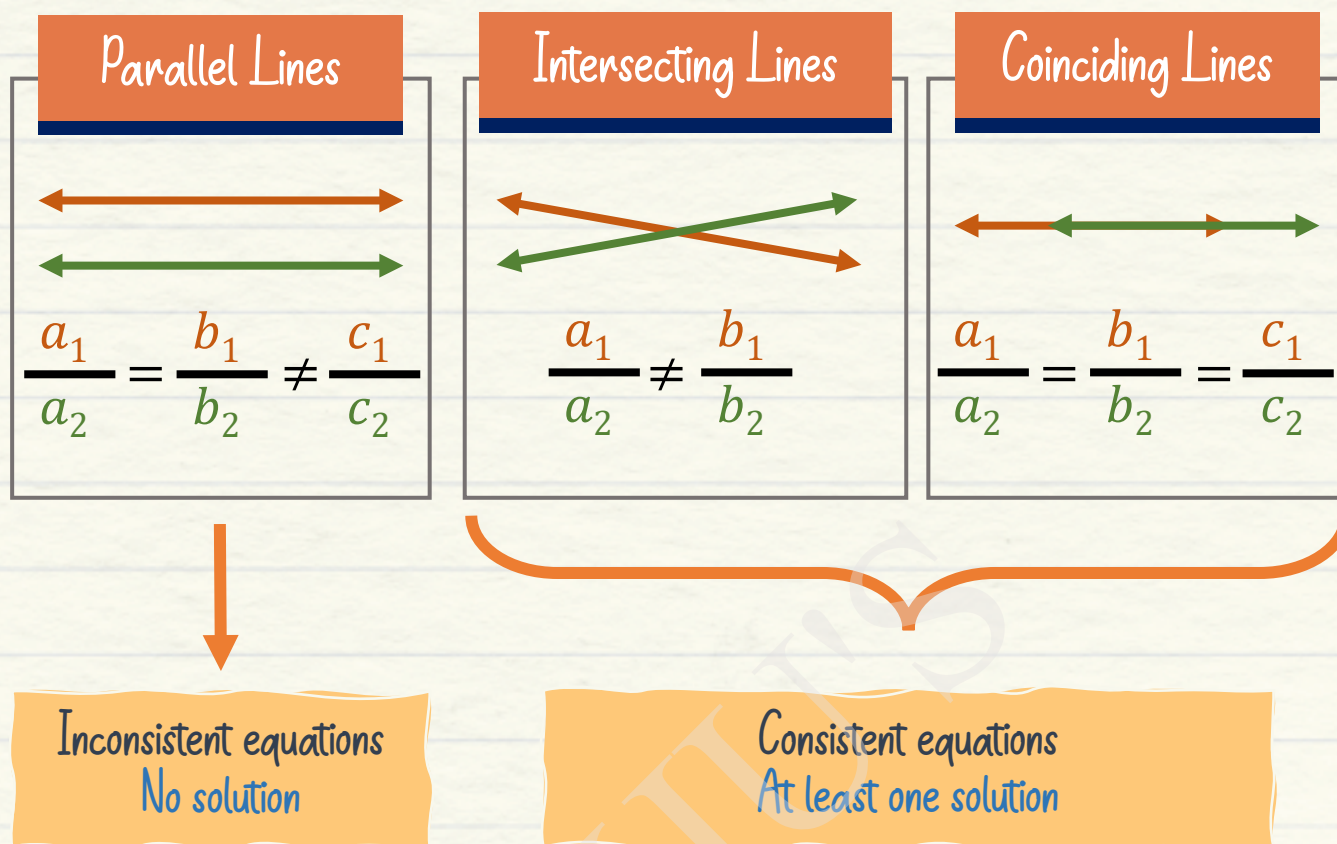
## General Form of Pair of Linear Equations in Two Variables

$$a_1x + b_1y + c_1 = 0$$

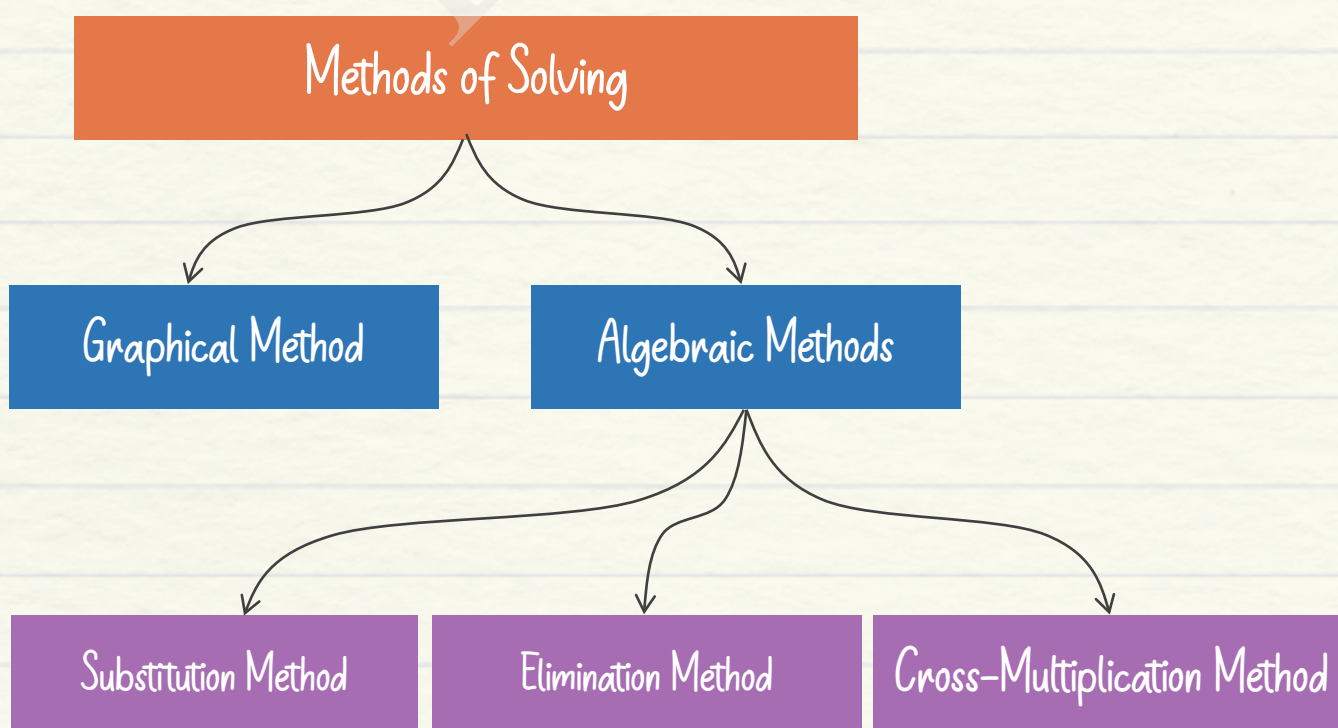
$$a_2x + b_2y + c_2 = 0$$



## 2. Types of Pairs of Linear Equations



## 3. Methods of Solving Pairs of Linear Equations



## 3.1 Graphical Method



$$2x - 1y = -1, \quad 3x + 2y = 9$$

Find points to construct lines on a graph paper for the two given equations

To construct a line, we need at least two point of the line, we find the value substituting values of  $x$  and  $y$  in the two equations.

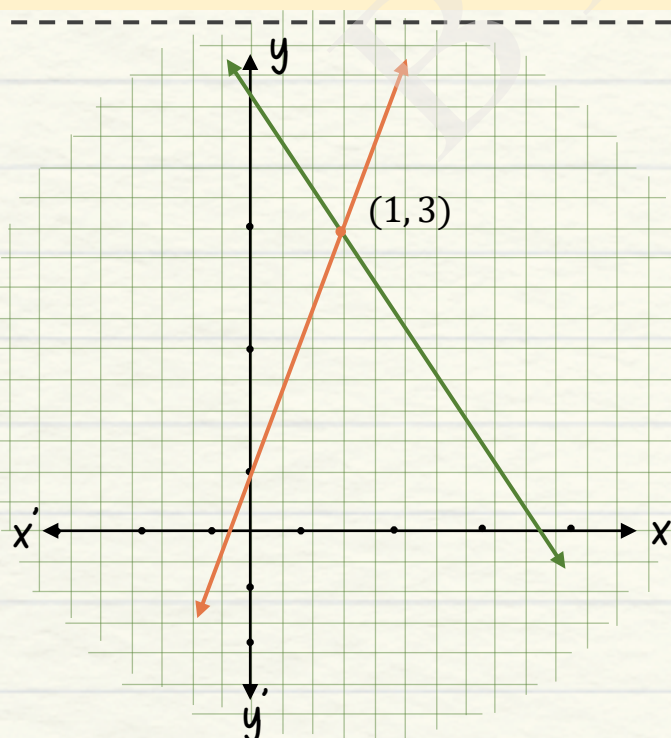
$$2x - 1y = -1$$

$x$	0	$-\frac{1}{2}$	1
$y$	1	0	3

$$3x + 2y = 9$$

$x$	0	3	1
$y$	$\frac{9}{2}$	0	3

Draw the two line on a graph and mark the points at which they intersect.



The  $x$ -coordinate and the  $y$ -coordinate of the point at which the two lines intersect is the solution(s) of the pair of equations.



## 3.2 Substitution Method



$$x + y = 4 \quad , \quad x - y = 2$$



Take one of the equations and move 'y' to LHS and the rest to RHS to get the value of 'y' in terms of 'x'.

$$y = 4 - x$$



Substitute the obtained value of 'y' in the other equation to get the numerical value of 'x'.

$$\begin{aligned} x - y &= 2 \\ x - (4 - x) &= 2 \\ 2x - 4 &= 2 \\ x &= 3 \end{aligned}$$



Now, substitute the obtained value of 'x' in either of the equations to get the value of 'y'.

$$\begin{aligned} x + y &= 4 \\ 3 + y &= 4 \\ y &= 1 \end{aligned}$$

## 3.3 Elimination Method



$$3x + 2y = 18, \quad 5x + 4y = 32$$

1

Note down equations aligned to respective variables as shown.

+3x	+2y	=	+18
+5x	+4y	=	+32

2

Pick the variable which will be easier to eliminate.

+3x	+2y	=	+18
+5x	+4y	=	+32

3

Equalise the coefficients of the variable to be eliminated by multiplying every term of the equation with the same number.

+3x	+2y	=	+18
$\times 2$	$\times 2$		$\times 2$
+5x	+4y	=	+32

4

Subtract the second equation from the first equation by reversing all the signs.

+6x	+4y	=	+36
-5x	-4y	=	-32
+x	+0y	=	+4

5

Substitute the value of the now known variable into the simpler equation to get the value of the other variable.

We know that,  
 $x = 4$   
 And,  $3x + 2y = 18$   
 $\Rightarrow 3 \times 4 + 2y = 18$   
 $\Rightarrow 12 + 2 = 18$   
 $\Rightarrow 2y = 6$   
 $\Rightarrow y = 3$

6

Verify the values obtained for  $x$  and  $y$  by putting them in the given equations

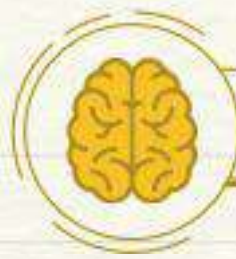
$$\begin{aligned} 3x + 2y &= 18, \\ \text{LHS} &= 3x + 2y \\ &= 3 \times 4 + 2 \times 3 \\ &= \text{RHS} \end{aligned}$$

$$\begin{aligned} 5x + 4y &= 32 \\ \text{LHS} &= 5x + 4y \\ &= 5 \times 4 + 4 \times 3 \\ &= \text{RHS} \end{aligned}$$



From the above,  $x = 4$  and  $y = 3$ .  
 Therefore,  $(4, 3)$  is the solution of the simultaneous equations  
 $"3x + 2y = 18"$  and  
 $"5x + 4y = 32"$ .





## Mind Map

